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Anticipative Generation and In-Situ Adaptation of Maneuvering Affordance in a Naturally Complex Scene

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1. Introduction

Computational resources combined with advanced mechanical systems rapidly expand the scope of ‘informatic vicinity’ (Kamejima, 2006) in which machine perception is delegated and networked to support human’s situation understanding and decision making. For instance, student knowledge can be expanded by space craft operated interactively from the classroom (Coppin et al., 2000). Final decisions on social safety in large scale natural disasters are determined mainly based upon information gathering and damage evaluation through network systems (Hamada & Fujie, 2001). Recent computer controlled vehicles, in particular, are developing the capability of understanding the situation for supporting human’s inherent maneuverability (Özgner & Stiller, 2007).

By expanding the scope of perception to satellite-roadway-vehicle network (Kamejima, 2008), we have an implementation of the informatic vicinity as shown in Fig.1. The latest Earth observation systems can provide a bird’s eye view for vehicles to identify themselves as consistent parts of the real world; current vision systems can analyze complex images captured at scene A to control a vehicle mechanism along the roadway specified in one frame of a specific satellite image (Urmson et al., 2009); and by using Global Positioning System (GPS), the vehicle can be localized within a small area in the satellite image in which the roadway pattern at scene A can be matched exactly and extended towards a possible goal, e.g. Scene B, prior to physical access (Kamejima, 2007). Therefore, the informatic vicinity can be exploited as a technological basis for the anticipative road following scheme. In addition, through the informatic vicinity, vehicles can mutually provide critical information for analyzing not-yet-accessible scenes, for example, precautionary safety information to human drivers and make effective predictions for machine vision as well.

As a consequence of evolution in the real world filled by uproarious illumination and reflection (Parker, 2003), the range of human’s perception is restricted to the physical-geometric perspective from a specific point of view. To facilitate human’s inherent perception in complex situations, the view from the vehicle should be located and oriented anticipatively in the informatic vicinity covering all possible transitions from the current scene. Such a cooperative system is expected to act as a substitute for essential parts of humans cognitive ability (Kamejima, 2008). As for playing an essential role in cooperative systems, however, the perceptive delegation is required to maintain on-going conformability.
with human capacity under the schematics of serious contradiction. In other words, subsequent maneuvering processes are anticipatively activated towards scenes beyond the horizon of human’s perception.

2. Existence of perceptual invariance

In a naturally complex scene, we are surrounded by optical flux modulating complete information that can afford to induce spontaneous maneuvering processes preestablishingly. For anticipative decision making, such affordance should be captured and transferred beyond the horizon of perception via a reconfiguration process; the a priori orientation of the roadway specified in the bird’s eye view should be mapped to the scene image via a posteriori adaptation of maneuvering processes. To this end, we introduce a fractal based representation of a roadway pattern in a naturally complex scene.

Fig. 2. Multi-Aspect Approach to Complex Scene
Following the collage theorem within the context of multi-fractal modeling (Barnsley, 2006), the expansion of the open space can be associated with the same class of self-similar patterns in multi-viewpoint imagery as illustrated in Fig.2. An approximation of roadway segment can be generated in satellite imagery as a ‘carpet’ (right aspect); this segment is mapped from the satellite image to associated scene images to yield a skewed ‘gasket’ (left aspect); through the multi-aspect access to a roadway, the perception process induces anticipative information into a part of the scene called the horizon of intension. This implies that fractal representation of a roadway pattern is transferable through the informatic vicinity as a common basis for mutual mediation of perceptive delegates. In what follows, the fractal coding scheme is introduced on an ineluctable information: noisy pattern covering really existing objects. By combining the randomness, we have robust fractal code for anticipative generation and in-situ adaptation of the maneuvering affordance.

3. Randomness-based approach

Suppose that the roadway is segmented in the bird’s eye view in terms of a sequence of vectors \( \{ v \} \) to be ‘downloaded’ in a scene image. With this anticipative segmentation, we can induce an aspect to be associated with the horizon of intention as shown in Fig.3 where the scope of perception is structured in the scene image in a stochastic sense; the belief on the open space is supported by a probability distribution \( \varphi_\rho \) confined by the estimate of the boundary \( \{ \varphi_\rho^+, \varphi_\rho^- \} \); within the horizon of control, the maneuvering process is guided to follow the boundaries under human’s spontaneous decision making; and, generated path \( \mathbf{x}^+ \) is extended towards the scope of perception as a stochastic process susceptive to not-yet-encountered uncertainties. Assume that the image of segment \( v \) is transferred via inter-viewpoint association and consider anticipative decision making problems in the information structure: how to project \( v \) in the observed scene; how to evaluate the depth and width of the open space; and, how to adapt the maneuvering process anticipatively to the open space.

![Fig. 3. Information Structure for Anticipative Decision](www.intechopen.com)
Let $\Omega$ be the projection of the vector $v$ into the image plane $\Omega = X \times Y$. From the viewpoint of ecological optics, a priori basis for spontaneous mobility is provided by random texture mapped onto an image plane $\Omega$. Let $f(\omega)$ be the brightness at the pixel $\omega \in \Omega$ and suppose that views of the objects to be detected are uniquely represented as subsets of $\Omega$ and identified within $\mathcal{F}$: the Borel field generated by the subsets of $\Omega$. In the totality of object images, then, we can introduce basic probability space $(\Omega, \mathcal{F}, P)$ where $P(\omega)$ is a uniform probability measure assigned to pixels $\omega$ without any a priori knowledge. By definition, $P(\omega)$ indexes a priori probability for the pixel $\omega$ to be a part of an object.

The a priori information is transferred to the observation $f(\omega)$ via complex physical, mathematical and cognitive processes. As for the physical complexity, we can utilize various results on geometric-chromatic investigations on optical information transmission. On the other hand, the mathematical complexity for assigning the pixel $\omega \in \Omega$ to a specific part of target object yields combinatorial explosion. However, without serious loss of generality, the combination of the existence theorem (Hutchinson, 1981) with ‘collage’ theorem (Barnsley et al., 1986) resolves the computational difficulty into the following non-deterministic representation:

$$\Xi = \bigcup_{\mu_i \in \nu} \mu_i(\Xi), \quad (1)$$

where $\Xi$ is a fractal version of the object image; $\nu$ denotes a fixed set of contraction mapping of size $||\nu||$:

$$\nu = \{\mu_1, \mu_2, \ldots, \mu_{||\nu||}\}, \quad \mu_i : \Omega \mapsto \Omega.$$  

In this representation, an attractor point $\xi \in \Xi$ can be mapped finally to the entire pattern $\Xi$ through a finite sequence of possible selection $\mu_i \in \nu$. By substituting the iteration of random selection $\mu_i$ in a fixed set $\nu$ for pattern association (1), we can identify constrained aggregation $\Xi$ with a trajectory of 2D stochastic processes driven by $\nu$. Due to the ‘whiteness’ in random selection $\mu_i \in \nu$, the expansion of the attractor $\Xi$ of geometric singularity can be visualized as a distribution $\chi_{\Xi}^p$ satisfying the following self-similarity

$$\chi_{\Xi}^p(\cdot) = \sum_{\mu_i \in \nu} p_{\mu_i} \chi_{\Xi}^{p-1}(\mu_i^{-1}\cdot), \quad (\cdot) \in \mathcal{F}, \quad (2)$$

with ‘coloring probability’ $\{p_{\mu_i}\}$ for selecting $\mu_i$ in fixed set $\nu$. The existence of the invariant measure implies the possibility for image based association $f \sim \chi_{\Xi}^p$.

Being given the invariant measure (2), we can evaluate the probability $\varphi(\omega|\nu)$ for capturing unknown fractal attractor $\Xi$ as the solution to the following equation (Kamejima, 2001):

$$\frac{1}{2}\Delta \varphi(\omega|\nu) + \rho[\chi_{\Xi}^p - \varphi(\omega|\nu)] = 0, \quad (3)$$

where $\rho = \log_2 ||\nu||$ denotes the complexity index of the imaging process (1) with (2). By this implicit dependence, the capturing probability $\varphi(\omega|\nu)$ can be generated prior to the specification of the mappings $\mu_i \in \nu$. 

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Define the stochastic feature \(\hat{\Theta}\) of fractal attractor \(\Xi\) as the totality of local maxima of the capturing probability \(\varphi(\omega|\nu)\), i.e.,

\[
\hat{\Theta} = \left\{ \hat{\theta} \in \Omega \mid \nabla \varphi(\hat{\theta}|\nu) = 0, \det \left[ \nabla \nabla^T \varphi(\hat{\theta}|\nu) \right] > 0, \Delta \varphi(\hat{\theta}|\nu) < 0 \right\},
\]

(4)

On this discrete set, we can verify the consistency of the mapping set \(\nu\) through the following computational test:

\[
\Theta = \left\{ \theta \in \hat{\Theta} \mid \exists \mu_1 \in \nu : \quad \mu_1^{-1} \left( \theta \right) \in \Theta \right\}.
\]

(5)

By definition, the following random process

\[
\xi_{t+1} = \mu_t(\xi_t), \quad \xi_0 = \theta,
\]

(6)

expands a point \(\theta \in \Theta\) towards the fractal attractor \(\Xi\) successively. Therefore, the connectedness of the point set \(\hat{\Theta}\) can be indexed in terms of the distribution of the invariant subset \(\Theta\) within \(\hat{\Theta}\). This provides a computational basis for the detection and connectedness analysis of the fractal model \(\nu\). Figures 4 and 5 demonstrate the detectability of fractal

Fig. 4. Detection of Fractal Model in Noisy Background

(a) Noisy Observation of \(\chi^p\)
(b) Capturing Probability \(\varphi(\omega|\nu)\)
(c) Invariant Feature \(\Theta\)
(d) Fractal Attractor Regenerated by \(\Theta\)
models. In these figures, noisy observations of fractal attractors (a) are identified with the measure $\chi^P_\Sigma$ to generate the capturing probability $\varphi(\omega|\nu)$ visualized as (b); from the stochastic feature $\Theta$ detected via local analysis of smooth distribution $\varphi(\omega|\nu)$, the invariant feature $\Theta$ is extracted as closed links (c); the existence of the invariant feature $\Theta$ activates the 2D random process (6) to visualize connected spaces (d). Therefore, we can restore known fractal models corrupted in noisy observation.

Fig. 5. Detection of a Fractal Model in Noisy Background

Considering the generic rule for associating the not-yet-identified invariant set $\chi^P_\Sigma$ with observed distribution $f(\omega)$, let a scene indicated in Fig.6 be observed by a viewer with the intentional coordinate system illustrated in Fig.7. By applying a 2D Laplacian filter to the scene, we can extract the noise component which can be utilized as a robust feature of the roadway image. Through the perspective projection, the power spectrum evaluated at the baseline of $\Delta f$-image (Fig.8) is expanded in accordance with the line shift towards the vanishing point as shown in Fig.9. Therefore, we can generate a generic representation of an open space in terms of scale information supported by the micro-structure of a roadway area.

Following a multi-scale approach (Jones & Taylor, 1994), the brightness distribution $f(\omega)$ can be decomposed into a function space consisting of class $\mathfrak{F} = \{ f_\sigma, \sigma > 0 \}$ given by
$g_{\sigma}$ is a 2D Gaussian distribution with variance parameter $\sigma$; $b$ stands for the aggregation of low frequency components such as $|\Delta b| \ll |\Delta g|$. By identifying the measure with an aggregation of ‘point images’, we can extract component images with specific scales as shown in Fig. 10, where a set of $\Delta g$-filter with 2D transfer function (see Fig. 11) is applied to the point image concentrated at the origin. Noticing the similarity of $\Delta g$ and $g_{\sigma}$ filters near the origin, we have the following local estimates for the scale information $\hat{\sigma}$ at $\omega$ (Kamejima, 2005):

$$f_{\sigma}(\omega) \sim g_{\sigma} * \chi^{\sigma}_{\omega}(\omega) + b(\omega),$$

where $g_{\sigma}$ is a 2D Gaussian distribution with variance parameter $\sigma$; $b$ stands for the aggregation of low frequency components such as $|\Delta b| \ll |\Delta g|$. By identifying the measure with an aggregation of ‘point images’, we can extract component images with specific scales as shown in Fig. 10, where a set of $\Delta g$-filter with 2D transfer function (see Fig. 11) is applied to the point image concentrated at the origin. Noticing the similarity of $\Delta g$ and $g_{\sigma}$ filters near the origin, we have the following local estimates for the scale information $\hat{\sigma}$ at $\omega$ (Kamejima, 2005):

$$\hat{\sigma}(\omega) \sim 2\sqrt{|f(\omega)|/|\Delta f(\omega)|}.$$ 

Let $\omega_0$ be the maximal scale associated with the noise component and define $d$ as the depth parameter indexed along the ‘direction of intention’ $\hat{\xi}^{d}$, the perspective projection of the orientation vector $\nu$ on the scene image. Here we have the following representation of the ‘generic’ roadway model $\mathcal{M}(\hat{\xi}^{d}, \chi^{\omega}_{\omega})$: 

$$\hat{\sigma}(\omega) \sim 2\sqrt{|f(\omega)|/|\Delta f(\omega)|}.$$ 

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$$\hat{\sigma}(\omega) \sim 2\sqrt{|f(\omega)|/|\Delta f(\omega)|}.$$
In (9a), the expansion of the roadway is identified with a pattern \( \Xi \in \mathcal{F} \) in which scale information \( \sigma_n \) is regulated by the linear diminishing rule from the bottom of the maneuvering affordance \( d_0 \) to the vanishing point \( d_\infty \). Hence, we can conclude that the scope of perception is confined in a probabilistic sense (9b) where the estimated distribution \( \lambda^P_\Xi \) can be utilized as a ‘noisy’ observation of the self-similarity (1).

4. Fractal coding of perceptual invariance

Via the self-similarity process (1), an attractor point \( \xi \) is allocated to satisfy the following constraint with respect to the not-yet-identified contraction mapping \( \mu_i \in \nu \):

\[
(10)
\]
where $\omega_{f}^{\mu}$ denotes the fixed point of $\mu$. By evaluating the attractive force within the framework of the Hausdorff topology (Kamejima, 1999), we can introduce a simultaneous estimation scheme for model parameters $(d_{\omega}, \tilde{\Omega}^{\phi})$ with non-unique estimates of fixed points $\Omega_{f}^{\mu}$ associated with not-yet-identified contraction mapping $\mu_{f}$. To apply the articulation scheme (10) with non-deterministic kinetics, first, a pixel $\omega \in \Omega$ is associated with not-yet-identified attractor $\Xi$ in a stochastic sense. Once we have observed the invariant measure $\chi_{\Xi}^{\mu}$, we can evaluate the probability $\varphi(\omega|\nu)$ for capturing unknown fractal attractor $\Xi$ as the solution to the following equation:

$$\frac{1}{2} \Delta \varphi(\omega|\nu) + \rho[\chi_{\Xi}^{\mu} - \varphi(\omega|\nu)] = 0.$$  

(11)

Following this, the image plane is partitioned in accordance with the fractal attractor to be detected. Since various types of attractors are simultaneously observed as object images (Barnsley, 2006) in practical imagery, generated information $\varphi(\omega|\nu)$ is expanded to cover noisy patterns as well. To confine the distribution into a target attractor, let the initial guess for the fixed points $\tilde{\Omega}^{\mu} = \{\tilde{\omega}_{f}^{\mu}\}$ be given as a perspective of the segment $v$ and consider the articulation $\Omega \rightarrow \{\Lambda_{i}\}$ as illustrated in Fig. 12:

$$\Lambda_{i} = \left\{ \omega \in \Omega \mid |\omega - \tilde{\omega}_{f}^{\mu}| < |\omega - \hat{\omega}_{f}^{\mu}|, \quad \text{for} \quad \hat{\omega}_{f}^{\mu} \neq \tilde{\omega}_{f}^{\mu} \right\},$$

with statistical moments $(\tilde{\omega}_{i}, \Sigma_{i})$ conditioned by $\nu$:

$$\int_{\Lambda_{i}} (\omega - \tilde{\omega}_{i}) \varphi(\omega|\nu) dP(\omega) = 0,$$

$$\Sigma_{i} = C_{i} \int_{\Lambda_{i}} (\omega - \tilde{\omega}_{i})(\omega - \tilde{\omega}_{i})^{T} \varphi(\omega|\nu) dP(\omega),$$

where $C_{i}$ denotes the normalization constant. In this articulation, the expansion of the domains $\Lambda_{i}$ is indexed in terms of the following ‘Laplacian-Gaussian basin’:

$$\Lambda_{i}^{\phi} = \left\{ \lambda \in \Lambda_{i} \mid \left( \frac{1}{2} \lambda^{T} \Sigma_{i}^{-1} \lambda - 1 \right) < 0 \right\}.$$  

(12)

In such a basin $\Lambda_{i}^{\phi}$, we have the following circumscribing polygon within the context of statistical clustering:

$$\left( \tilde{\Omega}_{i}^{\phi} \right)^{T} R(\pi/2) \left( \partial_{\omega} - \hat{\omega}^{\mu}_{f} \right) = 0,$$  

(13a)

$$\left( \tilde{\Omega}_{i}^{\phi} \right)^{T} R(\pi/2) \left( \hat{\omega}_{f} - \hat{\omega}_{j} \right) = 0,$$  

(13b)

where $\partial_{\omega}$ is the contact point with $\Lambda_{i}^{\phi}$, $\tilde{\Omega}_{i}^{\phi}$ and $\hat{\Omega}^{\phi}_{i}$ are unit vectors associating the fixed point $\hat{\omega}_{f}^{\mu}$, with $\hat{\omega}_{j}$, and $\hat{\omega}_{j}$, respectively; $R$ denotes the rotation matrix. By adjusting $\partial_{\omega}$ to the boundary of the Laplacian-Gaussian basin (12) along the external normal vector $\tilde{\Omega}_{i}^{\phi}$, we have the following adaptation scheme of the fixed point estimate:
Anticipative Generation and \textit{In-Situ} Adaptation of Maneuvering Affordance

In this scheme, the fixed points \{\tilde{\omega}^f_{\mu_j}\} are mutually separated by the expansion of the Laplacian-Gaussian basins (12); on the other hand, the expansion of the fractal attractor to be generated is confined in terms of the contact points \{\partial_{\omega}\}. As a result of this antagonistic dynamics, the update \(d\tilde{\omega}^f_{\mu_j}\) are coordinated via the integration rule:

\begin{align}
    d\tilde{\omega}^f_{\mu_j} &= -\kappa \phi_j (\tilde{\omega}^f_{\mu_j} - \tilde{\omega}_j), \\
    \phi_j &= \frac{1}{2} (\partial_{\omega} - \tilde{\omega}_j)^T \Sigma_j^{-1} (\partial_{\omega} - \tilde{\omega}_j) - 1, \\
    \partial_{\omega} - \tilde{\omega}_j &= -Q_j^{-1} K_{ij} (\tilde{\omega}^f_{\mu_j} - \tilde{\omega}_j), \\
    Q_j &= (\tilde{\Omega}_{ij}^T)^T \Sigma_j (\tilde{\Omega}_{ij}^T), \\
    K_{ij} &= \Sigma_j (\tilde{\Omega}_{ij}^T)^T (\tilde{\Omega}_{ij}^T)^T.
\end{align}

In this scheme, the fixed points \{\tilde{\omega}^f_{\mu_j}\} are mutually separated by the expansion of the Laplacian-Gaussian basins (12); on the other hand, the expansion of the fractal attractor to be generated is confined in terms of the contact points \{\partial_{\omega}\}. As a result of this antagonistic dynamics, the update \(d\tilde{\omega}^f_{\mu_j}\) are coordinated via the integration rule:

\begin{equation}
    \sum_j |\phi_j| \rightarrow \min.
\end{equation}

The statistical clustering is followed by geometric design and computational verification of mapping set \(\tilde{\nu} = \{\tilde{\mu}_i\}\). The self-similarity indicated in Fig.2 combined with the fixed point assignment yields the following description:

\begin{equation}
    \tilde{\nu} \ni \tilde{\mu}_i(\omega) : \quad \mu_i(\omega) = \frac{1}{2} (\omega + \tilde{\omega}^f_{\mu_i}), \quad p_{\mu_i} = \frac{1}{3}.
\end{equation}

The consistency of fixed point allocation \(\tilde{\Omega}^f\) should be verified by the self-similarity analysis of the mapping set \(\tilde{\nu}\) on the fractal attractor to be detected. To this end, we introduce the following computational test on a stochastic representation of the not-yet-identified \(\Xi\) (Kamejima, 2001):

\begin{figure}
\centering
\includegraphics[width=\textwidth]{fig12.png}
\caption{Laplacian-Gaussian Basin}
\end{figure}
Proposition 1 Let $\nu^\rho_\Theta$ be an invariant measure with respect to the mapping set $\nu$. Suppose that $\Theta$ is extracted from the capturing probability $\varphi(\omega|\nu)$ associated with $\nu^\rho_\Theta$. Then there exists the invariant feature $\Theta \subset \hat{\Theta}$ satisfying the following constraint

$$
\Theta = \left\{ \theta \in \hat{\Theta} \mid \exists \tilde{\mu}_\theta \in \nu : \tilde{\mu}_\theta^{-1}(\theta) \in \Theta \right\}.
$$

(17)

The existence of invariant features $\Theta$ implies that the range of designed imaging process $\nu$ can generate a version of a fractal attractor indicating a connected open space in the roadway area. The combination of equations (9), (11), (12), (14), (17) provides a computational basis for the coding of self-similarity of complex random patterns.

5. In-situ adaptation via ground-object separation

By identifying the vanishing point $\omega_v = (d_v, \xi)$ with a fixed point estimate $\hat{\omega}_v$, the generic model (9) induces a geometric structure into the scene image as shown in Fig. 13. A pixel in a Laplacian-Gaussian basin $\omega$ is non-deterministically attracted to one of the fixed points in $\hat{\omega}_v$ due to the generativity of the self-similarity process. Despite non-deterministic allocation, the structural consistency of the set $\hat{\omega}_v$ is verified by the existence of the capturing probability $\varphi(\omega|\nu)$ supporting invariant subset $\Theta$. Let $\hat{\xi}$ be the nearest point to the estimate of $\omega_v$ in the invariant subset $\Theta$. By using the point $\hat{\xi}$, we can specify the horizon of control as well as the depth of the boundary information $(b_L, b_R)$ to be marked in the scene image. Therefore, the generic model (9) combined with fractal coding yields an estimate of the roadway area prior to object identification.

Furthermore, we can design another generic model on the scale space information (8) to detect something perpendicular to the roadway. For this purpose, the mismatch with the generic model (9) is evaluated in terms of the following measure:

$$
p(\omega^1|\omega) = \frac{1}{\sqrt{2\pi \sigma^2}} \exp \left[ \frac{|\hat{\sigma}_\omega^1 - \hat{\sigma}_\omega|^2}{2\sigma^2} \right],
$$

(18)

where $\omega$ denotes a pixel selected in the domain confined by the boundary information $(b_L, b_R)$ and $\hat{\xi}^\omega = (\omega_v, \omega_{\nu,dy})$ is the upward extension of the pixel with the vertical interval $dy$. This pixel wise evaluation is chained to visualize not-yet-identified objects as follows:

$$
\chi_{<\omega>} \sim \prod_{\omega \in <\omega>} p(\omega^1|\omega) \cdot \varphi(\omega^1|\nu),
$$

(19)

$$
<\omega> = \cdots (\omega_x, \omega_{y+ndy}) \cdots,
$$

where $<\omega>$ denotes the vertical chain of pixels with bottom $\omega_1$ to be grounded on the maneuvering affordance. The first term of this evaluation indicates the length of the vertical chain; and the second term indexes the probability for the chain to ground somewhere in a plane supporting the roadway area. In equation (19), the probability for the segment $<\omega>$ to be a part of the object is evaluated as the ‘breakdown’ of the generic model to induce linear scale shift in the scene image.

As shown in equations (9) and (18), roadway area and object images are separated as generic models based on as-is information $\hat{\sigma}_\omega$. Noting that the connectedness of the detected roadway area is verified as the existence of a fractal attractor, we can utilize the aggregation
Fig. 13. Fractal Coding of Laplacian-Gaussian Basin

of grounding pixels ω_j as an estimate of the boundary of the roadway area confined by a distribution of ‘obstacles’ to be analyzed in the scene. Hence, we have the following computational scheme for object-ground separation:

- Fractal structure of maneuvering affordance is extracted in terms of 2D allocation of fixed points \( \hat{\Omega} f = \{ \omega_f^p \} \).
- The imaging mechanism of the randomness distribution \( \chi^p_{\hat{\xi}} \) is designed in terms of mapping set \( \hat{\nu} \) through simultaneous estimation of discrete information \( \hat{\Omega} f \) and induced 2D field \( \varphi(\omega|\nu) \).
- The integrity of decentralized estimate \( \hat{\Omega} f \) is visualized as associated attractor \( \Xi \) generated by using the imaging process parameter \( \hat{\nu} \) on the brightness distribution \( f(\omega) \).
- Self-similarity of the imaging process parameter \( \hat{\nu} \) based on the estimate \( \hat{\Omega} f \) is verified via computational generation of invariant subset \( \Theta \) on the local maxima \( \hat{\xi} \) a pattern sensitive sampling of smooth field \( \varphi(\omega|\nu) \).
- As a stochastic basis of the maneuvering affordance, the scale information \( \hat{\sigma}_p \) provides complementary information; noisy observation of an open space \( \chi^p_{\hat{\xi}} \) with the distribution of the breakdown \( p(\omega|\nu) \).
- The boundary of maneuvering affordance can be detected through the aggregation of as the breakdown as 1D imagery \( <\omega> \).

The mapping set \( \hat{\nu} \) can be designed non-uniquely on the estimate of fixed points \( \hat{\Omega} f \). Such non-unique representation provides computational basis for decentralized perception. The geometry of the maneuvering affordance is transferable via multi-viewpoint imagery and reconfigurable through dynamic interaction with the scene.

The mechanism for the multi-viewpoint integration is illustrated in Fig.14; based on a priori information \( v \) in the bird’s eye view, the direction of the roadway \( \hat{\Omega} f \) is transferred to the scene image to specify an initial guess of fixed points \( \hat{\Omega} f \); by articulating the capturing probability \( \varphi(\omega|\nu) \) into the Laplacian-Gaussian basin \( \{ \Lambda^p_{\nu} \} \), a fractal model is designed in terms of mapping set \( \hat{\nu} \); the fractal model is verified via computational detection of invariant feature \( \Theta \) and adapted to the as-is distribution of boundary objects via ground-object separation.
6. Experiments

Let a fixed point of the Gasket be associated with the vanishing point with a depth parameter $d_\infty$ and suppose that the rest of the fixed points are allocated at both bottoms of the roadway image where maximum scale of random patterns $\sigma_{\text{max}}$ may be detected. By introducing this initial guess, the equations (8) – (17) can be solved via the iteration process:

$$\{\hat{\omega}_m^f\} \rightarrow (8) \rightarrow (9) \rightarrow (11) \rightarrow (12) \rightarrow (14) \rightarrow (17) \rightarrow \{\hat{\omega}_m^f\} \cdots$$

(20)

Steady state of the iteration process applied on a scene image is indicated in Figs.15 – 18. As an initial guess for starting the iteration (20), the set $\{\hat{\omega}_m^f\}$ is assigned in a scene image displayed in Fig.15; three fixed points are allocated at top-center, left- and right bottom for specifying upper vertex and left-right vertexes of a ‘gasket’ pattern; as the result of the iteration (20), a mapping set with three fixed points $\{\hat{\omega}_m^f\}$ is designed as a generator of a priori gasket model. The a priori fractal model based on the fixed point estimates generates the fractal attractor indicated in Fig.16. In this case, the scale of distributed randomness is limited by $\sigma_0 = 2 \cdot \sigma_{\text{min}}$. The mapping set $\hat{\nu}$ associated with the gasket model is verified via finite self-similarity analysis as indicated in Fig.17; the consistency of the fractal attractor to be generated is computationally tested via the generation of an invariant subset $\Theta$ and indicated as a closed link on a representation of ‘most probable’ attractor points $\hat{\omega}$. By the existence of $\Theta$, the consistency of the measure $\chi^P_\Xi$ with the randomness distribution is verified as well as the self-similarity of associated attractor $\Xi$ visualized in Fig.18. Thus, the estimate of the vanishing point $(d_\infty, \hat{\omega}^d)$ is verified to be consistent with the generic model (9).

In complex scenes where the maneuvering area is clearly indicated as a lane mark as shown in Fig.18, designed mapping set $\hat{\nu}$ specifies the boundary of the fractal model $(b_L, b_R)$. Such boundary information is critical in the road following processes. In many practical situations, the boundary is obscured by sign patterns and occluded by obstacles as indicated in Fig.6. In such a scene, we can define the boundary of open space via ground-object separation. To this end, first, the scale shift of distributed randomness was matched with the generic model (9) to design a version of fractal code $\hat{\nu}$. The designed code was verified via a computational consistency test and visualized as shown in Fig.19. By the existence of the
fractal attractor, the validity of the designed version of fractal code $\hat{\rho}$ was verified as well as the perceptual consistency of the generic model. Hence, we can activate the ground-object separation process; the generic model (9) was applied to the entire scene image; the pixels of inconsistent scale estimate $\hat{\sigma}(\omega)$ were extracted and chained in the scene image as shown in Fig. 20. As shown in this figure, resultant chains can separate the image of something perpendicular to the open space supporting the generic rule: the linear scale shift due to perspective projection. Thus, we can define a version of an effective boundary as the vertical chain of the breakdown points with the length over the noise scale: $|| \omega || \geq \delta_{\min}$. To confine the fractal model $\nu$ within the open space, we re-assign the fixed points $\Omega f = \{ \hat{\omega}_j^k \}$ and re-activate the design process. The obtained fractal model was visualized in the scene image as shown in Fig. 21. This figure demonstrates that the fractal coding of maneuvering
Fig. 17. Computational Verification

Fig. 18. Road Following Process

Fig. 19. Associated Fractal Attractor
Fig. 20. Object Separation Based on $\hat{\sigma}_x$-Model

Fig. 21. Fractal Sampling

affordance with breakdown detection yields plausible reference for the visual guidance along a perceptually boundary in a naturally complex scene. Through these experimental studies, it was demonstrated that the anticipative road following results in the bird’s eye view can be applied to an extended class of roadway scenes as an a priori model. This implies that the design-and-refine steps of fractal coding can be applied to scenes consisting of objects covered by scale and chromatic randomness. This condition is satisfied in naturally complex scenes consisting of worn-out objects on which microscopic damage is expected to be uniformly distributed.

7. Concluding remarks

Fractal representation of the maneuvering affordance has been introduced on the randomness ineluctably distributed in naturally complex scenes. Scale shift of random patterns was extracted from scene image and matched to the a priori direction of a roadway. Based on scale space analysis, the probability of capturing not-yet-identified fractal
attractors is generated within the roadway pattern to be detected. Such an in-situ design process has been demonstrated to yield anticipative models for road following process. The randomness-based approach yields a design framework for machine perception sharing man-readable information, i.e., natural complexity of textures and chromatic distributions. This implies that the fractal roadway model can be used for mental load reduction through human-machine cooperation.

8. References

Rapid advances in the field of robotics have made it possible to use robots not just in industrial automation but also in entertainment, rehabilitation, and home service. Since robots will likely affect many aspects of human existence, fundamental questions of human-robot interaction must be formulated and, if at all possible, resolved. Some of these questions are addressed in this collection of papers by leading HRI researchers.

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