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1. Introduction

Understanding the structure of proteins is a key to understanding their functions. Infrared (IR) spectroscopy is a very sensitive tool for studying three-dimensional molecular structures of proteins [1,2] in conditions relevant to biology, for example, in solution phase. This is because the vibrational frequency is determined by the chemical structure of the chromophore. However, both intra- and intermolecular force fields are involved. For the intramolecular aspect, the frequency of a specific vibration is influenced by the collective interaction of this mode with the rest 3N-7 (or 3N-6 for linear molecule) modes, where N is the total number of atoms in the molecular system. As for the intermolecular aspect, the frequency of a specific vibration is also influenced by its neighboring solvent molecules. Further, the IR spectroscopy is essentially a label-free method. There are a variety of intrinsic vibrational modes that can be used to characterize protein structures, thus the use of external chromophore, as is obligatory in some other spectroscopic methods, is not absolutely necessary for the IR method.

Commercial Fourier-transform infrared (FTIR) spectrometer allows the measurement of the IR absorption spectra for a large number of vibrational transitions in proteins in the mid-IR frequency range (4000 – 650 cm\(^{-1}\)). Certain key vibrational modes are well studied, and empirical relationship between their frequency and protein structure has been established. A well-known example of such is the amide-I mode, which is mainly the C=O stretching vibration. It is usually used as a protein/peptide backbone conformational reporter, because the amide unit is the linkage between amino acid residues and appears periodically on the peptide chain. The well-known linear IR signature of the α-helix, although appears to be a single absorption peak at 1640-1658 cm\(^{-1}\), has a two-component (a low-frequency A-mode and a high-frequency E-mode) band structure [3]. For the anti-parallel β-sheet, there is a major sharp absorption band appearing at 1620-1640 cm\(^{-1}\) and a weak peak at 1680-1696 cm\(^{-1}\) [4-8].
while the parallel $\beta$-sheet only exhibits a major sharp absorption band at 1620-1640 cm$^{-1}$ [6,8,9]. Whereas the IR signature of other conformations, such as the $\beta$-turn and random coil, usually appears to be a single band at 1640-1658 cm$^{-1}$ for random coil, or at higher frequency for the $\beta$-turn.

Assuming a harmonic potential, quantum chemical calculations can yield a complete set of vibrational frequencies of mid-sized polypeptide molecules. Good performance of the Kohn-Sham formulation of density functional theory (DFT) for predicting molecular geometries and harmonic vibrational frequencies has been established. For example, the fundamental vibrational frequencies for nine amide modes (amide-I to -VII, and amide-A and -B) in simple peptides using the hybrid density functional B3LYP are found to be in reasonable agreement with measurements in the gas phase. In certain cases the results are even better than those from strictly $ab$ initio approaches, such as second-order Moller-Plesset perturbation theory (MP2) [10]. However, because of the crudeness of the harmonic approximation, a frequency scaling factor is often needed in order to better match the theoretical prediction with experimental measurement. The frequency scaling factor is dependent on the level of theory used. A typical scaling factor is 0.9914 at the level of B3LYP/6-31G(d) [11]. However, a single scaling factor cannot scale multiple vibrational frequencies satisfactorily for a given molecule.

In reality, molecular vibrations are intrinsically anharmonic. Because of this, experimentally measured IR spectra are often complicated: it contains not only absorption peaks coming from fundamental transitions, but also those from overtone and combination transitions. For a given vibrational chromophore, the frequency difference between its fundamental transition and its overtone transition is known as the (diagonal) anharmonicity. For a pair of vibrational chromophores, the frequency difference between the sum of their fundamental transitions and that of the combinational transition is known as the off-diagonal anharmonicity. The measurement and assignment of overtone and combination bands in conventional linear IR spectroscopy have been known to be troublesome. This is because for the low-frequency modes, their overtone and combination bands fall into the high-frequency region that could be already very crowded; and for the high-frequency modes, their overtone and combination bands will fall into the high-frequency region of the mid-IR or even into the near-IR regime. Using the two-dimensional infrared (2D IR) spectroscopy developed in recent years, measurement of anharmonic frequencies in the mid-IR region has been made easier. In this method, a typical two-frequency 2D IR spectrum containing a set of anharmonic vibrators can be obtained, and from which the anharmonic frequencies, diagonal- and off-diagonal anharmonicities can be measured.

With the aid of modern laser technology, 2D IR spectroscopic studies in the 3-μm wavelength region (frequency = 3300 cm$^{-1}$) [12], 4-μm (2500 cm$^{-1}$) [13], 5-μm (2000 cm$^{-1}$) [14-17], 6-μm (1666 cm$^{-1}$) [18-20] and 8-μm (1250 cm$^{-1}$) [21] have been reported. This method is expected to be more powerful with the use of broadband laser sources in the future. Further, the 2D IR spectroscopic method also allows additional anharmonic vibrational parameters to be acquired, for example, diagonal and off-diagonal anharmonicities, and anharmonic couplings. Recent studies have shown that these parameters are also sensitive to molecular structures. In addition, the distributions of these vibrational parameters can also be experimentally determined by 2D IR.
It is of great importance to computationally predict the anharmonic vibrational properties of biomolecules, so that they can be used to interpret experimental IR results. The second-order perturbative vibrational treatment (PT2) [22,23] allows such computations. In this method, a full cubic and a semidiagonal quartic force field is obtained by central numerical differentiation of analytical second derivatives [24]. Un-scaled anharmonic vibrational frequencies of medium size molecules can be obtained quite efficiently. A previous study [25] has shown that the performance of B3LYP functional with reasonable basis sets in computing anharmonic vibrational frequencies of semirigid molecules is quite satisfactory. In addition, high-performance computer clusters can be utilized to compute the cubic and quartic derivatives for a given molecular system so that the anharmonic vibrational frequencies can be obtained efficiently using the DFT/PT2 combination. Very recently, the chain-length dependent anharmonicity and mode-delocalization of the amide-I mode [26], and that of the amide-A mode [27], in typical peptide conformations, have been reported.

In this chapter, we present a review of our recent works in studying the anharmonic vibrations of peptide oligomers. Methods to predict the anharmonic parameters are reviewed followed by results and discussions, mainly on the amide-I modes of peptides. The conformational dependence of the obtained anharmonic parameters is discussed. Results are useful in gaining more insights into the structural basis of the anharmonic vibrations of proteins and peptides.

2. Methods

2.1. Anharmonic vibrational frequency and anharmonicity

In the normal mode picture, the vibrational energy of fundamentals, overtones and combination bands for an \( N \)-atom molecular system can be generally written in the following form:

\[
E(n_i, n_j) = E_i + \hbar c \sum_{i \neq j} \omega_i n_i + \frac{1}{2} \sum_{i \neq j} \omega_i n_i + \frac{1}{2} \sum_{i \neq j} \omega_i n_i + \frac{1}{2} \sum_{i \neq j} x_{ij} \left( n_i + \frac{1}{2} \right) \left( n_j + \frac{1}{2} \right),
\]

(1)

where \( \omega_i \) is the harmonic frequency, \( n_i \) is the vibrational quantum number of the \( i \)th mode, \( x_{ij} \) is the anharmonic correction term. Applying the perturbation theory to the second-order [22-24], one can obtain \( x_{ij} \) in terms of the cubic and quartic force constants. The resulting anharmonic fundamental, the overtone and the combination band frequencies are \( \nu_i = \omega_i + 2x_{ii} + \sum_{j \neq i} n_j x_{ij} \), \( \nu_{2i} = 2\nu_i + 2x_{ii} \) and \( \nu_{ij} = \nu_i + \nu_j + x_{ij} \), respectively, from which one obtains the diagonal anharmonicity: \( \Delta_{ii} = 2\nu_i - \nu_{2i} = -2x_{ii} \), and the mixed-mode off-diagonal anharmonicity \( \Delta_{ij} = \nu_i + \nu_j - \nu_{ij} = -x_{ij} \). The diagonal anharmonicity can be written as [22-24]:

\[
\Delta_{ii} = \frac{1}{8} \Phi_{ii} + \frac{5\Phi_{ii}}{3\omega_i} + \sum_{k \neq i} \Phi_{ik} \left( 8\omega_k^2 - 3\omega_i^2 \right) \left( 4\omega_k^2 - \omega_i^2 \right).
\]

(2)
The first two terms of equation (2) incorporate exclusively energy derivatives with respect to the \( i \)th mode whose diagonal anharmonicity is being considered. The coefficients \( \Phi_{ijk} \) and \( \Phi_{ijkl} \) are the third and fourth derivatives of the potential that involve other normal coordinates. The off-diagonal anharmonicity for any two vibrators \( i \) and \( j \) can also be expressed in terms of the cubic and quartic force constants and harmonic frequencies:

\[
\Delta = \frac{1}{4} \left[ \Phi_{ij} + \Phi_{ij} + \frac{2\Phi_{ij} + 2\Phi_{ij}}{4\omega_i^2 - \omega_j^2} + \frac{2\Phi_{ij} + 2\Phi_{ij}}{4\omega_j^2 - \omega_i^2} \right] + \frac{1}{4} \sum_{k \neq i,j} \left[ \Phi_{ik} + \Phi_{ik} + \frac{2\Phi_{ik} + 2\Phi_{ik}}{2(\omega_i^2 + \omega_j^2 + \omega_k^2) - 2(\omega_i^2 + \omega_j^2 + \omega_k^2 + \omega_i^2)} \right]
\]

The first bracket contains the interaction between mode \( i \) and \( j \), while the second line is due to the interaction of mode \( i \) and \( j \) with the remaining \( 3N-8 \) modes. In addition, the composition of \( \Delta_{ii} \) and \( \Delta_{ij} \) can be examined for a given vibrational mode to investigate the localization degree of the anharmonic forces [28]. Examples of such calculations have been given previously [24,29,30].

### 2.2. Anharmonic vibrational coupling and local modes

The through bond and through space interactions amongst vibrational chromophore units cause the anharmonic vibrational excitations to exchange from site to site. This is the physical origin of vibrational coupling. There are several ways to assess the vibrational coupling. The first approach is through \textit{ab initio} computations. Wavefunction de-mixing of a \( N \)-unit coupled system can yield \( N \) local mode frequencies and \( 1/2(N-1) \) bilinear couplings [29]. This method is ideal for a collection of vibrational chromophores of the same kind. Taken the amide-I mode for example, a collection of normal modes can be treated as a linear combination of uncoupled local modes, whose mixing angle \( \xi \) defined below can be obtained from the normal mode eigenvectors [29]:

\[
\xi = \frac{1}{2} \tan^{-1} \left[ \beta \sqrt{\left( \nu_i^0 - \nu_j^0 \right)^2} \right]
\]

where \( \beta \) is the coupling of two local states with frequencies \( \nu_i^0 \) and \( \nu_j^0 \). Normal-mode displacement in the basis of the entire \( 3N-6 \) normal modes can be obtained by a frequency calculation, from which the vibrational wave functions of the amide-I normal mode in the reduced normal mode basis can be reconstructed. For the amide-I modes in a peptide system such a calculation is straightforward if the mode is assumed to be mainly a C=O stretching vibration. In this way an \( N \) by \( N \) matrix (thus a reduced amide-I subspace from the entire \( 3N-6 \) normal modes) was obtained for a system containing \( N \) amide units. Through such a procedure, the transition frequency of the local modes, the wave function mixing angle, and intermode coupling are obtained together. This method is particularly useful for assessing the coupling strength between the nearest neighboring chromophores that are covalently-bonded.
The second approach is to use transition multipole interaction. Bilinear term in the expansion of the normal mode displacement of vibrational oscillator is the lowest order of the through space interaction potential [3]. The couplings can be evaluated conveniently either by using an electrostatic transition dipole coupling (TDC) scheme [31,32], or using the transition charge and charge flux interaction [3,33], or using the distributed transition-charge density derivative interaction proposed previously [34]. In these methods, the couplings of different vibrational modes were assumed to depend solely on the molecular structure. For the amide-I mode in peptides, if the two amide units are covalently bonded, the transition charge-based approaches have advantages over the transition dipole approach. However, as the inter unit distance increases, all the approaches tend to give the same answer.

The TDC is computed by using the following formula:

$$
\beta_{ij} = \left[\left(\mu_i \cdot \mu_j\right) - 3\left(\mu_i \cdot e_r\right)(\mu_j \cdot e_r)\right] / r_{ij},
$$

where $\mu_i$ is the transition dipole in (DÅ⁻¹amu⁻¹/₂) units, $r_{ij}$ is the distance between dipoles (in Å), $e_r$ is the unit vector connecting $i$th and $j$th vibrators.

The transition charge interaction approach has also been formulated for the amide-I mode in peptides [35]. In this method, atomic partial charge and transition charge are needed, which can be evaluated using the Mulliken charges and charge-fluxes via \textit{ab initio} calculations [33,35-38]. The inter-site potential is approximated by the second-order expansion in terms of the normal modes [3]:

$$
\beta_{ij} = \frac{1}{4\pi\varepsilon_0} \sum_{l,r,i} Q_l Q_r \left[ \frac{1}{2} \sum_{a,b,i,j} r_a r_b \left( q_{a,i}^0 + \delta q_{a,i} Q_r \right) \left( q_{b,j}^0 + \delta q_{b,j} Q_r \right) \right]_{i,j=1} / r_{a,i} r_{b,j}.
$$

In equation (6), $\beta_{ij}$ is the so-called pair-wise vibrational coupling for the $i$th and $j$th amide groups; $a,b,i,j$ are the atoms that involved in the two amide-I normal mode displacement, which are C, O, N and H atoms here; $q_{a,i}^0$ is the atomic partial charge of the $a$th atom; $\delta q_{a,i}$ is the transition charge for the $a$th atom in the normal mode $Q_r$; $r_{a,i}$ is the distance between the two atoms; and $\varepsilon_0$ is the dielectric constant. We use a monopeptide model compound, namely N-methylacetamide (NMA), for parameterization, as also previously described [33,35]. Here, the charges and charge fluxes can be refined to produce the desired transition dipole strength for the amide-I band [37], or to fit IR and Raman signals [40,41]. For NMA, the charges and charge fluxes obtained at the B3LYP/6-31+G* level yields a transition dipole magnitude of 0.38 D, in fair agreement with a previous report [31]. Further, as pointed out earlier [3], other charges schemes, such as Merz-Kollman [42], CHELP [43], CHSLPG [44], NPA [45] and dipole-derivative derived charges [39] are also potential choices for this purpose.
In the TDC approach, the angle between the transition dipole and amide C=O bond is usually set to between 15° and 23° to fit experimental IR spectra. In the TCI approach, the calculated orientation of the transition dipole is found to be ~20° with respect to the C=O bond axis and towards the nitrogen atom. This angle falls into the experimentally determined range (15° to 25°) for the model compound NMA [46]. However, various values of this angle have been obtained theoretically (between -19° and 20°) when using different force fields even for the same model compound [32,47-49].

When the through bond interaction is important, the \textit{ab initio} computation approach has to be used. For peptides in conformation covering the entire Ramachandran space, vibrational coupling maps for the amide-I mode based \textit{ab initio} computations have been documented in literature [38,50-52]. A more detailed \textit{ab initio} computation based coupling map for the amide-I mode is also available for peptides in helical conformations [3], or in the region of the polyproline-II conformations [53]. The local-mode frequency map for the amide-I modes of peptides has also been made available [51].

\section*{2.3. Potential energy distribution}

To evaluate how much a normal mode is delocalized onto its neighboring unit of the same kind, the potential energy distribution (PED) analysis can be carried out on the basis of the internal coordinates. This method has been recognized for some time [32]. The obtained PED value can be used to describe the relative contributions of various displacement coordinates to the total change in potential energy during a specific vibrational motion. When a normal mode $Q_k$ is excited, the potential energy $V_k$ of the molecule can be expressed as [32]

$$ V_k = \frac{1}{2} \sum_i Q_i^2 \lambda_i, $$

where $\lambda_i$ measures the potential energy change for unit displacement of $Q_i$, and

$$ \lambda_i = \sum_{ij} F_{ij} L_{ik} L_{jk}. $$

Here $F_{ij}$ is the force constant in internal coordinates, and $L_{ik}$ is the element of the eigenvector of the GF matrix [23]. The PED values are obtained using the vibrational energy distribution analysis (VEDA) [54]. The information on the coordinate orientation, force constants in Cartesian coordinates and frequencies with atom displacement matrix are extracted from \textit{ab initio} computations.

\section*{2.4. Simulation of 1D IR spectra}

In the following, we introduce two simple frequency-domain methods for simulating 1D IR spectra of peptides. First, for the entire $3N-6$ normal modes of a given molecule, a straightforward way of simulating its 1D IR spectra is to use the \textit{ab initio} computed (anharmonic) frequencies and intensities. Assuming certain line broadening functions, one can obtain the
simulated broadband 1D IR spectra. A combination of Lorentzian and Gaussian functions is usually used for homogeneous and inhomogeneous contributions to the line broadening. Even though the widths of these two functions can be set flexibly for each vibration in order to compare with experimental IR spectra, the obtained line width is not physically meaningful.

The excitonic modeling, on the other hand, is particularly useful for simulating the linear IR spectra of a set of identical vibrational modes in the frequency domain. It has been used effectively to the amide-I mode of peptides. The excitonic band structure is illustrated in Figure 1, in which site states and excitonic states are shown. A set of coupled anharmonic oscillators, i.e., the site states \( |m\rangle \), forms the one-quantum states \( |k\rangle \). The so-called one-exciton Hamiltonian for a particular polypeptide labeled by the index \( n \), was chosen as M coupled harmonic oscillators [3]:

\[
H_e = \sum_{m} (\varepsilon + \xi_{m}^{(n)}) |m\rangle \langle m| + \sum_{m \neq l} \beta_{ml}^{(n)} |m\rangle \langle l|
\]  

In equation (9), \( \varepsilon \) is defined as the vibrational transition frequency (or site energy) of the \( m \)th amide-I mode (\( m = 1 \) to \( M \)) in the \( n \)th polypeptide. The normal distribution (Gaussian distribution with the standard deviation \( \sigma \)) is very useful to describe the site energy fluctuations \( \{\xi_{m}^{(n)}\} \) in the fashion of “white noise” (where \( n \) denotes sampling size). The ensemble properties can be obtained by averaging over \( N \) molecules. However, special distributions can also be employed to account for correlated energy fluctuations in the fashion of “color noise”. The pair-wise coupling \( \beta_{ml}^{(n)} \) can be computed using various coupling schemes described above. Standard bond lengths and angles can be generated easily for peptides with known coordinates of heavy atoms. Further, the diagonal disorder describes the static ensemble averaging, which is valid in the case of Bloch dynamics [55-57] where the fast and slow structural dynamics are separated in time.

**Figure 1.** Excitonic model. A set of site states forms the one-excitonic band due to vibrational coupling. Only one-quantum states are given. Transition dipoles for both site states and excitonic states are shown.
The strength of the transition dipole of each eigenmode gives the total linear IR spectrum, as shown previously [3]:

$$S(\omega) = \left\{ \sum_{k=0}^{M} |\mu_{0k}|^2 \left( \frac{\gamma_{0k}}{(\omega - \omega_{0})^2 + \gamma_{0k}^2} \right) \right\}$$  \hspace{1cm} (10)$$

where $\mu_{0k} = \sum_{m=1}^{M} a_{km}(n) \mu_{0m}$, $\mu_{0m}$ is the local transition dipole vector of the $v = 0 \rightarrow v = 1$ transition of the $m$th amide unit in a peptide conformation and $a_{km}(n)$ is the amplitude of the site $m$ in the eigenstate $k$. $\gamma_{0k}$ is the homogeneous linewidth for the $|0 \rangle \rightarrow | k \rangle$ transition.

3. Results and discussion

3.1. Conformation dependent amide-I normal mode vibration in peptide oligomers

First we examine the anharmonic parameters of the amide-I mode of a model dipeptide. The molecular structure of the glycine dipeptide (Ac-Gly-NMe, or CH₃CONHC₂H₂CONHCH₃) is shown in Figure 2, in which backbone dihedral angles are defined to be $\phi$ (CNCαC) and $\psi$ (NCαCN). Here ten well-known secondary conformations are chosen, namely $\alpha_L2$-helix ($\phi = +90^\circ$, $\psi = -90^\circ$); $\pi$-helix ($-57^\circ$, $-70^\circ$); polyproline-II (PPⅡ, $-75^\circ$, $+135^\circ$); $\alpha_L1$-helix ($+60^\circ$, $+60^\circ$); C₇ conformation ($+82^\circ$, $-69^\circ$); extended structure ($180^\circ$, $-180^\circ$); $\alpha$-helix ($-58^\circ$, $-47^\circ$); 3₁₀-helix ($-50^\circ$, $-25^\circ$); anti-parallel $\beta$-sheet ($-139^\circ$, $+135^\circ$); and parallel $\beta$-sheet ($-119^\circ$, $+113^\circ$). Harmonic and anharmonic frequencies of the two amide-I modes in these dipeptides are evaluated using the density functional theory and Hartree-Fock (HF) methods. The results from the two methods are found to be highly correlated, as shown in Figure 3. Two amide-I normal modes in these dipeptides are linear combinations of the two amide-I local modes, which are dominated by the C=O stretching vibration. In the left column of Figure 3, two amide-I normal mode frequencies (harmonic picture) are shown: one is the symmetric stretching and has a relatively higher frequency (panel A) and the other is the asymmetric stretching whose frequency is lower (panel C). In order to better compare the HF frequencies (squares) and DFT frequencies (circles), the HF results are subtracted by 150 cm⁻¹. The results show that the calculated normal-mode harmonic frequencies at the level of Hartree-Fock theory have the same trend as those obtained at the level of the density functional theory. One can also draw the same conclusion from the anharmonic frequencies that are given in the right column of Figure 3 (panel B and D). In addition, the frequency difference between the high- and low-frequency modes in the harmonic picture (panel E) and in the anharmonic picture (panel F) are also meaningful to compare, because the frequency separation is closely related to the inter-mode coupling. Clearly the frequency separations obtained by the HF and DFT methods are also in good agreement, for both the harmonic and anharmonic cases. Further more, for the ten conformations the averaged DFT anharmonic frequency of the high-frequency mode is found to be 31.7 cm⁻¹ lower than that of the harmonic frequency, indicating the effect of considering the
anharmonic potential. Similarly, the lowered value is 28.7 cm$^{-1}$ for the low-frequency mode.

On the other hand, for the HF results, the anharmonic frequency drops 29.0 cm$^{-1}$ for the high-frequency mode, and 26.0 cm$^{-1}$ for the low-frequency mode. This indicates a similar anharmonic energy decrease using the two different methods. However, it is also noted that for some typical structures the frequency splitting show method-dependence, which will result in method-dependent inter-mode coupling, as discussed below. The performance of the DFT (B3LYP) and HF methods in computing the anharmonicities of the amide-I modes of peptide oligomers has been examined previously [29] and it was shown that the two methods were able to provide an optimum compromise between reliability and computer time.

Next, the full conformation space (-180° ≤ ϕ ≤ +180°, -180° ≤ ψ ≤ +180°) for peptide backbone is explored with total 169 samplings of partially optimized structures (Δϕ = Δψ = 30°). The partial optimization is performed at the HF level of theory by fixing ϕ and ψ to desired values each
time, to sample the entire conformational space. The result is given in Figure 4. The two amide-I normal-mode frequencies (panel A and B) show significant conformation sensitivity, with different dependences on the two dihedral angles. In panel A, the harmonic high-frequency component exhibits a low-frequency region that is anti-diagonally arranged (from lower right to upper left). In panel B, the harmonic low-frequency component, however, exhibits a similarly arranged low-frequency region, but in much smaller area. The conformational dependences of the anharmonic normal-mode frequencies, which are given in panel C and D respectively, resemble those of their harmonic counterparts (panel A and B respectively). However, a detailed analysis shows subtle difference in mean value and distribution of the harmonic and anharmonic frequencies: on average the anharmonic frequency drops ca. 30 cm\(^{-1}\) from the harmonic frequency. Further, the obtained harmonic frequencies change more dramatically along \(\psi\) in the region of \((-90^\circ \leq \phi \leq 90^\circ)\), as shown in Figure 4 (panel A and B). A similar behavior has been observed in a previous study [52]. Our results show that such a pattern still remains in the behavior of the anharmonic frequencies \(\nu_i\) and \(\nu_j\) in the \((\psi, \phi)\) conformational space (panel C and D).

![Figure 4. Conformation-dependent normal-mode frequencies (in cm\(^{-1}\)) for the two amide-I modes with and without anharmonic correction. (A): high-frequency harmonic component (\(\omega_i\)); (B): low-frequency harmonic component (\(\omega_j\)); (C): high-frequency anharmonic component (\(\nu_i\)); and (D): low-frequency anharmonic component (\(\nu_j\)). Frequencies are subtracted by 1900 cm\(^{-1}\). Adapted from reference [30] with permission.](image)

### 3.2. Conformation dependent amide-I local mode vibration in peptide oligomers

Local-mode frequencies can be obtained by decoupling the two amide-I normal modes in either the harmonic or anharmonic picture. The results are shown in Figure 5. In the harmonic picture, the obtained zero-order amide-I vibration frequency (denoted as \(\omega_{i0}\)) of the NMe side (or the C-terminus side, as shown in Figure 2) is generally higher than the zero-order frequency.
denoted as \( \omega_j^0 \) of the Ac side (or the N-terminus side). The two harmonic local-mode frequencies also show quite different dihedral-angle dependences, which is clearly shown in A and B panels. Figure 5A depicts a relatively larger low-frequency area (anti-diagonally located) for \( \omega_i^0 \), with a mean value of \( \bar{\omega}_i^0 = 1943.8 \text{ cm}^{-1} \). Figure 5B shows a relatively smaller low-frequency area with a mean value of \( \bar{\omega}_j^0 = 1934.3 \text{ cm}^{-1} \). Further, the conformational dependence of the harmonic local-mode frequencies bears a strong resemblance to that of the normal-mode frequencies. This is evident by comparing Figure 5 and Figure 4. The harmonic local-mode picture shown in Figure 5 A and B is also quite similar to that reported in a previous work [58], in which B3LYP functional and 6-31+G* basis set were used.

In the anharmonic picture, the conformational dependence of the local-mode frequencies differs slightly from that in the harmonic picture. The results are shown in Figure 5, C and D panels. In panel C, the conformational dependence of the zero-order vibrational frequency (\( \nu_i^0 \)) of the amide-I unit at the C-terminus side is shown, while in panel D the conformational dependence of the zero-order vibrational frequency (\( \nu_j^0 \)) of the amide-I unit at the N-terminus side is shown. It is found that their mean values are \( \bar{\nu}_i^0 = 1914.3 \text{ cm}^{-1} \) and \( \bar{\nu}_j^0 = 1904.5 \text{ cm}^{-1} \), respectively, thus \( \bar{\nu}_i^0 - \bar{\nu}_i^0 = 5.5 \text{ cm}^{-1} \) and \( \bar{\nu}_j^0 - \bar{\nu}_j^0 = -5.1 \text{ cm}^{-1} \). This means that in the anharmonic picture, the average frequency splitting between the two amide-I modes due to coupling is 10.6 cm\(^{-1}\), while in the harmonic picture the average frequency splitting is slightly larger (12.0 cm\(^{-1}\)). One can also estimate the average frequency splitting \( (\bar{\nu}_i^0 - \bar{\nu}_j^0) \), which is 9.8 cm\(^{-1}\), indicating the extent of local-mode non-degeneracy in the anharmonic picture.

Thus the computation results shown in Figure 5 indicate a generally non-degenerate zero-order frequency picture under both the harmonic and anharmonic approximations. Such a non-degeneracy is believed to be an intrinsic property of polypeptides. For example, in a \(^{13}\)C labeled β-hairpin two amide-I modes on the same peptide chain are found to have different zero-order frequencies by both 1D and 2D IR studies [59]. The non-degeneracy of the local states is believed to be due to the variation of local chemical and solvent environment of peptide amide group (-CONH-) [60]. Such a non-degenerate local-mode picture should be taken into account during empirical modeling of the 1D and 2D IR spectra of peptides and proteins. In particular, a set of zero-order transition energies can be initialized as the diagonal elements of the one-exciton Hamiltonian. Because these local-mode frequencies are backbone dihedrals (\( \phi, \psi \)) dependent, they bear site-specific local structure characteristics and are also sensitive to solvent environment. On the other hand, the normal modes in peptides do not carry direct local-structure identities because of the mode delocalization. Under such circumstances the IR frequency and peptide structure relationship cannot be established in a straightforward way. It is for these reasons that peak assignment in conventional IR spectroscopy could be troublesome.

Further, because the amide-I local-mode frequency in the conformational space in the anharmonic picture appears to be quite similar to that in the harmonic picture one may scale the frequency from the latter to the former. This suggests a simple way to approximately obtain the anharmonic frequencies. However, care should be taken when the scaling method is
utilized, because it is well known that the frequency scaling is not applicable simultaneously to all the $3N-6$ modes in a molecule. The frequency scaling scheme would be useful only when a very limited number of modes were considered; for example, amide-I modes only in this case. Furthermore, to obtain solution-phase vibrational frequencies, solution-phase frequency models has to be established, and several of such have become available particularly for the amide-I modes [58,61,62]. In addition, for a solvated peptide, the solvation effect may be added to the scaled harmonic frequencies or to the un-scaled anharmonic frequencies so as to yield modified zero-order frequencies for spectral modeling.

3.3. Anharmonicity, coupling and mode delocalization

In this work the diagonal anharmonicity is defined as the decrease of the energy gap between the first excited state and its overtone state ($n = 1$ and $n = 2$ where $n$ is the vibrational quantum number) with respect to that of the ground state and first excited state ($n = 0$ and $n = 1$). The diagonal anharmonicity, inter-mode coupling, and mode delocalization are very important anharmonic parameters. The conformational dependence of these parameters is examined and the results are given in Table 1 for several dipeptides in which two units are either covalently bonded or hydrogen bonded.

We first discuss the anharmonicity of a single vibrator case. In an isolated peptide unit, for example, trans-NMA, the amide-I mode is highly localized, the diagonal anharmonicity is found to be 18.0 cm$^{-1}$ by computation. The diagonal anharmonicity begins to change and exhibits conformational sensitivity in a two-vibrator case. For example in alanine dipeptide
with the α-helical conformation (−58°, −47°) the anharmonicities of both amide-I modes are smaller than that in the isolated amide unit, whereas in the conformation (−75°, +135°) and both anharmonicities are comparable with the value in the isolated amide unit. In AcProNMe the anharmonicity decreases for the C=O hydrogen-bonded amide-I mode. In hydrogen-bonded trans-NMA dimer, for the free and C=O hydrogen-bonded amide-I modes, the two diagonal anharmonicities decrease even more. Experimentally, an anharmonicity of 16.0 cm⁻¹ was reported for NMA [63], and smaller values were reported for two spatially connected amide units in different conformations, for example, 9-11 cm⁻¹ in the α-helix [64] and 13±2 cm⁻¹ in the amino-end amide of AcProNH₂ [65]. Also, relatively large value (ca.16.0 cm⁻¹) was found for two amide units in an alanine dipeptide with a negligible coupling constant [53]. Thus the calculated values correlate reasonably with the experimental results. This suggests that the diagonal anharmonicity of the amide-I mode may serve as a probe for the secondary structure of peptides, while only the off-diagonal anharmonicity was believed to be useful previously for structural determination because of its link to the pair-wise coupling of two vibrators.

As shown in equation (4), the wave function mixing angle is determined by the coupling and transition energy gap of two local modes. Large mixing angle means large mode delocalization. The results of the mixing angle and inter-mode coupling for several dipeptides are listed in Table 1. For alanine dipeptide in the α-helical conformation (ϕ, = −58°, ψ = −47°), the mixing angle between two local states is ξ = 31.8°, while the inter-mode coupling is 4.9 cm⁻¹ in the anharmonic picture (or 6.0 cm⁻¹ in the harmonic picture). Thus somewhat different coupling is expected when using the anharmonic frequency scheme rather than the harmonic case, even though the latter approach has been very popular previously [3,38,66]. For the dipeptide with dihedral angles of (−75°, +135°), the mixing angle is ξ ≈ 0.1°, and the coupling is very small (between −0.01 and −0.08 cm⁻¹) regardless of which frequency scheme is used. For the dipeptide with dihedral angles of (−50°, −25°), the mixing angle is ξ = 69.5° and the inter-mode coupling is 6.0 cm⁻¹ in the anharmonic picture (but −1.0 cm⁻¹ in the harmonic picture). For AcProNMe, the mixing angle is ξ ≈ 8.9° and the coupling is ca. −8.2 cm⁻¹ using either frequency scheme. In the case of the trans-NMA dimer, the mixing angle between two local states is ξ = 24.2°, while the inter-mode coupling is −3.1 cm⁻¹ in the anharmonic picture or −5.0 cm⁻¹ in the harmonic picture. Further, from the results shown in Table 1, one sees that generally the larger the diagonal anharmonicity, the smaller the mixing angle. The correlation between the anharmonicity and mode delocalization has been noted previously in the case of the C=O stretching modes of acetic acid dimer [67].

The term |tan²ξ| is a very sensitive measure of the vibrational delocalization. However, from equation (4) one obtains |tan²ξ| = |β_{ij}|/|ν_{ij} - ν_{ij}^0|, suggesting that highly delocalized states may not be strongly coupled. This is because, |tan²ξ| is determined by the ratio of the coupling and frequency separation. Thus for the case of a significant coupling but a much larger energy separation, one could still have |tan²ξ| ≪ 1, i.e., localized but still strongly coupled states. Two typical examples are shown in Table 1. For alanine dipeptide in the α-helical conformation, the two amide-I modes are both significantly delocalized (|tan²ξ| = 1.0) and coupled (β_{ij} = 4.9 cm⁻¹). For the remaining dipeptides, the amide-I modes are largely
localized (with small $|\tan \xi|$), but the strength of coupling varies. In particular, proline dipeptide AcProNMe shows a significant coupling ($\beta_{ij} = -8.2 \text{ cm}^{-1}$), but the two states are pretty much localized, which is mainly because of the presence of two largely separated transition frequencies.

Further, the degree of mode delocalization can be characterized by using the potential energy distribution that describes the relative contributions of various displacement coordinates to the total change in potential energy during the vibration. Here we examine the mode delocalization in gas-phase and in explicit solvent environment. We carry out computations at the harmonic level for alanine dipeptide systems in either $\alpha$-helical or $\beta$-sheet conformation, with four water molecules included in each case. The results are given below (Figure 6 and Table 2). Similar short peptide systems were examined previously to study the hydration effect of peptides [68]. The solution-phase local-mode frequencies are found to red shift from those in the gas-phase because the two amide units are both H-bonded with solvent molecules (Table 2). However, it is clear the frequency separations between the high-frequency mode and low-frequency mode for ADP in gas and in solution phases are quite similar. So it is expected that the decoupled local mode frequency separations are similar too. In other words, solvent effect on frequency separation (and mode localization caused by that) is not significantly affected by the first hydration layer in this case.

<table>
<thead>
<tr>
<th>$i$th and $j$th amide-I modes</th>
<th>alanine dipeptide</th>
<th>proline dipeptide</th>
<th>NMA dimer</th>
</tr>
</thead>
<tbody>
<tr>
<td>$(\phi, \psi)$</td>
<td>$(\phi, \psi)$</td>
<td>$(\phi, \psi)$</td>
<td>$(\phi, \psi)$</td>
</tr>
<tr>
<td>$\nu_i^0$</td>
<td>1734.2</td>
<td>1714.0</td>
<td>1734.8</td>
</tr>
<tr>
<td>$\nu_j^0$</td>
<td>1729.3</td>
<td>1675.0</td>
<td>1748.7</td>
</tr>
<tr>
<td>$\Delta \nu$</td>
<td>11.5</td>
<td>21.3</td>
<td>14.9</td>
</tr>
<tr>
<td>$\beta_{ij}$</td>
<td>4.9</td>
<td>-0.1</td>
<td>6.0</td>
</tr>
<tr>
<td>$\xi$</td>
<td>31.8</td>
<td>0.1</td>
<td>69.5</td>
</tr>
<tr>
<td>$</td>
<td>\beta_{ij}/(\nu_i^0-\nu_j^0)</td>
<td>$</td>
<td>1.0</td>
</tr>
</tbody>
</table>

Table 1. Anharmonic local-mode frequency ($\nu$, in cm$^{-1}$), anharmonicity ($\Delta$, in cm$^{-1}$), coupling ($\beta$, in cm$^{-1}$), and wave function mixing angle ($\xi$, in degree) for two nearest neighboring amide units in various dihedral angles ($\phi$ and $\psi$, in degree). The diagonal anharmonicity is obtained from the $ab\ initio$ calculations. Adapted from reference [29] with permission.

One sees that the PED values of the two modes decrease similarly (with a few percent variation). This is found to be the case for both conformations. Here the decreased PED indicates more mode delocalization, reaching over water bending modes through hydrogen-bonding interactions. This hydration picture is reasonable for short peptides because one can hardly have one amide unit hydrogen-bonded with solvent and another not, in a solvated short
peptide. This suggests that given a homogeneous solvent environment, the amide-I mode-delocalization in short peptide would probably change similarly for each amide unit. Note that for longer peptides containing different side chains and forming intramolecular hydrogen-bonds, it might be true that only some of the amide-I frequencies would be red-shifted due to hydrogen-bonding interaction, but certainly this is a case-dependent story.

<table>
<thead>
<tr>
<th>mode</th>
<th>α-helix</th>
<th>β-sheet</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>gas phase</td>
<td>solution phase</td>
</tr>
<tr>
<td></td>
<td>$\omega_1$</td>
<td>PED</td>
</tr>
<tr>
<td>a</td>
<td>1771.1</td>
<td>0.57</td>
</tr>
<tr>
<td>b</td>
<td>1758.0</td>
<td>0.58</td>
</tr>
</tbody>
</table>

Table 2. Computed harmonic frequency and PED for the amide-I modes in ADP- $(H_2O)_4$ in the α-helix and β-sheet conformations at the level of B3LYP/6-31+G*.

3.4. Simulated 1D IR spectra of peptides

The simulated 1D IR spectra of two typical turn conformations (Table 3) employing the vibrational exciton model in the frequency domain are shown in Figure 7. More details can be found in a recent work [3]. Discernable conformational-dependent spectral features are seen in simulated 1D IR spectra of these peptide structures. The spectral features include absorption peak positions and line width profiles. For the γ-turn, two amide-I local modes are coupled
and transition intensities are not equal. For the β–turn, three coupled local transitions form excitonic band structure (normal modes) that differs from that of the γ–turn. In Figure 7, stick spectrum are also given in each panel. Inhomogeneous distribution of the transition energies are clearly shown in each case [69]. Further, because of transition intensity transfer, a direct result of vibrational coupling, the computed 1D IR spectra show patterns that significantly different from the local-mode picture with three independent bands.

<table>
<thead>
<tr>
<th>species</th>
<th>dihedral angles</th>
<th>hydrogen-bonding ring</th>
</tr>
</thead>
<tbody>
<tr>
<td>γ–turn</td>
<td></td>
<td></td>
</tr>
<tr>
<td>classic</td>
<td>ω₁ 74.9</td>
<td>ψ₁ -75.0  -170.8</td>
</tr>
<tr>
<td>β–turn</td>
<td></td>
<td></td>
</tr>
<tr>
<td>type I</td>
<td>ω₁ 60.0</td>
<td>ψ₁ -30.0  -177.1  -90.0 +0.0 -171.2</td>
</tr>
</tbody>
</table>

Table 3. Glycine-based peptide oligomers in turn conformations: Ac−Glyₙ−NMe (n = 1 for the γ–turn and n = 2 for the β–turn).

Figure 7. Simulated 1D IR of selected peptide fragments in (A) the classic γ-turn and (B) the type-I β-turn. Sticks indicate ensemble sampling.

4. Conclusions

This chapter discusses the methods and application of anharmonic vibration parameters for the purpose of connecting the secondary structure of proteins and peptides to their IR spectra. Using the amide-I mode in particular, the usefulness of the methods is clearly demonstrated. The performance of the DFT and HF theories in predicting the anharmonic frequencies are compared and the conformational dependence of the obtained parameters are examined. The methods to compute vibrational coupling are also reviewed and examples are discussed. The coupled nature of the amide-I band for typical secondary structures is analyzed using the potential energy distribution function, and the local-mode properties (frequency and coupling) are discussed. Since the solvent effect on these parameters is unavoidable, as has shown for PED analysis, solvent molecules must be taken into account in assessing the vibrational
properties of solute. Polarizable continuum method [70] for solvent model can be used for such purposes. In addition, site-dependent dynamical interactions between peptide and water molecules in the hydration shells needs to be examined by molecular dynamics simulations employing proper molecular mechanical force fields, so that the statistical distributions and correlations of the transition frequencies can be computed. This can be done by carrying our instantaneous normal mode analysis, for example. Time-dependent vibrational couplings can also be computed based on the molecular dynamics trajectories. Nevertheless, simultaneous assessment of vibrational parameters of multiple vibrational modes shall prove useful in understanding the characteristics of linear and nonlinear infrared spectra of both static and equilibrium dynamical structures of proteins, peptides and other biomolecules [71].

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Author details

Jianping Wang*

Address all correspondence to: jwang@iccas.ac.cn

Institute of Chemistry, the Chinese Academy of Sciences, Beijing National Laboratory for Molecular Sciences, Beijing, P. R. China.

References


