We are IntechOpen, the world’s leading publisher of Open Access books
Built by scientists, for scientists

6,600 Open access books available
177,000 International authors and editors
195M Downloads

154 Countries delivered to
TOP 1% Our authors are among the most cited scientists
12.2% Contributors from top 500 universities

WEB OF SCIENCE™
Selection of our books indexed in the Book Citation Index in Web of Science™ Core Collection (BKCI)

Interested in publishing with us?
Contact book.department@intechopen.com

Numbers displayed above are based on latest data collected.
For more information visit www.intechopen.com
Rainfall Prediction Using Teleconnection Patterns Through the Application of Artificial Neural Networks

Gholam Abbas Fallah-Ghalhari  
Sabzevar Tarbiat Moallem University  
I.R of Iran

1. Introduction

All aspects of human life are, directly or indirectly, affected by climatic processes. This effect is especially noticeable in such fields as agriculture, irrigation, economy, telecommunications, transportation, traffic, air pollution and military industries (Haltiner & Williams 1980).

A number of researchers have studied the possibility of forecasting rainfall several months in advance using climate indices such as SOI, PDOI and NPI (e.g. Silverman and Dracup 2000).

A well-known atmospheric phenomenon is the Southern Oscillation (SO). The SO is an atmospheric see-saw process in the tropical Pacific sea level pressure between the eastern and western hemispheres associated with the El Niño and La Niña oceanographic features. The oscillation can be characterized by a simple index, the Southern Oscillation Index (SOI). (Kawamura et al., 1998). The Pacific Decadal Oscillation index (PDOI) is the leading principal component of monthly sea surface temperature (SST) anomalies in the North Pacific Ocean north of 20°N (Zhang et al., 1997; Mantua et al., 1997). Trenberth and Hurrell (1994) have defined the North Pacific Index (NPI) as the area-weighted sea level pressure over the region 30°N to 65°N, 160°E to 140°W to measure the decadal variations of atmosphere and ocean in the north Pacific.

Furthermore, the existence of substantial databases of sea surface temperature anomalies (SST) opens the possibility of using these data to forecast rainfall several months in advance. Most of the research carried out in this area has used traditional statistical methods such as linear correlation or time series methods to identify the significant variables. These methods test for a linear relationship between the independent variables and rainfall, whereas the relationships are more likely to be non-linear as the underlying processes are themselves non-linear (Iseri et al. 2005).

Long-term rainfall prediction is very important to countries thriving on agro-based economy. In general, climate and rainfall are highly non-linear phenomena in nature giving rise to what is known as butterfly effect (Abraham et al. 2001). In their quest for new ways of predicting important meteorological factors, researchers have devised and developed techniques such as intelligent methods, which are viable and flexible means independent of system dynamic models.
Pongracz & Bartholy (2006) designed a model of monthly rainfall in Hungary using types of atmospheric circulation patterns and ENSO (El Niño - Southern Oscillation) index. To this end, they used a modeling technique based on fuzzy rules to establish a relationship between inputs and rainfall. Their results indicated that the model based on fuzzy rules provides an excellent means for the prediction of statistical features of rainfall using monthly occurrence of types of daily circulation pattern and delayed SOI.

Halid & Ridd (2002) used the fuzzy logic to design a model and predict local rainfall in January at Hasanuddin airport, Indonesia, which is the largest rice-producing area in the country. Their results indicated that, compared to other statistical models, the fuzzy logic model is more useful for the prediction of rainfall in January. Choi (1999) used neural networks and the Geographical Information System to forecast rainfall. The results indicated the efficiency of the Geographical Information System and neural networks in rainfall forecast. Cavazos (2000) used neural networks to forecast daily rainfall. The parameters which were used included the thickness between 500 and 1000 hecto-Pascal levels, the altitude of 500 hPa levels, and the humidity of 700 hPa levels. The outcomes indicated the efficiency of neural networks in the prediction of rainfall. Maria et al (2005) used neural networks and regression models to forecast rainfall in Sao Paulo, Brazil. The parameters they used included: potential temperature, vertical wind component, specific humidity, precipitable water, relative vorticity and humidity flux divergence. The results indicated the efficiency of both methods in forecasting rainfall.

One of the most crucial issues of global climatic variability is its effect on water resources. If more accurate predictions of rainfall were possible, this would enable more efficient utilization of water resources. However, long-term rainfall prediction models are still unsatisfactory, whereas short-term rainfall prediction models have undergone significant development. The probable reasons for the difficulties in conducting long-term rainfall prediction are the complexity of atmosphere-ocean interactions and the uncertainty of the relationship between rainfall and hydro meteorological variables. So far, long-term climate prediction using numerical models has not demonstrated useful performance, and statistical models have shown better performance than numerical models (Zwiers & Von Storch 2004). Consequently, in this study Artificial Neural Networks and linear regression models have been applied to nonlinear and linear statistical prediction.

Due to the significance of rainfall in many decision making processes such as water resources management and agriculture, the present study aims to find out the relationship between large-scale climatic synoptic patterns and regional rainfall using such synoptic patterns as sea level temperature and temperature difference, sea level pressure and pressure difference, precipitable water, air temperature at 700-hPa level, the thickness between 500 and 1000-hPa levels and the relative humidity at 300-hPa level.

2. Data and methods

2.1 Data

2.1.1 Study area

The region studied in this research is Khorasan Razavi Province. The time series studied is the average rainfall from April to June during 38 years. The data of spring rainfall for each
year includes the rainfall in 34 visibility, climatology and rainfall measurement stations provided by the Weather Bureau and the Power Ministry. Of these, 24 stations are rainfall measurement stations of the Power Ministry and the rest belong to the Weather Bureau. Fig. 1 represents the map of the studied area and the name of the relevant stations. To compensate for some defects in rainfall data, subtractions and ratios method have used. Run test was also used to test the homogeneity of the data. The analysis of runs within a sequence is applied in statistics in many ways (for examples see Feller 1968 & Ducan 1974). The term run may in general be explained as a succession of items of the same class. Many concepts to analyze runs in a series of data have been studied. The main concepts are based on (i) the analysis of the total number of runs of a given class (see Guibas and Odlyzko 1980 and Knuth 1981) and (ii) examinations about the appearance of long runs (see Feller 1968, Guibas and Odlyzko 1980 and Wolfowitz 1944).

Fig. 1. Map of the region under study and selected stations (Fallah Ghalhary et al, 2010)
2.1.2 Climatological data

The data used in this study are:

1. Rainfall station data for the seasonal rainfall (April – June) were obtained from Iranian Meteorological organization. All of these stations are in the north eastern region of Iran.

2. Large-scale ocean and atmospheric circulation variables such as Sea Surface Temperature (SST), Sea Level Pressure (SLP), the difference Sea Level Pressure, the difference Sea Surface Temperature between surface and 1000 hPa level, relative humid at 300 hPa level, geopotential height at 500 hPa level, air temperature at 850 hPa level during months (Oct-Mar). These data were obtained from NCEP/NCAR Re-analysis data. These data sets span the period of 1948 – current, covering the globe on a 2.5 × 2.5 grid and available at http://www.cdc.noaa.gov National Oceanic and Atmospheric Administration (NOAA) website. Table 1 summarizes the data used in this study.

<table>
<thead>
<tr>
<th>Data source</th>
<th>Data time period</th>
<th>Year</th>
</tr>
</thead>
<tbody>
<tr>
<td>organization</td>
<td></td>
<td></td>
</tr>
<tr>
<td>analysis variables</td>
<td>atmospheric circulation</td>
<td></td>
</tr>
</tbody>
</table>

Table 1. Summaries of the data used in this study

2.2 Methods

2.2.1 Spatial prediction and kriging

The need to obtain accurate predictions from observed data can be found in all scientific disciplines. Those that have embraced statistical notions of random variation are able to do this by exploiting the statistical dependence among the data and the variables(s) to be predicted. However, the statistical approach has not been without its detractors; for example, Philip and Waston (1986) argue that geostatistics is unhelpful for solving problems in mining and geology. Their article and the accompanying discussions are worth perusing.

It is helpful to explain first the terms used in the title of this chapter. Let \( \{Z(s): s \in D \subset \mathbb{R}^d\} \) be a random function (or process), from which n data \( Z(s_1), \ldots, Z(s_n) \) are collected. The data are used to perform inference on the process, here, to predict some known functional \( g(Z(.)) \) of the random function \( Z(.) \). For example, point prediction assumes \( g(Z(.)) = Z(S_0) \), where \( S_0 \) is a known spatial location. \( g \) is mostly real-valued. Sometimes interest is not in \( Z(.) \), but in a “noiseless” version of it.

Suppose that

\[
Z(s) = S(s) + \epsilon(s), \quad s \in D, \tag{1}
\]

Where \( \epsilon(.) \) is a white-noise measurement-error process. In this case, one is interested in predicting a known functional \( g(S(.)) \) of the noiseless random function \( S(.) \).

Spatial prediction refers to prediction either \( g(Z(.)) \) or \( g(S(.)) \) from data \( Z(s_1), \ldots, Z(s_n) \) observed at known spatial locations \( s_1, \ldots, s_n \).

Notice that my terminology encompasses the temporal notions of smoothing (or interpolation), filtering, and prediction (e.g., Lewis, 1986, PP. 36), which rely on time-
ordering for their distinction. If temporal data are available from the past up to and including the present, smoothing refers to prediction of \( g(S(.)) \) at time points in the past, filtering refers to prediction of \( g(S(.)) \) at the present time and prediction refer to prediction of \( g(S(.)) \) at time points in the future. In this paper, the word "estimation" will be used exclusively for inference on fixed but unknown parameters; "prediction" is reserved for inference on random quantities.

**Kriging** is a minimum-mean-squared-error method of spatial prediction that (usually) depends on the second-order properties of the process \( Z(.) \).

Matheron (1963) named this method of optimal spatial linear prediction after D. G. Krige, a South African mining engineer who, in the 1950s, developed empirical methods for determining true ore-grade distributions from distributions based on sampled ore grades (e.g., Krige, 1951). However, the formulation of optimal spatial linear prediction did not come from Krige's work. (See Matheron, 1971, pp. 117-119, and Cressie, 1990, for the extent of the early work of Krige.) The contributions of Wold (1938), Kolmogorov (1941), and Wiener (1949) all contain optimal linear prediction equations that reflect the notion that observations closer to the prediction point (for them, closer in time) should be given more weight in the predictor.

At the same time as geostatistics was developing in mining engineering under G. Matheron in France, the very same ideas developed in meteorology under L. S. Gandin (Gandin, 1963) in the Soviet Union. The original (and simultaneous) contribution of these authors was to put optimal linear prediction (in terms of variogram) into a spatial setting. Gandin's name for his approach was *objective analysis*, and he used the terminology *optimum interpolation* instead of Kriging. Details of the origins of Kriging are set out in Cressie (1990) and Cressie (1993).

### 2.2.1.1 Observational and spatial scale

The following model is useful. Suppose that the data \( (Z(S_1), \ldots, Z(S_n)) \) represent \( Z \) values at points of \( D \subset R^3 \), and that they are modeled as a partial realization of the random process:

\[
\{Z(s): S \in D \subset R^3\}, \tag{2}
\]

Which satisfies the decomposition

\[
Z(s) = \mu(s) + W(s) + \eta(s) + \epsilon(s), \quad s \in D, \tag{3}
\]

Where:

- \( \mu(.) \equiv E(Z(.)) \) is the deterministic mean structure that will be called *large-scale variation*.
- \( W(.) \) is a zero-mean, \( L_2 \)-continuous \([i.e., E(W(s + h) - W(s))^2 \rightarrow 0 \text{ as } |h| \rightarrow 0]\), intrinsically stationary process whose variogram rang (if it exist) is larger than \( \min \{||s_i - s_j||:1 \leq i < j \leq n\} \). Call \( W(.) \) *smooth small-scale variation*.
- \( \eta(.) \) is a zero-mean, intrinsically stationary, independent of \( W, \) whose variogram rang exists and is smaller than \( \min \{||s_i - s_j||:1 \leq i < j \leq n\} \). Call \( \eta(.) \) *microscale variation*.
- \( \epsilon(.) \) is a zero-mean white-noise process, independent of \( W \) and \( \eta \) call \( \epsilon(.) \) *measurement error or noise*, and denote \( \text{var} \( \epsilon(s)\) = \sigma^2 ME \). There are occasions when \( \epsilon(.) \) may possess more structure than that of white noise (e.g., Laslett and McBratney, 1990).
In notation as follow,

\[ 2 \gamma_Z(\cdot) = 2 \gamma_W(\cdot) + 2 \gamma_\eta(\cdot) + 2c_{ME}. \]  
\[ (4) \]

The quantities \( c_{ME} \) and \( \gamma_Z(h) \), \( ||h|| \) larger, are pertinent to the observational scale; the other quantities contain information on the spatial scale.

From the decomposition (3), write

\[ Z(s) = S(s) + \varepsilon(s), \quad s \in D, \]  
\[ (5) \]

Where the "signal" or smooth process \( S(\cdot) \) is given by \( S(\cdot) = \mu(\cdot) + W(\cdot) + \eta(\cdot) \). The \( S \) process is often referred to as the noiseless version of the \( Z \) process or, in the engineering literature, as the state process. Also, write

\[ Z(s) = \mu(s) + \delta(s), \quad s \in D, \]  
\[ (6) \]

Where the correlated error process \( \delta(\cdot) \) is given by \( \delta(\cdot) = W(\cdot) + \eta(\cdot) + \varepsilon(\cdot) \). When the Correlation of \( \delta(s) \) white \( \delta(s+h) \) can be written as a function of \( h / \alpha(h) \), where \( 0 < \alpha(h) < \infty \), then \( \alpha(h) \) is sometimes called the spatial correlation scale of the process in direction \( h \) (Cressie, 1993).

### 2.2.1.2 Ordinary kriging

Ordinary Kriging produced better estimates than simple Kriging because of the non-stationarity of the data. The original data set had large areas where the values were low and large areas where the values were high. Simple Kriging requires the mean value of the data set to be provided, whereas ordinary Kriging calculates a mean for each individual block, based on the samples included in estimate. The local mean appears to be more meaningful in a situation where the global mean is not constant (Weber and Englund, 1992).

The word "Kriging" is synonymous with "optimal prediction" (as a noun) or with "optimally predicting" (as the present participle of a verb). In other words, it refers to making inferences on unobserved values of the random process \( Z(\cdot) \) given by (2) or of \( S(\cdot) \) given by (5) from data:

\[ Z \equiv (Z(S_1),...,Z(S_n)) \]  
\[ (7) \]

Observed at known spatial locations \( \{s_1,\ldots,s_n\} \).

Denote the generic predictor of \( g(Z(\cdot)) \) or \( g(S(\cdot)) \) by:

\[ P(Z; g) \]  
\[ (8) \]

Choice of a good predictor will depend on the geometry and location of the region of space where prediction is desired and weather it is the \( Z \) process or the \( S \) process that is to be predicted. When \( g(Z(\cdot)) = Z(B) |= \int_B Z(u)du / ||B|| \) or \( g(S(\cdot)) = S(B) \), write (3.2.3) as \( p(Z; B) \). In the special case of \( B = \{s_0\} \), write (8) as \( p(Z; s_0) \).

**Ordinary Kriging** (Matheron, 1971; Journel and Huijbregts, 1978) refers to spatial prediction under the following two assumptions.

www.intechopen.com
Model Assumption. In (6)

\[ Z(s) = \mu + \delta(s), \quad s \in D, \mu \in \mathbb{R}, \text{ and } \mu \text{ unknown.} \]  

(9)

Predictor Assumption.

\[ p(Z; B) = \sum_{i=1}^{n} \lambda_i Z(s_i), \quad \sum_{i=1}^{n} \lambda_i = 1. \]  

(10)

This latter condition, which the coefficients of the linear predictor sum to 1, guarantees uniform unbiasedness. \( E(p(Z; B)) = \mu = E(Z(B)), \) for all \( \mu \in \mathbb{R}. \)

There is a version of Kriging called simple Kriging, where \( \mu \) in (9) is known and the coefficients are not constrained to sum to 1.

Hence, if

\[ g(Z(.)) = Z(B) = \begin{cases} \int B Z(u) du / |B|, & |B| > 0 \\ \text{ave}\{Z(u) : u \in B\}, & |B| = 0 \end{cases} \]  

(11)

Then the optimal \( p(.; B) \) will minimize the mean-squared prediction error

\[ \sigma^2 = E(Z(B) - p(Z; B))^2 \]  

(12)

Over the class of linear predictors \( \sum_{i=1}^{n} \lambda_i Z(s_i) \) that satisfy \( \sum_{i=1}^{n} \lambda_i = 1 \) (Cressie, 1993).

2.2.1.3 Kriging and calculating the average regional rainfall

In this research, we have used ordinary Kriging for obtaining the average regional rainfall in the area under study. Kriging is the estimation procedure used in geostatistics using known values and a semivariogram to determine unknown values. It was named after D. G. Krige from South Africa. The procedures involved in Kriging incorporate measures of error and uncertainty when determining estimations. Based on the semivariogram used, optimal weights are assigned to unknown values in order to calculate unknown ones. Since the variogram changes with distance, the weights depend on the known sample distribution (Davis 1990).

The final goal of studying spatial changes of rainfall is to simulate the changes in rainfall data in the spatial dimension in order to pave the way for attaining other goals such as forecasting rainfall and getting necessary information for the long-term analysis of rainfall in every region in the area under study. As mentioned before, Kriging method used in this study to calculate the average regional rainfall. The following steps were taken to obtain the time series of average regional rainfall:

1. Making input files for the Arc GIS 9.2 software
2. Obtaining the experimental variogram
3. Analyzing and drawing annual spatial changes of rainfall in the region
4. Obtaining the values of annual average rainfall in the region under study
5. Making time series of rainfall in the region under study.
Fig. 2 for example shows the diagram of the Variogram using spherical model to estimate of the average regional rainfall for the year of 2007.

![Variogram diagram using spherical model to estimate of the average regional rainfall for year of 2007. Units on the horizontal and vertical axes are meter and square millimeter respectively.](image)

### 2.2.2 Determining seasonal rainfall and predictors

The predictors studied in this research are classified into two groups: meteorological parameters at ground level and meteorological parameters at upper levels of the atmosphere. Table 2 shows these parameters.

<table>
<thead>
<tr>
<th>Upper level of atmosphere</th>
<th>Ground level</th>
</tr>
</thead>
<tbody>
<tr>
<td>Air temperature at 700-hPa level</td>
<td>Sea level pressure</td>
</tr>
<tr>
<td>the thickness between 500 and 1000-hPa levels</td>
<td>Sea level pressure difference</td>
</tr>
<tr>
<td>Relative humidity of 300-hPa level</td>
<td>Sea level temperature</td>
</tr>
<tr>
<td>Temperature difference between sea level and 1000-hPa level</td>
<td>Precipitable water</td>
</tr>
<tr>
<td>Zonal wind</td>
<td>Meridional wind</td>
</tr>
</tbody>
</table>

Table 2. Meteorological Parameters used in this study

One distinctive scenario is considered in this study. This scenario uses input data with 6 months lags to investigate the possibility of forecasting more than 3 months in advance.

One of the objectives of this study is the identification of a possible relationship between rainfall in Iran and climatic predictors, using Pearson's correlation coefficient. The other objective is to verify the forecasts produced using the predictors identified with Pearson's correlation coefficient.
Seasonal rainfall and predictors have been determined using the average of the values of a predictor in order to predict the amount of seasonal rainfall. We made sure that the seasons of the predictor do not include months with rainfalls.

Since we aimed to investigate the relation between meteorological parameters and spring rainfall in this study (spring rainfall is very important in dry land cultivation and water resources management), we used the average value of meteorological predictors in the period between October and March as the time series of the predictors and the average rainfall in the period between April and June as the rainfall time series.

To analyze the parameters of the upper levels of the atmosphere as well as three ground parameters, i.e. zonal wind, meridional wind and precipitable water in the present study, we used $5^\circ \times 5^\circ$ and $10^\circ \times 10^\circ$ degrees spatial resolution. The study areas, where meteorological parameters at ground level and upper levels of atmosphere have been factor-analyzed, are located between 0-80 °E and 10-50 °N in $5^\circ \times 5^\circ$ degrees spatial resolution and between 0-100 °E and 0-70 °N in $10^\circ \times 10^\circ$ degrees spatial resolution. The area includes regions where changes in the pattern of temperature, pressure, humidity, and wind speed affect Iranian rainfall (Fig. 3).

For other parameters at ground level including pressure, temperature, pressure difference and temperature difference between sea level and 1000-hPa level, some points has been selected. That is, points were selected and analyzed in different parts of the seas, which were known to affect the climate of Iran from previous studies by other researchers (Nazemosadat & Cordery 2000, Alijani 2006).

We have used factor analysis to analyze the meteorological parameters at upper atmosphere and ground levels (zonal wind, meridional wind and precipitable water). The field of factor analysis involves the study of order and structure in multivariate data. The field includes both theory about the underlying constructs and dynamics which give rise to observed
phenomena, and methodology for attempting to reveal those constructs and dynamics from observed data. Factor analysis is preferable to principal components analysis. Components analysis is only a data reduction method. It became common decades ago when computers were slow and expensive to use; it was a quicker, cheaper alternative to factor analysis (Gorsuch 1997). It is computed without regard to any underlying structure caused by latent variables; components are calculated using all of the variance of the manifest variables, and all of that variance appears in the solution (Ford et al. 1986).

In this statistical method designed to reduce the number of variables, the initial parameters are transformed into independent variables based on their correlation coefficients. These independent variables are called factors. The value of each of the observations in the new factors is calculated as factorial score. Hence, rather than true values of observations, their scores in new components are used as new criteria for clustering. The advantage of this method is that while it reduces the number of variables, it preserves the initial variance of the main data (Alijani 2006).

As mentioned above, to find out the relation between rainfall in the region under study and the changes in meteorological parameters of pressure, temperature, pressure difference and temperature difference, the points in different parts of the seas have been studied, which are supposed to affect the climate of Iran. These include points in the Mediterranean, Persian Gulf, Oman Sea, Aden Gulf, Arab Sea, Red Sea, Black Sea, the Adriatic, Aral Lake, Indian Ocean, The Atlantic, North Sea and Siberia (Fig. 4). Table 3 shows Time series of average regional rainfall (from April to June) and value of predictors.

![Fig. 4. Name and coordinates that have used for relation between rainfall and Remote Linkage Controlling (Fallah Ghalhary et al, 2010)](www.intechopen.com)
Rainfall Prediction Using Teleconnection Patterns
Through the Application of Artificial Neural Networks

<table>
<thead>
<tr>
<th>Year</th>
<th>Rainfall</th>
<th>x1</th>
<th>x2</th>
<th>x3</th>
<th>x4</th>
<th>x5</th>
<th>x6</th>
<th>x7</th>
<th>x8</th>
<th>x9</th>
<th>x10</th>
<th>x11</th>
<th>x12</th>
<th>x13</th>
<th>x14</th>
</tr>
</thead>
<tbody>
<tr>
<td>1970</td>
<td>20.40</td>
<td>-1.15</td>
<td>0.27</td>
<td>0.17</td>
<td>-0.73</td>
<td>-1.65</td>
<td>-0.97</td>
<td>-1.63</td>
<td>-1.23</td>
<td>-1.28</td>
<td>0.20</td>
<td>-6.57</td>
<td>36.53</td>
<td>33.29</td>
<td>31.94</td>
</tr>
<tr>
<td>1971</td>
<td>20.40</td>
<td>-1.15</td>
<td>0.27</td>
<td>0.17</td>
<td>-0.73</td>
<td>-1.65</td>
<td>-0.97</td>
<td>-1.63</td>
<td>-1.23</td>
<td>-1.28</td>
<td>0.20</td>
<td>-6.57</td>
<td>36.53</td>
<td>33.29</td>
<td>31.94</td>
</tr>
<tr>
<td>1972</td>
<td>20.40</td>
<td>-1.15</td>
<td>0.27</td>
<td>0.17</td>
<td>-0.73</td>
<td>-1.65</td>
<td>-0.97</td>
<td>-1.63</td>
<td>-1.23</td>
<td>-1.28</td>
<td>0.20</td>
<td>-6.57</td>
<td>36.53</td>
<td>33.29</td>
<td>31.94</td>
</tr>
<tr>
<td>1973</td>
<td>20.40</td>
<td>-1.15</td>
<td>0.27</td>
<td>0.17</td>
<td>-0.73</td>
<td>-1.65</td>
<td>-0.97</td>
<td>-1.63</td>
<td>-1.23</td>
<td>-1.28</td>
<td>0.20</td>
<td>-6.57</td>
<td>36.53</td>
<td>33.29</td>
<td>31.94</td>
</tr>
</tbody>
</table>

Table 3. Time series of regional monthly average rainfall (from April to June) and value of predictors

2.2.3 Neural information processing systems

Artificial neural networks (ANNs) form a class of systems that is inspired by biological neural networks. They usually consist of a number of simple processing elements, called neurons that are interconnected to each other. In most cases one or more layers of neurons are considered that are connected in a feed forward or recurrent way (Zurada 1992, Grossberg 1988, Lippmann 1987). In trying to understand the emergence of the new discipline of neural networks it is useful to look at some historical milestones in Table 4 (Johan et al. 1997).

2.2.4 Basic neural network architectures

The best known neural network architecture is the multilayer feedforward neural network (multilayer perceptron). It is a static network that consists of a number of layers: input

www.intechopen.com
layer, output layer and one or more hidden layers connected in feedforward way (see e.g. Zurada 1992).

One signal neuron makes the simple operation of a weighted sum of the incoming signals and a bias term (or threshold), fed through an activation function \( \sigma \) and resulting in the output value of the neuron. A network with one hidden layer is described in matrix-vector notation as

\[
y = W \sigma(V^T + \beta),
\]

(13)

Or in elementwise notation:

\[
y_i = \sum_{j=1}^{n_h} \omega_{ij} \sigma \left( \sum_{r=1}^{m} v_{jr} x_r + \beta_j \right), \quad i = 1, \ldots, l.
\]

(14)

Here \( \chi \in \mathbb{R}^m \) is the input and \( y \in \mathbb{R}^l \) the output of the network and the nonlinear operation \( \sigma \) is taken elementwise. The interconnection matrices are \( W \in \mathbb{R}^{l \times n_h} \) for the output layer \( V \in \mathbb{R}^{n_h \times m} \) for the hidden layer, \( \beta \in \mathbb{R}^{n_h} \) is the bias vector (thresholds of hidden neurons) with \( n_h \) the number of hidden neurons.

<table>
<thead>
<tr>
<th>Year</th>
<th>Network</th>
<th>Inventor / Discoverer</th>
</tr>
</thead>
<tbody>
<tr>
<td>1942</td>
<td>McCulloch-Pitts neuron</td>
<td>McCulloch, pitts</td>
</tr>
<tr>
<td>1957</td>
<td>Perceptron</td>
<td>Rosenblatt</td>
</tr>
<tr>
<td>1960</td>
<td>Madaline</td>
<td>Widrow</td>
</tr>
<tr>
<td>1969</td>
<td>Cerebellatron</td>
<td>Albus</td>
</tr>
<tr>
<td>1974</td>
<td>Back propagation network</td>
<td>Werbos, parker, Rumelhart</td>
</tr>
<tr>
<td>1977</td>
<td>Brain state in a box</td>
<td>Anderson</td>
</tr>
<tr>
<td>1978</td>
<td>Neocognitron</td>
<td>Fukushima</td>
</tr>
<tr>
<td>1978</td>
<td>Adaptive Resonance Theory</td>
<td>Carpenter, Grossberg</td>
</tr>
<tr>
<td>1980</td>
<td>Self-organizing map</td>
<td>Kohonen</td>
</tr>
<tr>
<td>1982</td>
<td>Hopfield</td>
<td>Hopfield</td>
</tr>
<tr>
<td>1985</td>
<td>Bidirectional assoc. mem.</td>
<td>Kosko</td>
</tr>
<tr>
<td>1985</td>
<td>Boltzmann machine</td>
<td>Hinton, Sejnowsky</td>
</tr>
<tr>
<td>1986</td>
<td>Counterpropagation</td>
<td>Hecht-Nielsen</td>
</tr>
<tr>
<td>1988</td>
<td>Cellular neural network</td>
<td>Chua, yang</td>
</tr>
</tbody>
</table>

Table 4. The best known artificial neural network architectures together with their year of introduction and their inventor/discoverer. See Hecht Nielsen (1988) for part of this table (Johan et al, 1997).

Fig. 5 shows a multilayer perceptron, which is a static nonlinear network that consists of a dummy input layer, an output layer and two hidden layer. A layer consists of a number of McCulloch-pitts neurons that perform the operation of a weighted sum of incoming signals, fed through a saturation-like nonlinearity. One hidden layer is sufficient in order to be universal approximators for any continues nonlinear function (Johan et al. 1997).
Rainfall Prediction Using Teleconnection Patterns
Through the Application of Artificial Neural Networks

373

Fig. 5. Multilayer perceptron neural network (Johan et al, 1997).

For a network with two hidden layers (see Fig. 5):

\[ y = W \sigma(V_2 \sigma(V_1 x + \beta_1) + \beta_2) \]  
(15)

Or:

\[ y_i = \sum_{s=1}^{n_1} w_{i s} \sigma(\sum_{j=1}^{m} v_{i j}^{(2)} \sigma(\sum_{k=1}^{n_2} v_{kj}^{(1)} x_j + \beta_j^{(1)}) + \beta_j^{(2)}), \quad i = 1, \ldots, l. \]  
(16)

The interconnection matrices are \( W \in \mathbb{R}^{k_1 \times h_2} \) for the output layer, \( V_2 \in \mathbb{R}^{h_2 \times h_2} \) for the second hidden layer and \( V_1 \in \mathbb{R}^{h_1 \times m} \) for the first hidden layer. The bias vectors are \( \beta_2 \in \mathbb{R}^{h_2} \), \( \beta_1 \in \mathbb{R}^{h_1} \) for the second a first hidden layer respectively. In order to describe a network with \( L \) layer (\( L-1 \) hidden layers, because the input layer is a 'dummy' layer), the following notation will be used in the sequel.

\[ x_i^l = \sigma(\xi_i^l), \]  
(17)

\[ \xi_i^l = \sum_{j=1}^{N_l} w_{ij}^l x_j^{l-1} \]  
(18)

Where \( l = 1, \ldots, L \) is the layer index, \( N_l \) denotes the number of neurons in layer \( l \) and \( x_i^l \) is the output of the neurons at layer \( l \). The thresholds are considered here to be part of the interconnection matrix, by defining additional constant inputs.

The choice of the activation function \( \sigma \) may depend on the application area. Typical activation functions are shown in Fig. 6.
Fig. 6. Some possible activation functions for the neurons in the multilayer perceptron (Johan et al., 1997).

Fig. 6 shows some possible activation functions for the neurons in the multilayer precipitation. In this paper, we take the hyperbolic tangent function $\tanh$. Note that this is a static nonlinearity that belongs to the sector $[0, 1]$.

For applications in modeling and control the hyperbolic tangent functions:

$$\tanh(x) = \frac{1 - \exp(-2x)}{1 + \exp(-2x)}$$  \hspace{1cm} (19)

Is normally used. In case of a $\tanh$ the derivative of the activation function is:

$$\sigma' = 1 - \sigma^2$$  \hspace{1cm} (20)

The neurons of the input layer have a linear activation function.

A network that has received a lot of attention recently in the field of neural networks is the radial basic function network. This network can be described as:

$$y = \sum_{i=1}^{n_h} w_i g(\|x - c_i\|)$$  \hspace{1cm} (21)

With $x \in \mathbb{R}^m$ the input vector and $y \in \mathbb{R}$ the output (models with multiple outputs are also possible). The network consists of one hidden layer with $n_h$ hidden neurons. One of the basic differences with the multilayer perceptron is in the use of the activation function. In many cases one takes a Gaussian function for $g$, which is radially symmetric with respect to the input argument. The output layer has output weights $\omega \in \mathbb{R}^{n_h}$. The parameters for the hidden layer are the centers $c_i \in \mathbb{R}^m$ (Johan et al. 1997).

### 2.2.5 Recurrent neural network model

In recurrent neural network, some outputs of the nodes (output nodes or hidden nodes) are fed back to the previous layers. Most commonly used recurrent neural networks are external
recurrent neural networks (Fig.7). In this scheme, the outputs of a neural network are fed back to form a part of its input layer. Another recurrent scheme is internal recurrent neural networks, in which the outputs of hidden nodes (instead of output nodes) are fed back to the input layer (Fig.8) (Aoyama et al, 1999).

Fig. 7. External recurrent neural networks (Aoyama et al, 1999).

Fig. 8. Internal recurrent (state space) neural networks (Aoyama et al, 1999).

After various runs to test the network and the number of neurons of the hidden layer and different activation functions in the hidden and output layers, eventually found out that the final model with its one input layer, one hidden layer and one output layer (average regional rainfall) had the least error so in this research, used it as the main model. The numbers of the neurons in the input, hidden and output layers is fourteen, four and one respectively (14-4-1). The hidden layer activation function is a function of the hyperbolic tangent and the output layer activation function is a function of the linear hyperbolic tangent.

To assess the accuracy of the model, the index of Root Mean Square Error (RMSE) has been used which is calculated by the following formula:
In the above formula, RMSE is Root Mean Square Error, $O_i$ and $e_i$ are the observed and predicted value of the variable respectively in the point i and n is number of network outputs.

3. Results and discussion

3.1 Predicting spring rainfall by means of artificial neural networks

In this study, Pearson Correlation Method has used to obtain meteorological predictors which affect regional rainfall. Thus, all the predictors which have shown a correlation with %5 level of significance in the period between October and March have been used as predictors in the structure of the rainfall forecast model. After numerous checking, it became clear that the optimum effect of predictors is when the period between October and March is used. Therefore, the following predictors in the period between October and March were used as predictors in rainfall forecast models: 1) SST Central Atlantic, 2) SST Western Mediterranean, 3) ∆SST Aral Lake, 4) ∆SST Labrador Sea, 5) SLP Northern Persian Gulf, 6) SLP Oman Sea, 7) SLP Southern Persian Gulf 8) SLP Southern Red Sea, 9) ∆SLP Between Eastern Mediterranean and Oman Sea, 10) air temperature at 700-hPa level in the region of index factor 2 in 5x5 degrees spatial resolution (Fig. 9), 11) air temperature at 700-hPa level in the index region of factor 3 in 5x5 degrees spatial resolution (Fig. 9), 12) precipitable water content in the index region of factor 10 in 10x10 degrees spatial resolution (Fig. 10), 13) relative humidity at 300-hPa level in the region of factor 2 in 5x5 degrees spatial resolution (Fig. 11), 14) relative humidity at 300-hPa level in the region of factor 4 in 5x5 degrees spatial resolution (Fig. 11). The variables which used as predictors in the rainfall forecast models show in the Table 5.

The above model divides the data into three different sections, namely, training data, validation data and testing data. The data belonging to 38 years were in turn divided into 19 years (1970–1988) of training data, 9 years (1989–1997) of validation data and 10 years (1998–2007) of testing data. In the other words, from the whole set of historical data, two-thirds (1970-1997) were considered as calibration data, and one-third (1998 – 2007) as testing data. There is a clear analogy between the neural network weights and the parameters of other modeling approaches, and between the learning set and what we have before calles a period of calibration data. Work in neural networks often does not draw this analogy but it is a useful one in that just as an increase in the number of parameters gives a model more degrees of freedom in calibration but may result in over parameterization with respect to information in the data set, so in a neural network an increase in the number of layers, nodes and interconnections will also result in more degrees of freedom in fitting the learning set, also with the possibility of over parameterization (Beven 2001). Table 6 presents the results of the calibration period of the rainfall forecast model. As is shown, the minimum mean-square error after 1000 learning epochs is 0.169. Also, the maximum mean-square error is 0.169. In the other words, at this stage in the epoch of 1000, the network shows the maximum error. The minimum mean-square error of the validation epoch in the epoch of 3 is 0.234. The results of the prediction model are illustrated in Table 7 and Fig. 12. It is to be
noted that these results were presented for the years 1998 to 2007, which was the testing epoch of the model. The features of this model have been presented in Table 8.

| Symbol (X1) | SST Central Atlantic | Time Oct-Mar | Correlation Coefficient with the average regional rainfall -0.31 | P-value 0.05 |
| Symbol (X2) | SST Western Mediterranean | Time Oct-Mar | Correlation Coefficient with the average regional rainfall -0.38 | P-value 0.01 |
| Symbol (X3) | ΔSST Aral Lake | Time Oct-Mar | Correlation Coefficient with the average regional rainfall -0.35 | P-value 0.03 |
| Symbol (X4) | ΔSST Labrador Sea | Time Oct-Mar | Correlation Coefficient with the average regional rainfall 0.36 | P-value 0.02 |
| Symbol (X5) | SLP Northern Persian Gulf | Time Oct-Mar | Correlation Coefficient with the average regional rainfall 0.31 | P-value 0.05 |
| Symbol (X6) | SLP Oman Sea | Time Oct-Mar | Correlation Coefficient with the average regional rainfall 0.38 | P-value 0.01 |
| Symbol (X7) | SLP Southern Persian Gulf | Time Oct-Mar | Correlation Coefficient with the average regional rainfall 0.31 | P-value 0.05 |
| Symbol (X8) | SLP Southern Red Sea | Time Oct-Mar | Correlation Coefficient with the average regional rainfall 0.34 | P-value 0.03 |
| Symbol (X9) | ΔSLP Between Eastern Mediterranean and Oman Sea air temperature at 700-hPa level in the region of index factor 2 in 5°×5° degrees spatial resolution (Fig. 9) | Time Oct-Mar | Correlation Coefficient with the average regional rainfall -0.32 | P-value 0.04 |
| Symbol (X10) | air temperature at 700-hPa level in the region of index factor 2 in 5°×5° degrees spatial resolution (Fig. 9) | Time Oct-Mar | Correlation Coefficient with the average regional rainfall -0.38 | P-value 0.01 |
| Symbol (X11) | precipitable water in the region of index factor 10 in 10°×10° degrees spatial resolution (Fig. 10) | Time Oct-Mar | Correlation Coefficient with the average regional rainfall -0.45 | P-value 0.004 |
| Symbol (X12) | relative humidity at 300-hPa level in the region of index factor 2 in 5°×5° degrees spatial resolution (Fig. 10) | Time Oct-Mar | Correlation Coefficient with the average regional rainfall -0.31 | P-value 0.05 |
| Symbol (X13) | relative humidity at 300-hPa level in the region of index factor 4 in 5°×5° degrees spatial resolution (Fig. 11) | Time Oct-Mar | Correlation Coefficient with the average regional rainfall 0.45 | P-value 0.004 |
| Symbol (X14) | precipitable water in the region of index factor 10 in 10°×10° degrees spatial resolution (Fig. 10) | Time Oct-Mar | Correlation Coefficient with the average regional rainfall 0.46 | P-value 0.003 |

Table 5. Selected predictor variables which used in the rainfall prediction model

<table>
<thead>
<tr>
<th>Best Networks</th>
<th>Training</th>
<th>Cross Validation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Epoch 1000</td>
<td>1000</td>
<td>3</td>
</tr>
<tr>
<td>Minimum Mean Squared Error</td>
<td>0.169</td>
<td>0.235</td>
</tr>
<tr>
<td>Final Mean Squared Error</td>
<td>0.169</td>
<td>0.426</td>
</tr>
</tbody>
</table>

Table 6. Minimum & Maximum Error in Training and Validation Epochs

As Table 8 shows, the mean square error is 46.5 and the normalized mean square error is 0.55. Also, the mean absolute error for this model was calculated to be 6.15 millimeters. The minimum absolute error is 0.13 millimeter and the maximum absolute error is 10.9 millimeters. Also, the correlation coefficient between observed and predicted rainfall for the model is 0.79. The root mean square error for this model was calculated to be 6.8 millimeters.
Table 7. Rainfall prediction in the region under study by means of neural network model

<table>
<thead>
<tr>
<th>Year</th>
<th>Observed rainfall</th>
<th>Predicted rainfall</th>
</tr>
</thead>
<tbody>
<tr>
<td>1998</td>
<td>32</td>
<td>27</td>
</tr>
<tr>
<td>1999</td>
<td>19</td>
<td>15</td>
</tr>
<tr>
<td>2000</td>
<td>9</td>
<td>15</td>
</tr>
<tr>
<td>2001</td>
<td>7</td>
<td>15</td>
</tr>
<tr>
<td>2002</td>
<td>20</td>
<td>15</td>
</tr>
<tr>
<td>2003</td>
<td>34</td>
<td>24</td>
</tr>
<tr>
<td>2004</td>
<td>28</td>
<td>17</td>
</tr>
<tr>
<td>2005</td>
<td>21</td>
<td>15</td>
</tr>
<tr>
<td>2006</td>
<td>15</td>
<td>15</td>
</tr>
<tr>
<td>2007</td>
<td>10</td>
<td>15</td>
</tr>
</tbody>
</table>

Table 8. The features of artificial neural network model

<table>
<thead>
<tr>
<th>Performance</th>
<th>Y (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mean Squared Error</td>
<td>46.54</td>
</tr>
<tr>
<td>Normalized Mean Squared Error (MSE/variance desired output)</td>
<td>0.55</td>
</tr>
<tr>
<td>Mean Absolute Error</td>
<td>6.15</td>
</tr>
<tr>
<td>Minimum Absolute Error</td>
<td>0.13</td>
</tr>
<tr>
<td>Maximum Absolute Error</td>
<td>10.98</td>
</tr>
<tr>
<td>Linear correlation coefficient</td>
<td>0.79</td>
</tr>
</tbody>
</table>

Fig. 9. The index areas detected by factor analysis at the temperature of 700-hPa level in the period October to March in networks of 5×5 degrees spatial resolution (Fallah Ghalhary et al, 2010)
Rainfall Prediction Using Teleconnection Patterns
Through the Application of Artificial Neural Networks

Fig. 10. The detected areas of precipitable water in the period October to March in networks of 10×10 degrees spatial resolution (Fallah Ghalhary et al, 2010)

Fig. 11. The detected areas of relative humidity at 300-hPa level in networks of 5×5 degrees spatial resolution (Fallah Ghalhary et al, 2010)
The analysis of the results shows that the model is basically incapable of predicting rainfall in dry or wet extreme years. This is due to the fact that these extreme years have not been repeated in the calibration epoch of the prediction model and, for this reason, the model is not able to predict these extreme years. It must be noted that the minimum rainfall in the rainfall time series occurred in 2000 and 2001. To remove this problem, we must train the model with these extreme data. For this reason and in order to enable the neural network model to predict seasonal rainfall in such a way that it can be applied to all cases including dry, wet and normal years, we deleted the years 1998 and 2000 as the two extreme years in the test epoch of the model. One represents the dry extreme year and the other the wet extreme year. These two years were replaced by other data. They were taken out of the testing data and transferred into the training data and calibration epoch of the model. The results of the calibration epoch of the rainfall forecast model have been illustrated in Table 9. It is indicated that the minimum training error in the epoch of 17 is 0.108. The ultimate training error is 0.175. Also, the minimum validation error in the epoch of 1 is 0.087 and the ultimate validation error is 0.399. As the data show the accuracy of the model in detecting all dry, wet and normal years has amazingly increased. We can see that the accuracy of the model is higher than the previous model, as shown in Fig. 13, changes in the type of training data have affected the results of rainfall forecast model and that this model can estimate rainfall with higher accuracy.

<table>
<thead>
<tr>
<th></th>
<th>Training</th>
<th>Cross Validation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Epoch</td>
<td>17</td>
<td>1</td>
</tr>
<tr>
<td>Minimum Mean Squared Error</td>
<td>0.108</td>
<td>0.087</td>
</tr>
<tr>
<td>Final Mean Squared Error</td>
<td>0.175</td>
<td>0.399</td>
</tr>
</tbody>
</table>

Table 9. Minimum and maximum error in training and validation epochs after modifying the network with proper historical data.

The observed and predicted rainfall by the model after modifying the input vector of the model in the training epoch has been presented in Table 10. The accuracy of the model has highly increased in this case and the root mean-square error has reached 2.5 millimeter, which indicates the high efficiency of the model in predicting rainfall in the area under study. The
features of this model have been presented in Table 11. The mean-square error is 6.7 millimeter and the normalized mean-square error is 0.12. Furthermore, the mean absolute error for this model was equal to 2.12 millimeters. The minimum absolute error was 0.03 millimeter and the maximum absolute error was 4.97 millimeters. The correlation coefficient between observed and predicted rainfall was 0.95, which is very reasonable. Fig. 14 shows the observed values of rainfall versus predicted values. The equation of the regression line for the changes in the values of observed versus predicted rainfall is as follows:

\[
\text{Observed Rainfall (mm)} = 0.05 + 0.93 \times \text{Predicted Rainfall}
\]

<table>
<thead>
<tr>
<th>Year</th>
<th>Observed rainfall</th>
<th>Predicted rainfall</th>
</tr>
</thead>
<tbody>
<tr>
<td>1996</td>
<td>21</td>
<td>22</td>
</tr>
<tr>
<td>1997</td>
<td>25</td>
<td>27</td>
</tr>
<tr>
<td>1998</td>
<td>32</td>
<td>35</td>
</tr>
<tr>
<td>1999</td>
<td>19</td>
<td>18</td>
</tr>
<tr>
<td>2001</td>
<td>7</td>
<td>7.7</td>
</tr>
<tr>
<td>2002</td>
<td>20</td>
<td>22</td>
</tr>
<tr>
<td>2004</td>
<td>28</td>
<td>25</td>
</tr>
<tr>
<td>2005</td>
<td>21</td>
<td>26</td>
</tr>
<tr>
<td>2006</td>
<td>15</td>
<td>15</td>
</tr>
<tr>
<td>2007</td>
<td>10</td>
<td>14</td>
</tr>
</tbody>
</table>

Table 10. Rainfall forecast in the region under study after modifying the network with historical data

The observations of the linear regression between observed values of rainfall and predicted values and the results of the variance analysis of the linear regression between the observed values of rainfall and predicted values have been summarized in Table 12 and Table 13 respectively. As we can see in Table 12, considering the confidence range of %99 of the linear regression between the observed values of rainfall and predicted values, the root mean-square error was calculated to be 2.46 millimeters. Table 13 shows that the F ratio is significant at %1 level, which is indicative of a strong relation between the changes in the
observed values of rainfall versus predicted values. The significance test of the gradient of the regression line between the true values of rainfall and the values predicted by the model has also been done (Table 14). As observed here, the gradient of the regression line is also significant at %1 level. The P-value for the significance test of the gradient of the regression equation was smaller than 0.0001.

<table>
<thead>
<tr>
<th>Performance</th>
<th>Y (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mean Squared Error</td>
<td>6.73</td>
</tr>
<tr>
<td>Normalized Mean Squared Error (MSE/</td>
<td>0.12</td>
</tr>
<tr>
<td>variance desired output)</td>
<td></td>
</tr>
<tr>
<td>Mean Absolute Error</td>
<td>2.12</td>
</tr>
<tr>
<td>Minimum Absolute Error</td>
<td>0.03</td>
</tr>
<tr>
<td>Maximum Absolute Error</td>
<td>4.97</td>
</tr>
<tr>
<td>Linear correlation coefficient</td>
<td>0.95</td>
</tr>
</tbody>
</table>

Table 11. Features of artificial neural network after modifying the network with historical data

<table>
<thead>
<tr>
<th>Variable</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>RSquare</td>
<td>0.908079</td>
</tr>
<tr>
<td>RSquare Adj</td>
<td>0.896589</td>
</tr>
<tr>
<td>Root Mean Square Error</td>
<td>2.466808</td>
</tr>
<tr>
<td>Mean of Response</td>
<td>19.8</td>
</tr>
<tr>
<td>Observations (or Sum Wgts)</td>
<td>10</td>
</tr>
</tbody>
</table>

Table 12. Summary of the observations of the linear regression between the true values of rainfall and predicted values

<table>
<thead>
<tr>
<th>Source</th>
<th>DF</th>
<th>Sum of Squares</th>
<th>Mean Square</th>
<th>F Ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model</td>
<td>1</td>
<td>480.91887</td>
<td>480.919</td>
<td>79.0317</td>
</tr>
<tr>
<td>Error</td>
<td>8</td>
<td>48.68113</td>
<td>6.085</td>
<td>.0001</td>
</tr>
<tr>
<td>C. Total</td>
<td>9</td>
<td>529.60000</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 13. The variance analysis of the linear regression between the true values of rainfall and predicted values

| Term                    | Estimate  | Std Error | t Ratio | Prob>| t | |
|-------------------------|-----------|-----------|---------|--------|
| Intercept               | -0.075552 | 2.367907  | -0.03   | 0.9753 |
| Predicted rainfall (mm) | 0.9388546 | 0.105608  | 8.89    | <.0001 |

Table 14. Summary of the statistical observations of the estimation of the parameters of the model

<table>
<thead>
<tr>
<th>Model</th>
<th>RMSE</th>
<th>Maximum Absolute Error</th>
<th>Minimum Absolute Error</th>
</tr>
</thead>
<tbody>
<tr>
<td>ANN Model</td>
<td>6.82</td>
<td>10.98</td>
<td>0.13</td>
</tr>
<tr>
<td>Modified ANN Model</td>
<td>2.5</td>
<td>4.97</td>
<td>0.03</td>
</tr>
</tbody>
</table>

Table 15. Statistical comparative of two models
Rainfall Prediction Using Teleconnection Patterns
Through the Application of Artificial Neural Networks

Fig. 14. Changes in the true values of rainfall versus predicted values. The slanted line is the regression line.

Fig. 15. The confidence range of %99 for changes of the observed rainfall versus predicted values.

The confidence range of %99 for the changes of the observed rainfall versus the predicted values has been illustrated (Fig. 15). Here again, the changes of the observed rainfall and the predicted rainfall shows a close correspondence, being significant at 0.01 level. Fig. 16 Displays the changes in the values of residuals versus predicted values of rainfall. Here again, the changes in the values of residuals versus predicted values of rainfall are completely accidental and normal, indicating the high accuracy of the model in predicting rainfall. In sum, the analysis of the results indicates that the difference between the observed and predicted rainfall is within a reasonable range; moreover, the model has been able to predict rainfall in all years with an acceptable error. The root mean-square error for this model was 2.5 millimeter, which is very small, indicating the accuracy of the model in predicting rainfall. We can conclude from
the above discussion that the variables used in the model have been able to detect the distribution pattern of rainfall in the region with great ease and accuracy. We can also decide that the model can be successfully used for predicting rainfall in spring.

Fig. 16. Changes of the values of residuals versus predicted values of rainfall in terms of millimeter

4. Conclusion

Based on the obtained results, we can conclude that ANN models were successful in the prediction of spring rainfall, but the ANN model has higher accuracy after the revision of training data with a root mean square error of 2.5 milliliters. This is clearly observable in Fig.13, ANN model after the revision of training data has been more successful than the before. Table 15 shows the results of two ANN models to predicting the amount of the rainfall in the area under study. At the end, we can result that the variables entering rainfall prediction models have been well able to detect the rainfall distribution patterns in the region and can be used in rainfall prediction patterns in the region. This plays a vital role in the management and planning of drink and agriculture water resources. Considering these predictions, we can plan future policies for optimizing the costs and possibilities for maximum efficiency.

5. Acknowledgement

This paper presents part of the findings of the research project “Predicting spring rainfall in Khorasan Razavi Province based on meteorological predictors by means of fuzzy logic, artificial neural networks and adaptive neuron-fuzzy networks” by the same author. The author greatly appreciates the cooperation of the directors and managers of the “Climatological Research Institute” who provided the possibilities required for the completion of this project.

6. References

Rainfall Prediction Using Teleconnection Patterns
Through the Application of Artificial Neural Networks


www.intechopen.com

www.intechopen.com
Climatology, the study of climate, is no longer regarded as a single discipline that treats climate as something that fluctuates only within the unchanging boundaries described by historical statistics. The field has recognized that climate is something that changes continually under the influence of physical and biological forces and so, cannot be understood in isolation but rather, is one that includes diverse scientific disciplines that play their role in understanding a highly complex coupled "whole system" that is the earth's climate. The modern era of climatology is echoed in this book. On the one hand it offers a broad synoptic perspective but also considers the regional standpoint, as it is this that affects what people need from climatology. Aspects on the topic of climate change - what is often considered a contradiction in terms - is also addressed. It is all too evident these days that what recent work in climatology has revealed carries profound implications for economic and social policy; it is with these in mind that the final chapters consider acumen as to the application of what has been learned to date.

How to reference
In order to correctly reference this scholarly work, feel free to copy and paste the following:
