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1. Introduction

Polycrystalline silicon thin-film transistors (poly-Si TFTs) have recently attracted considerable attention for their high field-effect mobility and response velocity [1,2]. For low fabrication cost, poly-Si TFTs should be made on inexpensive glass substrates. In order to lower the crystallization temperature of amorphous silicon (a-Si) below the intrinsic crystallization temperature (~600 °C), effects of metal impurities on crystallization have been investigated using Au [3], Al [4], and Sb [5] forming eutectics with Si, and Pd [6] and Ni [7] forming silicides with Si. This process is referred to as metal-induced crystallization (MIC). Following the MIC, its variants, such as the metal-induced lateral crystallization (MILC) [8] and the field-aided lateral crystallization (FALC) [9–12], have been introduced as attempts to lower crystallization temperature and to reduce the contamination by a metal catalyst. For the MILC process, the flux of the diffusing species is governed only by the concentration gradient, but for the FALC process, the flux can be affected by not only the concentration gradient but also the applied electric potential gradient. In the FALC process, the crystallization front typically migrates from the negative electrode side to the positive electrode side. In the FALC, the application of a DC electric field increases the crystallization rate, as compared with the MILC (without any electric field) and MIC. In the FALC process, Ni and Cu, both of which are silicide forming metals, have been reported to produce high crystallization rates [12]. The mechanism of the crystallization induced by Ni was examined in detail by Hayzelden and his coworkers [13, 14] using in situ transmission electron microscopy (TEM) and high-resolution TEM.

The a-Si films are generally deposited on glass by physical or chemical vapor deposition. When annealed, they undergo crystallization by nucleation and growth. For the solid-phase crystallization of a-Si films on glass by heating, the directed crystallization, in which crystallization is favored in special crystallographic directions of crystallites, is not easily expected because both a-Si and glass are physically isotropic. However, the directed crystallization is rather general in the solid-phase crystallization of a-Si on glass at low temperatures [8,15–19]. Lee et
al. [8] advanced a model for the directed crystallization and later the model was further refined [20,21]. The model is introduced and is applied to the solid-phase epitaxial growth rate of c-Si in self-implanted Si(100) wafer, the solid-phase epitaxial growth rate of c-Si in self-implanted Si(100) wafer [22,23], the metal-induced crystallization of a-Si film on glass, and the silicide mediated crystallization.

2. Directed crystallization theory

The solid-phase transformation of a metastable amorphous material into a crystal, or the solid-phase crystallization of an amorphous material, needs the activation energy. The energy is usually supplied in the form of thermal energy by increasing the temperature of the material. When the nucleation occurs, the strain energy develops in the amorphous matrix as well as in the crystallites. The strain energy may be referred to as the accommodation strain energy. The strain energy is likely to give rise to inhomogeneous growth rates of crystallites due to their elastic anisotropy, if any. We discuss the evolution of the strain energy qualitatively [20,21].

The stress state of thin film deposits can be approximated by plane stress because the principal stress normal to the film surface is negligibly small compared with those along the surface. We consider a circular disk cut from a large, elastically isotropic metastable-phase sheet. When the disk is transformed into its stable phase, its dimension is likely to differ from the original diameter of the metastable phase due to a difference in density between the two phases. If the stable phase is elastically isotropic, the stable disk will be circular. When the density of the stable phase is higher than that of the metastable phase, the diameter of the stable-phase disk is smaller than that of the metastable phase, and vice versa. When the ends of the two phases are pulled toward each other and joined together, the strain and stress fields develop in the both phases.

In order to obtain the stress distribution of this system, we first adopt the solution of the stress distribution in a hollow cylinder subjected to uniform pressure on the inner and outer surfaces (Figure 1). The solution of this problem is due to Lamé and expressed as follows [22]:

\[
\sigma_r = \frac{a^2b^2(p_i - p_o)}{(b^2 - a^2)r^2} + \frac{p(a^2 - p)b^2}{b^2 - a^2} \tag{1}
\]

\[
\sigma_\theta = \frac{a^2b^2(p_i - p_o)}{(b^2 - a^2)r^2} + \frac{p(a^2 - p)b^2}{b^2 - a^2} \tag{2}
\]

where \(\sigma_r\) and \(\sigma_\theta\) denote the normal stress components in the radial and circumferential directions, and \(p_i\) and \(p_o\) the uniform internal and external pressures. Other symbols are defined in Figure 1. This solution is useful because it gives the stress distribution in the region
of $a < r < b$, which may be equivalent to the metastable region in the present case. When the cylinder is subjected to internal pressure only, $p_o = 0$, with $b >> a$, Eqs. 1 and 2 give

$$\sigma_r = \frac{a^2 p_i}{b^2} \left(1 - \frac{b^2}{r^2}\right)$$

(3)

$$\sigma_\theta = \frac{a^2 p_i}{b^2} \left(1 + \frac{b^2}{r^2}\right)$$

(4)

These equations show that $\sigma_r$ is always a compressive stress and $\sigma_\theta$ a tensile stress. If the cylinder is subjected to uniform internal tensile stress only, $p_i < 0$, $\sigma_r$ is always a tensile stress and $\sigma_\theta$ a compressive stress. This is relevant to the case when the density of the stable phase is higher than that of the metastable phase, as in crystallization of a-Si. The magnitude of $\sigma_r$ and $\sigma_\theta$ are maxima at $r = a$, decreasing with increasing $r$ regardless of internal pressure or internal tensile stress.

When the stable phase is elastically anisotropic, the pulling displacement of the circumference of the stable phase depends on its stiffness, the stiffer the smaller displacement at a given force. The smaller displacement of the stable phase requires the larger pulling displacement of the metastable phase, which induces the higher strain energy in the metastable phase.

![Figure 1. Hollow cylinder subjected to uniform pressure.](http://dx.doi.org/10.5772/59723)
A qualitative account of this can be made using rectangular elements shown in Figure 2(a). The elements may be approximated by uniaxial specimens with fixed ends as shown in Figure 2(b). Let the metastable phase be elastically isotropic and its stiffness be $C_m$. If the stable phase is an elastically anisotropic single crystal, its stiffness is likely to vary with its crystallographic direction. $C_h$ and $C_l$ denote the stiffnesses of elements along different crystallographic directions of the stable phase, with $C_h > C_l$. The force $F_1$ for joining the specimen of $C_l$ to that of $C_m$ can differ from the force $F_2$ for joining the specimen of $C_h$ to that of $C_m$.

![Figure 2.](image)

From Figure 2(c), we can obtain the following relations.

$$C_l = F_1 / \delta_2$$  \hspace{1cm} (5)

$$C_h = F_2 / \delta_1$$  \hspace{1cm} (6)

$$C_m = F_1 / \delta_3 = F_2 / \delta_4$$  \hspace{1cm} (7)

$$\delta = \delta_1 + \delta_4 = \delta_2 + \delta_3$$  \hspace{1cm} (8)

It follows from the above relations that

$$\delta = \delta_1 + \delta_4 = \delta_2 + \delta_3$$  \hspace{1cm} (9)

$$W_2 = F_2 \delta / 2$$  \hspace{1cm} (10)

Similarly, that of the metastable phase adjacent to the stable phase with $C_h$ is given by

$$W_1 = F_1 \delta / 2$$  \hspace{1cm} (11)
Since \( C_h > C_p \), Eq. 9 gives \( \delta_4 > \delta_3 \) and hence we obtain \( F_2 > F_1 \) from Eq. 7.

The strain energy of the metastable phase adjacent to the stable phase with \( C_h \) is given by

\[
W_2 = \frac{F_2 \delta_4}{2}
\]

Similarly, that of the metastable phase adjacent to the stable phase with \( C_i \) is given by

\[
W_1 = \frac{F_1 \delta_3}{2}
\]

Since \( \delta_4 > \delta_3 \) and \( F_2 > F_1 \), we obtain \( W_2 > W_1 \). In other words, the metastable phase is subjected to the higher strain energy in the higher stiffness direction of the stable phase.

The stiffness \( C \) is related to Young’s modulus \( E \) as \( C = EA/L \) with \( A \) and \( L \) being the cross-sectional area and the length of the stable-phase element, respectively. Therefore, it can be stated that the highest strain-energy density region in the metastable phase containing a stable phase crystallite is the stable/metastable interface region in the highest Young’s modulus directions of the stable phase. As the heating temperature increases, the strain energy contribution to the activation energy for continuing crystallization will decrease [21].

For a thin amorphous deposit, another form of strain energy can develop due to a difference in thermal expansion coefficient between the deposit and the substrate in addition to the accommodation strain energy. The strain energy is termed the thermal strain energy. The thermal stress developed in the thin deposit, which is associated with the thermal strain energy, is equivalent to an external stress along the surface. If the stress is planar isotropic, the directed crystallization is unlikely to occur along the deposit surface in the absence of the accommodation strain energy. However, the stress can influence the crystal growth rate.

3. Solid-phase epitaxial growth rate of crystalline Si in self-implanted Si(100) wafer

3.1. Uniaxial stress ranged from \(-0.55\) to \(0.55\) GPa

The \( a\)-Si/c-Si interface region is under the tensile stress because the density of c-Si is higher than that of \( a\)-Si (Section 4). According to Section 2, if the tensile stress in specimen is increased by external tensile forces, the strain energy in the interface region will increase, which in turn will increase the crystallization rate, and vice versa.

Aziz et al. [23] studied the solid-phase epitaxial growth rate of c-Si from \( a\)-Si by bending bar-shaped Si(001) wafers with a three-point bending system at about 540 °C. The Si wafers (\( p\) type, 1 ohm cm, 0.84 mm thickness) were implanted on both sides at 77 K with \( ^{30}\)Si \((60 \text{ keV}, 1\times10^{15} \text{ cm}^{-2}; 180 \text{ keV}, 2\times10^{15} \text{ cm}^{-2})\) to create 280-nm-thick amorphous surface layers. The wafers were diced into bars >20 mm in length in the [110] direction by 5 mm in width.
One side of the elastically bent specimen is approximately under a uniaxial tensile stress state and the other side under a uniaxial compressive stress state, in which the stress ranged from $-0.55$ GPa (compressive) to $0.55$ GPa (tensile). Their measured crystallization rate as a function of applied stress showed that the rate in the tension side was higher than that in the compression side. Aziz et al. claimed that the stress existed in the crystal at the crystalline-amorphous interface because there is no stress in the bulk of the $a$-Si due to stress relief by viscous flow [24]. Even though the initial stress in the $a$-Si could be completely relieved during the stress measurement, the stress developed in the $a$-Si at the $c$-Si/$a$-Si interface during crystallization might not be removed immediately.

Even if we cannot distinguish the initial stress from the stress developed during crystallization, it is apparent that the $a$-Si film on the tension side of the sample could be more stressed in tension than that on the compression side. Therefore, we can expect that the grain growth rate in the film on the tension side will be higher than that in the film on the compression side in agreement with the measured data.

3.2. Effect of hydrostatic pressure up to 3.2 GPa

Lu et al. [25] measured the hydrostatic pressure dependence of the solid-phase epitaxial growth rate of self-implanted Si(100) by using the in situ time-resolved interferometric technique and high-pressure diamond anvil cell. With fluid argon as the pressure transmission medium, a hydrostatic pressure environment was achieved around the sample. The external heating geometry employed provided a uniform temperature across the sample. At temperatures of 530–550 °C and pressures up to 3.2 GPa, the growth rate was enhanced by up to a factor of 5 over that at 1 atmosphere pressure ($\approx 0.1$ MPa).

This result appears to contradict the non-hydrostatic stress effect explained in Section 3.1. The crystallization of $a$-Si results in a decrease in volume. Therefore, a hydrostatic compression is expected to accelerate crystallization. We roughly estimate a hydrostatic pressure for the crystallization of $a$-Si without taking the thermal activation into account.

Let $P$ and $\Delta$ denote the hydrostatic pressure and the volumetric dilatation for crystallization of $a$-Si, respectively. The pressure is related to the dilatation as follows:

$$ P = -B\Delta $$

where $B$ is the bulk modulus of $a$-Si and the volumetric dilatation $\Delta$ is defined as

$$ \Delta = \frac{V - V_0}{V_0} $$

Here $V_0$ is the volume before crystallization, and $V$ is the volume after crystallization. The density of $c$-Si at room temperature is 2320 to 2340 kg m$^{-3}$ [26]. If the density of $c$-Si is set to be
2330 kg m\(^{-3}\), the specific volume of \(c\)-Si is calculated to be \(4.29\times10^{-4}\) m\(^3\) kg\(^{-1}\). Ion-implanted amorphous silicon is 1.8\% less dense than \(c\)-Si at room temperature [27]. Therefore, the density of \(a\)-Si at room temperature is calculated to be 2288 m\(^3\) kg\(^{-1}\) and its specific volume is calculated to be \(4.37\times10^{-4}\) m\(^3\) kg\(^{-1}\). Since the volumes of \(a\)-Si and \(c\)-Si vary with temperature, we calculate those at 540 °C. The linear thermal expansion coefficients of \(a\)-Si and \(c\)-Si are almost the same, about \(3\times10^{-6}\) K\(^{-1}\) [24, 28]. Therefore, the specific volume of \(a\)-Si at 540 °C is \(4.39\times10^{-4}\) m\(^3\) kg\(^{-1}\) \([= 4.37\times10^{-4}\times[1+3\times3\times10^{-6}\times(540-25)]\] \), and that of \(c\)-Si at 540 °C is \(4.31\times10^{-4}\) m\(^3\) kg\(^{-1}\) \([= 4.29\times10^{-4}\times[1+3\times3\times10^{-6}\times(540-25)]\] \). The volumetric dilatation at 540 °C is

\[\Delta = \frac{(4.31 - 4.39)}{4.39} = -0.0182. \tag{14}\]

For lack of the bulk modulus of \(a\)-Si at 540 °C, it has been calculated using the biaxial modulus of ion-beam-sputtered \(a\)-Si at 110 °C, \(M_{\sigma}(110) = 140\) GPa [24], the temperature dependence of \(M\) for Si(100) [24], and Poisson’s ratio \(\nu\) of \(a\)-Si film deposited by rf sputtering onto Si substrate in an atmosphere of \(P_{\text{H}_2}/(P_{\text{H}_2}+P_{\text{Ar}}) = 0.001\) [29]. The bulk modulus \(B\) and the biaxial modulus \(M_{\sigma}\) can be expressed as

\[B = \frac{E}{3(1-2\nu)} \tag{15}\]

\[M_{\sigma} = \frac{E}{(1-\nu)} \tag{16}\]

where \(E\) is Young’s modulus. The temperature dependence of \(M_{\sigma}(T)\) for Si(100) is given by

\[\frac{d\ln M_{\sigma}(T)}{dT} = -62\times10^{-6}\text{K}^{-1}\]

From this we obtain \(M_{\sigma}(540) = 136\) GPa. According to Jiang et al. [29], \(\nu = 0.32\). Substitution of \(M_{\sigma}(540) = 136\) GPa and \(\nu = 0.32\) into Eq. 16 gives \(E(540) = 92.5\) GPa. In this calculation, Poisson’s ratio was assumed to be independent of temperature. From these elastic constants, the bulk modulus of \(a\)-Si at 540 °C, \(B(540) = 85.6\) GPa, is obtained. Therefore, the hydrostatic pressure for crystallization at 540 °C is calculated as \(P(540) = 1.56\) GPa. From this estimation we can see that hydrostatic pressures of the order of GPa will accelerate the crystal growth rate.

Stresses of the order of 0.1 GPa in Section 3.1 are too low to be effective in the grain growth of \(c\)-Si. On the other hand, its contribution to the local tensile stress developed in the \(a\)-Si/\(c\)-Si interface could be much higher. Therefore, the compressive stresses of the order of 0.1 GPa reduced the growth rate, and the tensile stresses increased the growth rate.
4. Crystallization of amorphous Si on glasses

According to the directed-growth theory described in Section 2, the highest crystallization rate would be along the maximum Young’s modulus direction (MxYMD). In order to understand crystallization anisotropy of a-Si, we need to calculate Young’s modulus of crystalline Si (c-Si). Young’s modulus $E$ for crystals of cubic system is given by Eq. 17 [30,31],

$$\frac{1}{E} = S_{11} + 2(S_{44} - 2S_{12}) \left( a_{11}^2 a_{12}^2 + a_{12}^2 a_{13}^2 + a_{13}^2 a_{11}^2 \right)$$

where $S_{11}$, $S_{44}$, and $S_{12}$ are the compliances referred to the symmetric axes and $a_{ii}$ are the direction cosines of the uniaxial stress direction $i$ referred to the symmetric axes $i$. For the [hkl] direction,

$$a_{11} = h/l, \quad a_{12} = k/l, \quad a_{13} = l/l,$$

For silicon at 293 K, $S_{11} = 0.007685$, $S_{12} = -0.002139$, and $S_{44} = 0.01256 \text{ GPa}^{-1}$ [32], and $[S_{44} - 2(S_{11} - S_{12})] = -0.00708 < 0$. Therefore, the maximum and minimum values of $(a_{11}^2 a_{12}^2 + a_{12}^2 a_{13}^2 + a_{13}^2 a_{11}^2)$ in Eq. 17 are 1/3 for the <111> directions and 0 for the <100> directions, respectively. Therefore, the growth rate of c-Si is likely to be the highest in the <111> directions.

For a-Si film/SiO$_2$ glass-substrate structure, the thermal strain-energy is the highest near the interface between the film and the substrate, or in the deepest place of the a-Si film, which is under the highest compressive stress because the thermal expansion coefficient of Si is higher than that of the SiO$_2$ layer. At low temperatures, crystallization of a-Si is likely to be dominated by the accommodation strain-energy along with the thermal strain energy. In this case, crystallization is likely to start near the film/substrate interface and the highest growth directions (the <111> directions) tend to be parallel to the surface because the film stress is the highest along the film/substrate interface or the surface.

Because the thickness of the Si film including a-Si and c-Si is much smaller than the dimensions along the film surface, the stress in the thickness direction is negligible, and the film is approximately under the plane stress state. That is, the film stress is the highest along the interface or the film surface. Therefore, when the <111> directions are placed along the film surface, the growth rate of crystallites will be the highest.

Let two of four <111> directions, for example, the [111] and [–1 1 1] directions be placed along the surface, then the thickness direction becomes the [0–1 1] direction (110 projection in Figure 3). Thus, the texture of crystallites is approximated by the <110>//ND (ND: the surface normal direction) orientation with the <111> branches. When three of the <111> directions are at 19.4° to the film/substrate interface and one of the <111> directions is parallel to the thickness direction [(111) projection in Figure 3], the <111>//ND texture can be obtained. This possibility is based on the relatively small angle of 19.4°. The directed crystallization can give rise to the dendritic
Because the thickness of the Si film including \( a\)-\( Si \) and \( c\)-\( Si \) is much smaller than the dimensions along the film surface, the stress in the thickness direction is negligible, and the film is approximately under the plane stress state. That is, the film stress is the highest along the interface or the film surface. Therefore, when the \( <111> \) directions are placed along the film surface, the growth rate of crystallites will be the highest.

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When the annealing temperature is high enough to activate the volume diffusion, the random orientation will change to the \( <111> \) texture because the \( [111] \) planes have the minimum surface energy density, to reduce the surface energy which is the major energy source in thin films. The \( <110> \) or \( <111> \) to random transition temperature or the random to \( <111> \) transition temperature is likely to decrease with increasing purity of Si films.

Silicon has a stacking-fault energy of about 50 mJ/m\(^2\). This relatively small energy generates many twins during crystallization. The twinning planes and directions of \( c\)-\( Si \) are \( [111] \) and \( [1 1 0] \) directions [20].

![Figure 3. Cubic (110) and (111) stereographic projections [21].](http://dx.doi.org/10.5772/59723)

![Figure 4. Twinning plane traces in [1 1 0] //ND oriented dendritic crystal whose branches are directed along [1 1 1] and [1 1 1] directions [20].](http://dx.doi.org/10.5772/59723)
<112>. Figure 4 shows the [1 1–2] twinning direction and twinning-plane traces in the [1–1 0]//ND oriented dendritic crystal whose branches are directed along the [111] and [1 1–1] directions. The angle between the [1 1–2] and [1 1–1] directions can appear smaller than 19.5°, when the specimen is slightly rotated about the [1 1–2] axis. This may make crystallites appear to grow along the <112> directions.

### 4.1. Evaporation-deposited a-Si films

Table 1 summarizes deposition conditions of a few a-Si films and their annealing textures. When heated at 650 °C for 1 h in flowing nitrogen in an open tube furnace, Si dendrites were observed. The selected area diffraction pattern of a dendrite indicated that dendrite arms were parallel to the <111> directions (Figure 5). The [1 1–1] was erroneously indexed as the [0 1–1] in [15]. When the heat-treatment temperature was raised to 850 °C, the film fully crystallized with equiaxed grains of 640 nm in normal mean size and dendrite remnants. The texture of the film was random. After heating at 1040 °C, the film had a microstructure consisting solely of equiaxed grains without dendrite remnants. The normal mean grain size for this film was 205 nm, and the texture of the film was random. The result is compatible with the prediction of the directed crystallization theory because the strain energy contribution to the activation energy decreases with increasing annealing temperature and in turn the anisotropic crystallization rate decreases [20].

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<td>900 nm; evapor.</td>
<td>SiO₂ on &lt;100&gt; p-type Si</td>
<td>370</td>
<td>10₁Ο⁶</td>
<td>300</td>
<td>Flowing N₂</td>
<td>600</td>
<td>Random</td>
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<td>500 nm; evapor. fused silica base</td>
<td></td>
<td>380</td>
<td>6</td>
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<td>Random</td>
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<tr>
<td>~100 nm; LPCVD</td>
<td>Glass</td>
<td>550</td>
<td>CF</td>
<td>3</td>
<td>610</td>
<td>&lt;110&gt;</td>
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<td>70 nm; Dose</td>
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deposit.: deposition; evapor.: evaporation; substr.: substrate; temp.: temperature; anneal.: annealing; CF: conventional furnace; RTP: rapid thermal process; Dose: implanted by a dose of 5×10¹⁵ cm⁻² Si⁺ at 30 keV; UHV: ultrahigh vacuum.

Table 1. Deposition conditions of a-Si films and their annealing textures
Whenever contamination is avoided prior to annealing under ultrahigh vacuum, crystallization occurred at 600 °C regardless of the substrate temperature in evaporation and the crystallized films had no texture [16]. They attributed the random orientation to the existence of voids in the amorphous films. However, the amorphous phase itself can give rise to the randomness at the absence of strain energies. The voids can reduce the strain energy of films, which in turn may enhance the random orientation. After annealing at 700 °C, the <111>/ND texture was obtained. In Anderson’s work [15], the random orientation was obtained at 850 °C or 1040 °C and the <111>/ND texture was not observed within the experimental range. The differences are caused by differences in purity of the samples. Films obtained at lower pressures are likely to have higher purity. It is well known that the higher purity gives rise to the lower crystallization temperature.

4.2. Amorphous Si$_1$–xGe$_x$ films on SiO$_2$

Hwang et al. [19] deposited a-Si$_{1-x}$Ge$_x$ films with $x = 0$–0.53 on thermally oxidized Si<100> wafers by molecular beam epitaxy. The nominal thickness of the film was 100 nm and the deposition temperature was 300 °C. The base pressure and the deposition pressure were $10^{-10}$ Torr and $10^{-9}$ Torr, respectively, and the deposition rate was about 3 nm/min. When annealed at 600 °C, a-Si film ($x = 0$) crystallized into dendritic forms similar to Figure 5 with a strong <111>/ND texture. When annealed at 600 °C, a-Si$_{1-x}$Ge$_x$ ($x = 0$) crystallized into dendritic forms similar to Figure 5 with a strong <111>/ND texture. When annealed at 600 °C, a-Si$_{1-x}$Ge$_x$ ($x = 0$) crystallized into dendritic forms similar to Figure 5 with a strong <111>/ND texture. When annealed at 600 °C, a-Si$_{1-x}$Ge$_x$ ($x = 0$) crystallized into dendritic forms similar to Figure 5 with a strong <111>/ND texture. When annealed at 600 °C, a-Si$_{1-x}$Ge$_x$ ($x = 0$) crystallized into dendritic forms similar to Figure 5 with a strong <111>/ND texture. When annealed at 600 °C, a-Si$_{1-x}$Ge$_x$ ($x = 0$) crystallized into dendritic forms similar to Figure 5 with a strong <111>/ND texture. When annealed at 600 °C, a-Si$_{1-x}$Ge$_x$ ($x = 0$) crystallized into dendritic forms similar to Figure 5 with a strong <111>/ND texture. When annealed at 600 °C, a-Si$_{1-x}$Ge$_x$ ($x = 0$) crystallized into dendritic forms similar to Figure 5 with a strong <111>/ND texture. When annealed at 600 °C, a-Si$_{1-x}$Ge$_x$ ($x = 0$) crystallized into dendritic forms similar to Figure 5 with a strong <111>/ND texture. When annealed at 600 °C, a-Si$_{1-x}$Ge$_x$ ($x = 0$) crystallized into dendritic forms similar to Figure 5 with a strong <111>/ND texture. When annealed at 600 °C, a-Si$_{1-x}$Ge$_x$ ($x = 0$) crystallized into dendritic forms similar to Figure 5 with a strong <111>/ND texture. When annealed at 600 °C, a-Si$_{1-x}$Ge$_x$ ($x = 0$) crystallized into dendritic forms similar to Figure 5 with a strong <111>/ND texture. When annealed at 600 °C, a-Si$_{1-x}$Ge$_x$ ($x = 0$) crystallized into dendritic forms similar to Figure 5 with a strong <111>/ND texture. When annealed at 600 °C, a-Si$_{1-x}$Ge$_x$ ($x = 0$) crystallized into dendritic forms similar to Figure 5 with a strong <111>/ND texture. When annealed at 600 °C, a-Si$_{1-x}$Ge$_x$ ($x = 0$) crystallized into dendritic forms similar to Figure 5 with a strong <111>/ND texture. When annealed at 600 °C, a-Si$_{1-x}$Ge$_x$ ($x = 0$) crystallized into dendritic forms similar to Figure 5 with a strong <111>/ND texture. When annealed at 600 °C, a-Si$_{1-x}$Ge$_x$ ($x = 0$) crystallized into dendritic forms similar to Figure 5 with a strong <111>/ND texture. When annealed at 600 °C, a-Si$_{1-x}$Ge$_x$ ($x = 0$) crystallized into dendritic forms similar to Figure 5 with a strong <111>/ND texture. When annealed at 600 °C, a-Si$_{1-x}$Ge$_x$ ($x = 0$) crystallized into dendritic forms similar to Figure 5 with a strong <111>/ND texture. When annealed at 600 °C, a-Si$_{1-x}$Ge$_x$ ($x = 0$) crystallized into dendritic forms similar to Figure 5 with a strong <111>/ND texture. When annealed at 600 °C, a-Si$_{1-x}$Ge$_x$ ($x = 0$) crystallized into dendritic forms similar to Figure 5 with a strong <111>/ND texture.
When thickness factors are taken into account, its texture could be approximated by $<110> + <311>/\text{ND}$. Even though the accurate texture of the films cannot be obtained by this method, the texture of the films could be approximated by random orientation with weak $<110>/\text{ND}$ and $<311>/\text{ND}$ components. The near-spherical crystallites and the near-random texture seem be related to an increased contribution of the thermal energy. The solidus temperature of $\text{Si}_{0.47}\text{Ge}_{0.53}$ is 1095 °C, which is lower than the melting point of Si, 1414 °C (Figure 7). Therefore, at an annealing temperature of 600 °C, crystallization of $\text{Si}_{0.47}\text{Ge}_{0.53}$ was dominated by the thermal energy. The aspect ratio of crystallites decreased with increasing content of Ge [19]. This also reflects an increase in thermal energy contribution with increasing Ge content. The grain size in fully crystallized Si-Ge films decreased with increasing Ge content. The crystal structures, lattice parameters, intrinsic stacking-fault energy, and elastic anisotropies of Ge and Si are similar, and so the characteristics of the Ge-Si alloys are likely to be similar to those of Ge and Si. Therefore, for a given annealing temperature $T$, the decrease in the solidus temperature is equivalent to an increase in $T/T_m$, with $T_m$ being the absolute melting point of a reference material (eg. Ge or Si) in the Ge–Si system.

The grain size $G$ is likely to be reciprocally proportional to the nucleation rate $dN/dt$. Since the nucleation is a thermally activated process, the grain size and the nucleation rate can be expresses as

$$\frac{A}{G} = \frac{dN}{dt} = B\exp\left(-\frac{Q}{RT}\right)$$

(19)

where $A$ and $B$ are constants, and $Q$ is the activation energy for nucleation. Therefore, we obtain

$$G = C\exp\left(\frac{Q}{RT}\right) \text{ or } \ln G = C_0 + \frac{Q}{RT} \text{ or } \ln G = C_0 + \frac{Q}{RT} \frac{T_m}{T_m}$$

(20)
where \( C (= A/B) \) and \( C_0 (= \ln C) \) are constants. As discussed above, \( T/T_m \) can be assumed to be proportional to \( T/T_s \) with \( T_s \) being the solidus temperatures of the Ge–Si system. Then Eq. (20) can be expressed as
\[
\ln G = C_0 + \frac{Q}{RT} = C_0 + \frac{Q T_s}{RT}
\]  

(21)

Here \( Q_0 \) \( (Q/T_m) \) is a constant. The relationship between \( \ln G \) and \( T_s/T \) is plotted in Figure 8. The good linear relationship in the figure supports the above assumption.

5. Metal-induced crystallization

5.1. Copper-induced crystallization

Lee et al. \[8\] deposited an 80 nm \( a \)-Si on Corning 1737 glass by plasma-enhanced chemical vapor deposition (PECVD) at 280°C using Si\(_2\)H\(_6\) and H\(_2\) as source gases. The wafer was cut into \( 3 \times 3 \) cm\(^2\) square specimens for the subsequent process. To deposit copper on the \( a \)-Si film, the photoresist (PR) was spin-coated and patterned by a photolithographic process using rectangular mask patterns of \( 60 \times 30 \) μm\(^2\). A copper layer of 2 nm in thickness was deposited in a DC sputtering system. Copper on the PR patterns was removed by the lift-off method and only that deposited on the \( a \)-Si was left. The crystallization annealing was done at 500°C for 1 h in N\(_2\) ambience. During the crystallization annealing an electric field of 1.80 kV/m was applied to the above metal-deposited specimen by the DC power supply.

From the crystallized specimen, 3 mm disks were cut using an ultrasonic cutter for TEM specimen preparation. For the plan-view studies of the \( a \)-Si film, the disks were mechanically back-thinned to a thickness of about 10 μm, and then ion milled on the glass substrate side at an accelerating voltage of 5 kV using a PIPS. The crystallization microstructure was characterized by TEM. High-resolution TEM (HRTEM) was performed at 400 kV in a JEM4010 (point-to-point resolution: 0.15 nm, JEOL Co., Ltd.). Energy dispersive X-ray spectroscopy (EDXS) was applied for composition analysis of \( a \)-Si and \( c \)-Si regions.

An enlarged view of the patterns between the electrodes is shown in Figure 9. The crystallization front migrates from the negative electrode side to the positive electrode side. A needlelike morphology of \( c \)-Si was clearly observed at the interface between the fully crystallized and amorphous regions indicated by ‘O’ in Figure 9 as shown in Figure 10 (a). As revealed in Figures 10 (b), almost all the \( c \)-Si needles exhibit the <011>/ND orientations with respect to the \( a \)-Si film surface normal and grew the <111> and <211> directions, forming an angle of 90° between the needles. The [011] diffraction pattern taken from the needle ‘A’ in Figure 10 (b) showed streaks along the [111] direction, indicating that there are many stacking faults or twins normal to that direction. The \( a \)-Si region was measured to contain \( (2.99 \pm 0.97) \) at.% Cu on average by EDXS measurement of five areas. In fully crystallized regions many needles were interwoven, as shown in Figure 11. The regions contained \( (1.63 \pm 0.15) \) at.% Cu on average by XEDS measurements of four areas. The solubility of Cu in \( c \)-Si is negligible, and therefore, the detected Cu is believed to arise from trapped Cu solutes in the interfaces between the interwoven \( c \)-Si needles. Figure 12 (a) shows an HRTEM image also revealing the growth directions of <111> and <211> with the <011>/ND orientation, which means the [011] planes...
being parallel to the surface plane. At a higher magnification (Figure 12 (b)), three \{111\} twins and a stacking fault can be seen. In order to consider the role of any Cu silicides on the nucleation and growth of the \(c\)-Si needles, the edges of the \(c\)-Si needles were examined. Figure 13 displays the typical edge, where Cu silicides are not observed, and instead, Si lattice image is seen. Furthermore, Cu silicides are observed even in the \(a\)-Si and the crystallized region within the limited field of view. The \(c\)-Si region at the edge contains many \{111\} twins and stacking faults indicated by white triangles and arrows, respectively. There seems to be also some lattice distortion in some areas, due to defects (twins or stacking faults) which are not clearly visible. As in the NiSi\(_2\)-mediated crystallization (Section 5.2) Cu-induced crystallization proceeds in the \(<111>\) directions with a shape of needles as shown in Figure 10(b) and Figure 12 (a). The \(c\)-Si needles have the \(<011>\)/ND orientations.

Figure 9. Optical image of patterns between electrodes [8].

Additionally, as shown in Figure 10 (b) and 12 (a), the growth occurs also in the \(<211>\) directions. At variance with the NiSi\(_2\)-mediated crystallization, however, as shown in Figure 13, Cu silicides are not observed at the leading edges of the \(c\)-Si needles, indicating that the crystallization of the Cu/\(a\)-Si system in this study is not mediated by any Cu silicides. Radnoczi et al. [4] suggested that Au, Sb, In and Al, which form eutectic with Si, dissolved in the \(a\)-Si film may loosen the covalent bonds in Si and make the \(a\)-Si even unstable, enhancing crystallization. Even though Cu is a silicide-forming metal, Cu atoms appear to enhance crystallization in a similar way to the eutectic-forming metals. Since Cu has a negligible solubility in crystalline Si [33], the Cu solute atoms are repelled by the \(c\)-Si. The Cu atoms will diffuse into the \(a\)-Si matrix, making the \(a\)-Si unstable, and the Si atoms will migrate into the \(c\)-Si side from the \(a\)-Si, resulting in crystallization. Diffusion of Cu atoms in \(a\)-Si seems to be rate-controlling. Without the application of any electric field during annealing at 500 °C (i.e., in the MILC process), the crystallization rate is reported to be 1.5–2 \(\mu\)m h\(^{-1}\) [12]. Copper is reported to diffuse in \(a\)-Si with \(D > 10^{-12} \text{ cm}^2 \text{ s}^{-1}\) in a temperature range between 400 and 600 °C [34]. From the
the increase in crystallization rate with an electric field of 210 V m
study [8], because no Cu silicides are observed at the leading edges of the
some crystallization parameters such as pattern size, shape, and the applied electric field
obtained without any electric field in the MILC process (1.5–2 μm h
the resistivity of
effect is likely to hold for the diffusion of Cu in
intensity are different, a high crystallization rate of ~40 μm h
[13,14] and is limited to the diffusion of Ni in NiSi
are different, a high crystallization rate of ~40 μm h
The crystallized pattern images in Figure 9 reveal that the macroscopic crystallization direction under an
areas, due to defects (twins or stacking faults) which are not clearly visible. As in the NiSi
bonds in Si and make the
atoms in
a-Si unstable, and the Si atoms will migrate into the
Cu atoms will diffuse into the
a-Si, resulting in crystallization. Diffusion of Cu
Si matrix, making the
a-Si unstable, and the
a-Si needles grow in directions of <111> and <112> directions with <110>//ND orientations
in a temperature range between 400 and 600°C [34]. From the diffusivity value of 10
Cu-induced crystallization proceeds in the <111>-directions with a shape of needles as shown in Figure 10(b) and
growth occurs also in the <211> directions. At variance with the
the minimum diffusion length (\(D_t\)) is calculated to be 0.6 μm for 1 h at 500°C. This diffusion length is in qualitative agreement with the crystallization rate
Additionally, as shown in Figure 10(b) and 12(a), the growth occurs also in the <211> directions. At variance with the
the momentum exchange induces the Ni atoms in NiSi
et al. [35] propose that the electron wind effect (electromigration) via current flow in the pattern at the elevated temperature [35]. Choi
et al. [4] suggested that Au, Sb, In and Al, which form eutectic with Si, dissolved in the a-Si film may loosen the covalent
a-Si even unstable, enhancing crystallization. Even though Cu is a silicide-forming metal, Cu
needles, indicating that the crystallization of the Cu/
the crystallization rate obtained without any electric field in the MILC process (1.5–2 μm h
-12 Si unstable, and the Si atoms will migrate into the
Cu solute atoms are repelled by the
a-Si. The Cu solute atoms are repelled by the
a-Si, making the
a-Si needles have the <011>//ND orientations. Without the application of any electric field during annealing at 500°C, Cu-
in the NiSi
the crystallization rate obtained without any electric field in the MILC process (1.5–2 μm h
Lee et al. [12] showed
-1). Lee et al. [12] showed the
pattern in Figure 9 reveals that the macroscopic crystallization direction under an applied electric field is not the same as the one obtained without any electric field. Since Cu has a negligible solubility
the crystallization parameters such as pattern size, shape, and the applied electric field
interest is the difference in the crystallization or NiSi
the NiSi
NiSi
-12 -Si unstable, and the Si atoms will migrate into the
a-Si side from the NiSi
NiSi
-12 -Si system in this study is not mediated by any Cu silicides. Radnoczi
Cu-induced crystallization proceeds in the <111>-directions with a shape of needles as shown in Figure 10(b) and Figure
obtained, without any electric field in the MILC process (1.5–2 μm h
-1). The crystallized pattern images in Figure 9 reveal that the macroscopic crystallization direction under an applied electric field is not the same as the one obtained without any electric field.
in intrinsic carrier concentration, and at such high temperature, the electron flow in a-Si can cause the electron wind effect. The effect will accelerate the diffusion of Ni along the electron flow direction, and concomitantly, the crystallization rate.

Figure 11. (a) High-resolution TEM image showing growth directions of <111> and <112> with <110>//ND orientation of c-Si needle. Beam direction (zone axis) is parallel to [011]. At higher magnification (b) of area indicated by white-lined box in (a), three {111} twin boundaries and one stacking fault (SF) are visible [8].

Figure 12. High-resolution image of typical edge without Cu silicides, where Si lattice image is shown. {111} twins and stacking faults are indicated by white triangles and arrows, respectively [8].
Crystallization behavior of a-Si in the Cu/a-Si bilayer (without any electric field in this case) was studied by Russell et al. [36]. They found that on heating to 175°C, Cu$_3$Si phase appeared and subsequent heating to 485°C resulted in the crystallization of the a-Si in the form of dendrites in the Cu$_3$Si matrix. At variance with the results of Russell et al., the matrix was observed to be still a-Si and discernible Cu silicides including Cu$_3$Si phase were not observed in the study by Lee et al. [8]. In the study by Russell et al., the thickness ratio of Cu to a-Si was determined to obtain an average composition of Cu$_{3-\delta}$Si, where $\delta$ is from 0.5 to 1. In this case the matrix (continuous phase) could become Cu$_3$Si phase. In the study by Lee et al. [8], however, the deposited Cu film (2 nm thick) is very thin with the thickness ratio to the a-Si underlying layer (80 nm) of 1:40. Therefore, as already mentioned, they could not be easily observed. They may act as heterogeneous nucleation sites for crystallization. However, the difficulty in observing the phases indicates that their nucleation density was too low and their size was too small to explain the observed, overall crystallization behavior, strongly implying that the presence of Cu solutes, not Cu silicides, enhances crystallization.

The <111> growth directions and the <011>//ND orientations observed by Lee et al. [8] are caused by anisotropic elastic properties of c-Si, although a-Si is isotropic because the strain energy can influence the crystallization rate as discussed in Sections 2 and 4. The higher strain energy will give rise to the higher crystallization rate. One of the major strain energy sources may be the thermal strain energy due to differences in thermal expansion coefficient between a-Si and the substrate glass. The thermal strain energy can influence the crystallization rate, but is not related to the directional crystallization. Since the thermal expansion coefficients of a-Si and c-Si are expected to be almost the same, the thermal strain energy between a-Si and c-Si can be negligible.

Another strain-energy may arise from the accommodation strain between a-Si and c-Si due to different structures and densities (The densities of a-Si and c-Si are measured to be 2.1 to 2.3 [37] and 2.32 to 2.34 [26], respectively). This strain energy can be anisotropic because of anisotropic elastic properties of c-Si, even though a-Si is isotropic. Since the thickness of the Si film including a-Si and c-Si is much smaller than the dimensions along the film surface, the stress in the plane normal direction (ND) is negligible, and the film is under the plane stress state. Initial Si crystallites will form in the surface layer, where the Cu concentration is highest, and they could be of a disk-shape. The surface orientation of c-Si disks is presumably random because they form from a-Si. However, their growth rates will vary with their orientations because different orientations give rise to different strain energies. According to the directed growth theory (Section 2), c-Si grows in its MxYMD <111>, resulting in the needlelike shape. If c-Si grows along the [1 1–1] direction, the growth front will be subjected to tensile stresses, which will increase with growth. When the stresses reach a point where the distance between atoms in c-Si/a-Si interface is too far to be shuffled, another <111> growth, e.g., the [–1 1–1] growth, will be activated. When the <111> direction are parallel to the film surface, the c-Si needles can grow extensively and occupy large areas within the a-Si films, resulting in <110>//ND orientation (Figure 4). This may be expressed as the [110]<111> orientation.

The additional growth in the <211> directions may occur with the help of many [111] twins and stacking faults observed in the c-Si (Figure 12 (b) and Figure 13) which are certainly due
to the low stacking fault energy of Si (~50 mJ m$^{-2}$), even though the <211> growth directions are not favored in terms of the strain energy consideration. These [111] twins and stacking fault planes can generate steps for growth at the interface between the c-Si and a-Si, enhancing the growth in directions parallel to the twin and stacking fault planes. Because the angle between the <111> and <211> growth directions is 19.4°, we can make some errors in measurements. Even though there is some change in growth direction into <211>, the <011>/ND orientations will remain unchanged, as revealed in Figures 10 (b) and 12 (a).

### 5.2. Nickel-silicide mediated crystallization

Hayzelden et al. [13,14] studied the formation of buried precipitates of NiSi$_2$ in Ni-ion implanted a-Si and the subsequent NiSi$_2$-mediated crystallization of a-Si using in situ transmission electron microscopy (TEM) and high resolution TEM. a-Si thin films of 95 nm in thickness was deposited by low-pressure chemical-vapor deposition on Si substrates capped with 100 nm of thermally grown SiO$_2$. The a-Si could not crystallize from the c-Si substrate directly. Ion implantation of Ni into the a-Si was performed at an energy of 55 keV with doses of 1 and 5×10$^{15}$ ions cm$^{-2}$ to give a peak Ni concentration of 4×10$^{20}$ and 2×10$^{21}$ ions cm$^{-3}$, respectively, at a depth of approximately half the a-Si film thickness.

They observed that the NiSi$_2$ precipitates with CaF$_2$ structure formed in a-Si at about 400 °C, which were octahedra bounded by eight [111] faces. On the other hand, Yeh et al. [38] made a stacked structure of a-Si/Ni/SiO$_2$/Si(100) as follows: the <100>/ND oriented p-type Si wafers were chemically cleaned, followed by a dry oxidation in an atmospheric pressure chemical vapor deposition furnace to form a 3-nm-thick tunnel oxide. Subsequently, a 3.5-nm-thick Ni layer was deposited onto the tunnel oxide by electron beam evaporation. The Ni layer was capped by a 12.5-nm-thick a-Si layer deposited by sputtering. The stacked structure was, afterwards, dry oxidized at 900 °C to form a layer with control oxide on the top and NiSi$_2$ nanocrystals precipitated and embedded between tunnel oxide and control oxide. After dry oxidation, the well-separated and spherical NiSi$_2$ nanocrystals embedded in the SiO$_2$ layer are observed. The whole a-Si layer was oxidized to serve as the control oxide. The distance between NiSi$_2$ nanocrystals and the oxide/Si interface is about 10 nm indicating that about 3-nm-thick Si substrate was oxidized to contribute to about 6.5-nm-thick SiO$_2$, in addition to the 3-nm-thick tunnel oxide. The mean size and areal density of the NiSi$_2$ nanocrystals were measured to be ~ 7.6 nm and 3.3×10$^{11}$ cm$^{-2}$, respectively. The nanocrystals were identified to be NiSi$_2$ phase. This indicates that the initial NiSi$_2$ crystals are spherical.

Figures 1 and 3 in [14] show that NiSi$_2$ precipitates embedded in Ni-implanted a-Si thin films appear partly rectangular and partly spherical and spherical precipitates look a little smaller than rectangular precipitates. Therefore, the initial shape of the precipitate may be spherical and the octahedral shape of NiSi$_2$ precipitates may not be intrinsic. MIC of a-Si in Section 5.1 showed that c-Si grew in its <111> directions without NiSi$_2$-mediation. This is associated with contribution of strain energy to activation energy for crystal growth at low crystallization temperatures (Section 2) or low transformation temperatures [39].

Eight [111] faces of a spherical NiSi$_2$ precipitate are likely to be the best spots for the nucleation of c-Si because the growth rate of c-Si is the highest in the <111> directions and the extremely
good lattice match between the [111] faces of NiSi$_2$ and c-Si [the lattice parameter of NiSi$_2$ (0.5406 nm) is nearly equal to that of c-Si (0.5430 nm)], resulting in the better stability of the [111] faces of NiSi$_2$ precipitate than other faces. The eight spots are shown in Figure 14. Therefore, the [111] faces are likely to grow and bound the precipitate, forming the octahedral shape during annealing. The gradual transition from spheroidal NiSi$_2$ to octahedral NiSi$_2$ is represented in Figure 15. In this way, a structure of a-Si/c-Si/NiSi$_2$/c-Si/a-Si may be formed in a-Si thin film. The c-Si precipitates on the left and right of NiSi$_2$ can differ in thickness. Let the left c-Si be thicker than the right c-Si. In order to distinguish the right c-Si from the left c-Si, the right c-Si is denoted by c-Si(I) and the left c-Si by c-Si(II), then the structure is expressed as a-Si/c-Si(II)/NiSi$_2$/c-Si(I)/a-Si.

![Figure 13. Octahedron bounded by [111] planes. $S_1$: center (c) of ΔABE, $S_2$: c of ΔBCE, $S_3$: c of ΔCDE, $S_4$: c of ΔADE, $S_5$: c of ΔABF, $S_6$: c of ΔBCF, $S_7$: c of ΔCDF, $S_8$: c of ΔADF. Triangles (Δ) are [111] planes and edges are <110> directions. Arrows indicate <111> directions. $S_1$ to $S_8$ are on surface of one sphere.](image13.png)

![Figure 14. Schematic diagram showing gradual shape change from spherical NiSi$_2$ to octahedral NiSi$_2$. Arrows indicate <111> directions of NiSi$_2$ precipitate projected on a plane parallel to (001) plane. Black deposits indicate c-Si nucleated on [111] planes of NiSi$_2$ precipitate. Far left circle is made of $S_1$, $S_2$, $S_4$ or $S_5$, $S_6$, $S_7$, $S_8$ in Figure 13.](image14.png)

At about 500 °C, the epitaxial c-Si was nucleated on one or more of the NiSi$_2$ [111] surfaces and the c-Si needles grew in the <111> directions in the amorphous matrix with the <011>/ND
and Si(II) are Si contents in NiSi2. The NiSi2 precipitates were observed to be always present at the leading edges of c-Si needles [13, 14].

The extremely good lattice match between c-Si and NiSi2, and a mismatch between c-Si and a-Si give rise to stresses in c-Si near the c-Si/a-Si interface, as shown in Figure 15. Therefore, the average stress of c-Si layer in the structure of NiSi2/c-Si/a-Si increases with decreasing thickness of the layer, and the molar free energy of c-Si is likely to increase with decreasing thickness. In the structure of a-Si/c-Si(II)/NiSi2/c-Si(II)/a-Si, the molar free energy of c-Si(I) is likely to be higher than that of c-Si(II) and lower than that of a-Si, as shown in Figure 16. It can be seen from Figure 16 that the hysteresis drawn from both c-Si(I) and c-Si(II) to the NiSi2 show that in equilibrium, NiSi2 in contact with c-Si(I) is expected to be Si rich in comparison to NiSi2 in contact with c-Si(II). The intersections of the tie lines with the energy axes yield the chemical potentials for Ni and Si at the NiSi2/a-Si interface. A migrating NiSi2 precipitate consuming a-Si at the leading interface and forming a trail of epitaxial c-Si [= c-Si(II)] is shown schematically in Figure 17. There is a higher average stress of c-Si in contact with c-Si(I) than that of c-Si(II). The extremely good lattice match between c-Si and NiSi2 is capable of accommodating Si deficits of ~35 at.% [40]. The intersections of the tie lines with the energy axes yield the chemical potentials for Ni and Si at the NiSi2/c-Si(I) and NiSi2/c-Si(II) interfaces. The chemical potential of the Ni atoms is lower at the NiSi2/a-Si interface, whereas the chemical potential of the Si atoms is lower at the c-Si/NiSi2 interface. A migrating NiSi2 precipitate consuming a-Si at the leading interface and forming a trail of epitaxial c-Si [= c-Si(II)] is shown schematically in Figure 17.
The driving force behind the NiSi₂ precipitate migration and Si crystallization, although not an equilibrium process, can be described by reference to the equilibrium free energy associated with the transformation of metastable NiSi₂ to stable Si. The driving force for transformation is the reduction in free energy associated with the transformation of metastable NiSi₂ to stable Si. Tie lines in an equilibrium molar free-energy diagram of the type shown in Figure 16. The intersections of the tie lines with the energy axes yield the driving force for the forward diffusion of Si atoms through the NiSi₂ needlelike precipitation and rejection of Si to the epitaxial Si trail. In Figure 17 leads to the needlelike Si morphology. Note that the NiSi/SSi₂ epitaxial interface is formed behind the migrating NiSi₂ precipitation.

The curvature of the NiSi phase may be quite significant. For example, laser quenching has shown that the CaF₂ crystal structure of NiSi₂ is capable of accommodating Si deficits of ~35 at.% [40]. The intersections of the tie lines with the energy axes yield the chemical potential of the Ni atoms, \( \mu_{\text{Ni}} \), and the chemical potential of the Si atoms, \( \mu_{\text{Si}} \), respectively. Si in contact with NiSi₂ is expected to be Si rich in comparison to NiSi₂ in contact with Si(II) interface, as shown in Figure 16.

There are two limiting cases that describe the diffusional process of NiSi₂ in contact with Si(II)/NiSi₂ interface. These can be the dissociative and nondissociative diffusion models. In the first case, the dissociative model, NiSi₂ dissociates free Si for epitaxial growth at the Si/NiSi₂ interface, with new NiSi₂ formed at the leading NiSi₂/Si interface. The diffusing species in the dissociative mechanism would be Ni atoms and Si atoms from the Si(II)/NiSi₂ interface. A migrating NiSi₂ precipitation consumes Si atoms through the NiSi₂ interface, whereas the chemical potential of the Si atoms, \( \mu_{\text{Si}} \), is lower at the NiSi₂/Si interface than at the NiSi₂/Si interface. In the sequential formation of NiSi₂ and NiSi, and NiSi, respectively. Si in contact with NiSi₂/Si(II) interface diffusing through NiSi₂ would apply to Ni atoms. In the nondissociative model, Si atoms would simply be the fast-diffusing species [41-43].

Figure 16 also shows that the chemical potential of the Ni atoms, \( \mu_{\text{Ni}} \), is higher at the NiSi₂ interface, whereas the chemical potential of the Si atoms, \( \mu_{\text{Si}} \), is lower at the NiSi₂/Si(II) interface than at the NiSi₂/Si interface. Therefore, the NiSi₂ layer dissociates to provide free Ni atoms for epitaxial growth at the NiSi₂/Si interface.
dissociative model, the NiSi$_2$ layer dissociates to provide free Si for epitaxial growth at the c-Si/NiSi$_2$ interface, with new NiSi$_2$ formed at the leading NiSi$_2$/a-Si interface. In this case all the Si atoms that were originally in the NiSi$_2$ layer would be incorporated in the epitaxially grown c-Si and replaced by Si atoms from the a-Si. The diffusing species in the dissociative mechanism would be Ni atoms and the measured effective diffusivity would apply to Ni atoms. In the nondissociative model, Si atoms would simply diffuse through the NiSi$_2$ layer from the a-Si and bond to the epitaxial c-Si. The effective diffusivity would then apply to Si moving through the NiSi$_2$. In the sequential formation of Ni$_x$Si, NiSi, and NiSi$_2$, formed from thin-film diffusion couples of around 100 nm of Ni on Si, Ni is known to be the fast-diffusing species [41-43].

Figure 16 also shows that the chemical potential of the Ni atoms, $\mu^{Ni}$, is higher at the NiSi$_2$/c-Si(II) interface, or the c-Si(II)/NiSi$_2$ interface, than at the NiSi$_2$/c-Si(I) interface, whereas the chemical potential of the Si atoms, $\mu^{Si}$, is lower at the NiSi$_2$/c-Si(II) interface than at the NiSi$_2$/c-Si(I) interface. Therefore, the NiSi$_2$ layer dissociates to provide free Si for epitaxial growth at the c-Si(II)/NiSi$_2$ interface, with excess Ni at the c-Si(II)/NiSi$_2$ interface diffusing through NiSi$_2$ into the NiSi$_2$/c-Si(I) interface, interacting with c-Si(I) to form Ni$_x$Si$_2$ resulting in depletion of Si in c-Si(I). The depleted Si is replaced by Si from a-Si because the molar free energy of c-Si(I) is lower than that of a-Si. In this way, the Ni atoms diffuse from the c-Si(II)/NiSi$_2$ interface through NiSi$_2$ and c-Si(I) into the c-Si(I)/a-Si interface, whereas the Si atoms effectively diffuse from the c-Si(I)/a-Si interface through the Si(I) and NiSi$_2$ layers into the c-Si(II)/NiSi$_2$ interface. This process eventually makes the NiSi$_2$ precipitate migrate rightward consuming a-Si at the leading interface [c-Si(I)/a-Si] to form a trail of epitaxial c-Si(II) as shown in Figure 17. As this process proceeds, the c-Si(II) layer gradually thickens and the c-Si(I) layer gradually thin to a few layers, which is stable enough to survive because of the extremely good lattice match between NiSi$_2$ and c-Si. Consequently, the consumption of a-Si at the leading edge and rejection of Si to the epitaxial c-Si(II) trail take place and leads to the needlelike c-Si forming behind the migrating NiSi$_2$ precipitate.

The reason why during crystallization, the shape of the NiSi$_2$ precipitates at the leading edges of the c-Si needles assume the thin plate shape, whereas the leading edges of the c-Si needles are not flat (Figure 9) can be attributed to the extent of elastic anisotropy between NiSi$_2$ and c-Si. Zener’s anisotropy factor, $A = 2(S_{11}-S_{12})/S_{44}$ is used to denote the extent of elastic anisotropy of cubic materials. When the ratio $A$ is unity, the elastic properties are isotropic, but they can deviate from isotropy in two ways, by $A$ being either greater than or less than unity. $A = 1.83$ for NiSi$_2$ ($S_{11} = 0.01219$, $S_{12} = -0.00505$, $S_{44} = 0.01887$ GPa$^{-1}$ [44]) and $A = 1.56$ for c-Si (Section 4). Thus, the extent of elastic anisotropy of NiSi$_2$ is higher than that of c-Si, implying that the [111] planes of NiSi$_2$ have higher potential of existence than the [111] planes of c-Si. The higher Young’s modulus reflects the higher bonding strength. Therefore, the region surrounding the interface edge is strained, which in turn gives rise to crystallization along the interface plane as well as along the needle axis. In this way, the c-Si needles fan out during its growth (Figure 18), and simultaneously, the NiSi$_2$ precipitates become thinner. As the interface area increases, the accommodation strain increases to a point such that coherency between the two crystals cannot be maintained, resulting in dissociation of the NiSi$_2$ crystal into a few smaller crystallites. These smaller precipitates continue to mediate the growth [14]. Because the growth is
mediated by the NiSi₂ whose {111} planes have higher potential of existence than that of c-Si, the [011]<111>-oriented growth for the NiSi₂-mediated crystallization remains without growth in other directions (e.g., <211> for the Cu-enhanced crystallization).

Diffusion of Ni through c-Si to reach the a-Si in Figure 18 is consistent with previous experiments on Ni-assisted Si epitaxy. Erokhin et al. [45] deposited a film of Ni on a c-Si/a-Si structure and observed Ni diffusion to the c-Si/a-Si interface to form NiSi₂ after annealing for 43 h at 350 °C. Decomposition of NiSi₂ at the NiSi₂/c-Si interface with Ni diffusion into the a-Si was suggested as a mechanism for Si crystallization. This is in good agreement with the model of dissociative diffusion of Ni from the NiSi₂/c-Si interface to leave an abrupt planar interface. Low-temperature crystallization has also been reported following Ni deposition on hydrogenated a-Si/H. It was reported that NiSi₂ formed first at 330 °C followed by NiSi at 420 °C. Crystallization of the a-Si/H occurred at approximately 480 °C and it was suggested [43] that crystallization resulted from heterogeneous nucleation of a-Si at the NiSi₂/a-Si interface for 43 h at 350 °C. Decomposition of NiSi₂ at the NiSi₂/a-Si interface with Ni diffusion into the a-Si was suggested as a mechanism for Si crystallization. This is in good agreement with the model of dissociative diffusion of Ni from the NiSi₂/a-Si interface to leave an abrupt planar interface. Low-temperature crystallization has also been reported following Ni deposition on hydrogenated a-Si (a-Si:H) [43]. The silicidation process of Ni/a-Si:H on a fused silica substrate was investigated by in situ electrical resistance measurements and x-ray diffraction and Rutherford backscattering spectroscopy [7]. It was reported that NiSi₂ formed first at 330 °C followed by NiSi at 420 °C. Crystallization of the a-Si:H occurred at approximately 480 °C and it was suggested [43] that crystallization resulted from heterogeneous nucleation of a-Si at the NiSi₂/a-Si interface.

Figure 18. Schematic representation of diffusion-controlled growth of silicide-mediated crystallization of Si [14].
through NiSi$_2$ into the c-Si(II)/NiSi$_2$ interface, and the depleted Si atoms in the c-Si(I) layer are replaced by a-Si. This process eventually makes the NiSi$_2$ precipitate migrate consuming a-Si at the leading interface [c-Si(I)/a-Si interface] and forming the needlelike trail of epitaxial c-Si(II). Consequently, the c-Si(II)/NiSi$_2$ epitaxial interface is formed behind the migrating NiSi$_2$ precipitate. Migrating NiSi$_2$ precipitates resulted in crystallization of Si at temperatures as low as 484 °C, which is ~200 °C lower than the intrinsic temperature required for crystallization of pure a-Si. The NiSi$_2$-mediated crystallization rate is controlled by diffusion through the migrating NiSi$_2$ precipitates.

6. Conclusions

1. The solid-phase crystallization of an amorphous material needs the activation energy. The energy is usually supplied in the form of thermal energy by increasing the temperature of the material. When the nucleation occurs, the strain energy develops in the amorphous matrix as well as in the crystalline nuclei, or crystallites. The strain energy is the highest in the stable/metastable interface region in the highest Young’s modulus directions of the stable phase. Therefore, the growth rate of the crystallites is the highest in the metastable phase along the maximum Young’s modulus directions of the crystallites because the activation barrier can be surmounted by the strain energy when the thermal energy is not high enough to surmount the barrier. The strain energy is likely to give rise to inhomogeneous growth rates of crystallites due to their elastic anisotropy, if any. This directed crystallization theory can explain the following results.

2. The solid-phase epitaxial growth rate of c-Si from a-Si by bending the bar-shaped Si(001) wafers (p type, 1 ohm cm, 0.84 mm thickness) whose both sides were implanted to create 280–nm-thick amorphous surface layers, were elastically bent using a three-point bending system at about 540 °C. One side of the elastically bent specimen is approximately under a uniaxial tensile stress state and the other side under a uniaxial compressive stress state, in which the stress ranged from ~0.55 GPa (compressive) to 0.55 GPa (tensile). The measured crystallization rate as a function of applied stress showed that the rate in the tension side was higher than that in the compression side. The result is understood because the a-Si film on the tension side of the sample could be more stressed than that on the compression side. On the other hand, at temperatures of 530–550 °C and hydrostatic pressures up to 3.2 GPa, the solid-phase epitaxial growth rate of self-implanted Si(100) was enhanced by up to a factor of 5 over that at 1 atmosphere pressure (~0.1 MPa). This result appears to contradict the non-hydrostatic stress effect of the bent specimen. The crystallization of a-Si results in a decrease in volume. Therefore, a hydrostatic compression is expected to accelerate crystallization. However, the stress of ~0.55 GPa is too low to yield effective densification.

3. Evaporated a-Si film crystallizes into dendrite forms with dendrite arms in the <111> directions at low annealing temperatures. As the annealing temperature increases the a-Si film crystallized with increasingly equiaxed grains and random textures. The results
are compatible with the directed crystallization theory because the strain energy contribution to the activation energy decreases with increasing annealing temperature and in turn the isotropic crystallization rate increases. The crystallization temperature decreases with increasing purity of $a$-Si films.

4. The solidus temperature of $Si_{0.47}Ge_{0.53}$ is 1095 °C, which is lower than the melting point of Si, 1414 °C. Therefore, at an annealing temperature of 600 °C, crystallization of $a$-$Si_{0.47}Ge_{0.53}$ was dominated by the thermal energy unlike Si. The aspect ratio of crystallites decreased with increasing content of Ge. This also reflects an increase in thermal energy contribution with increasing Ge content.

5. The crystallization behavior of a Cu-deposited $a$-Si/glass sample annealed at 500 °C for 1 h with an electric field of 180V/cm has shown that the Si crystallites grow in the $<111>$ and $<112>$ directions with the $<110>$//ND orientation, assuming a needlelike shape. No Cu silicides are observed, and it seems that the Cu atoms in the $a$-Si film make the $a$-Si unstable, resulting in crystallization at the relatively low temperature. The growth directions of $<111>$ and the $<110>$//ND orientations are compatible with the directed crystallization theory. The $<112>$ directions can be possible with the help of many $[111]$ twins and stacking faults in $c$-Si.

6. The NiSi$_2$-mediated crystallization of $a$-Si can occur through the following processes. The initial shape of the NiSi$_2$ precipitated in the $a$-Si thin film is likely to be spherical and transforms into the octahedral shape during annealing because of the extremely good lattice match between $c$-Si and NiSi$_2$ and preferential growth of $c$-Si along its $<111>$ directions. Crystalline silicon layers nucleated on the [111] faces of NiSi$_2$ precipitates can differ in thickness. This brings about a structure of $a$-$Si/c$-$Si(II)/NiSi$_2/c$-$Si(I)/a$-$Si$ with $c$-$Si(II)$ layer being thicker than $c$-$Si(I)$ layer. The $c$-$Si(I)$ layer is more stressed than the $c$-$Si(II)$ layer, and so the molar free energy of $c$-$Si(I)$ is higher than that of $c$-$Si(II)$, but lower than that of metastable $a$-Si. Therefore, in this system, the Ni atoms diffuse from the $c$-$Si(II)/NiSi$_2$ interface through NiSi$_2$ into the $c$-$Si(I)/a$-$Si$ interface, whereas the Si atoms diffuse from the $c$-$Si(II)/a$-$Si$ interface through NiSi$_2$ into the $c$-$Si(I)/NiSi$_2$ interface, and the depleted Si atoms in the $c$-$Si(I)$ layer are replaced by $a$-Si. This process eventually makes the NiSi$_2$ precipitate migrate consuming $a$-Si at the leading interface [$c$-$Si(I)/a$-$Si$ interface] and forming the needlelike trail of epitaxial $c$-$Si(II)$.

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