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Growth and Characterization of Single Crystals of Potassium Sodium Niobate by Solid State Crystal Growth

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1. Introduction

Due to the toxic nature of PbO in Pb(Zr,Ti)O3 (PZT), the most common type of piezoceramic, many studies on lead-free materials are being conducted worldwide (Röedel et al., 2009). One of the most studied groups of lead-free ferroelectric materials is based on a solid solution of potassium sodium niobate, K0.5Na0.5NbO3 (KNN) (Jaffe et al., 1971; Kosec et al., 2008). However, activity in attempts to find a lead-free replacement for PZT really accelerated with the discovery of textured (K,Na,Li)(Nb,Ta,Sb)O3 ceramics, with properties comparable to those of PZT (d33 > 300 pC/N, relative permittivity > 1500, planar coupling coefficient k33 > 60%) (Saito et al., 2004).

One way to enhance the piezoelectric properties of KNN is to grow KNN-based single crystals along certain crystallographic directions, as has been demonstrated for the case of KNbO3 (Wada et al., 2004) and relaxor-based ferroelectric single crystals (Park & Shrout, 1997). The most frequently used methods for growing alkali niobate based single crystals are top seeded solution growth and the flux methods (Chen et al., 2007; Davis et al., 2007; Kizaki et al., 2007; Lin et al., 2009). However, these methods are not yet fully commercialized due to high costs and poor reproducibility related to compositional inhomogeneity within the crystals. A possible way to improve the homogeneity of crystals with complex composition is to grow them by the low cost Solid State Single Crystal Growth (SSCG) method.

The SSCG method is essentially a form of induced abnormal grain growth, a phenomenon which is very well known in the solid state sintering community. A significant breakthrough in the solid state synthesis of lead-free materials has been achieved in recent years (Kosec et al., 2010; Malič et al., 2008a). However, due to the strongly hygroscopic nature of alkaline carbonates usually used in solid state synthesis, different diffusion rates of involved ionic species during annealing, and the high sublimation rates of the alkaline species at high temperatures (Bomlai et al., 2007; Jenko et al., 2005; Kosec & Kolar, 1975; Malič et al., 2008b), it may be rather difficult to obtain compositionally homogeneous alkali niobate-based single crystals by SSCG.
The chemical homogeneity and porosity, as well as crystal and domain structure of such single crystals strongly affect their ferroelectric behaviour. They depend on many parameters such as the initial growth setup used for SSCG, i.e. the choice of the seed and the presence of a liquid sintering aid, and further growth conditions, such as annealing rate, temperature, pressure etc. In order to be able to understand the composition-property relationship of single crystals their structure and chemical composition has to be accurately determined. This can be achieved using different complementary analytical methods such as optical, scanning and transmission electron microscopes, X-ray diffraction analysis, etc.

The aim of the following chapter is firstly to present basic principles of the SSCG technique and its application to the growth of $K_{0.5}Na_{0.5}NbO_3$ (KNN) and Li,Ta-modified KNN single crystals. Secondly, the use of complementary analytical characterization techniques for obtaining the precise compositional and structural data from the produced crystals and its correlation with the electrical properties will be discussed.

### 2. Principles of the solid-state crystal growth technique

The SSCG method is a way of growing single crystals from a polycrystalline starting material. In this method, a single crystal (called a seed crystal) is embedded in ceramic powder of the desired crystal composition and pressed. The sample is then sintered and a single crystal with the composition of the ceramic powder grows using the seed crystal as a template (Fig.1). Alternatively, a seed crystal is placed on top of a pre-sintered ceramic sample and annealed (both the faces of the seed crystal and the ceramic that are in contact must be polished). A single crystal then grows downward from the seed crystal into the ceramic.

![Fig. 1. Schematic of Solid-State Single Crystal Growth](https://www.intechopen.com)
The SSCG method was first used to grow single crystals of BaTiO$_3$ (DeVries, 1964) and has since been used to grow single crystals of manganese zinc ferrite (Kugimiya et al., 1990), Pb(Mg$_{1/3}$Nb$_{2/3}$)O$_3$–PbTiO$_3$ (Khan et al., 1999), Pb(Mg$_{1/3}$Nb$_{2/3}$)O$_3$–PbZrO$_3$–PbTiO$_3$ (Zhang et al., 2007), Ba(Ti,Zr)O$_3$ (Rehrig et al., 1999) and BaTiO$_3$ (Yamamoto & Sakuma, 1994). The piezoelectric properties of single crystals grown by the SSCG method are comparable to those of crystals grown by flux-based methods (Lee, 2003).

The SSCG method has several advantages over more traditional flux or melt-based methods of single crystal growth (Lee, 2003). Conventional ceramic processing equipment can be used, avoiding the need for expensive crystal-growing apparatus. The SSCG method is particularly suited to growing single crystals which melt incongruently or which have volatile components. Because the SSCG method does not involve melting and re-solidification of the ceramic powder, problems such as compositional variations in crystals can be avoided. Furthermore, since SSGC is an isothermal crystal growth method, problems of temperature-gradient induced stresses in the crystal are avoided.

However, the SSCG method also has some disadvantages. If pores exist or form in the substrate, they can be included in the growing single crystal (DeVries, 1964; Kim et al., 2006). Once pores are trapped within the crystal they are very difficult to remove, as gases trapped in the pore have to diffuse through the crystal lattice (Choi et al., 2001). Also, if abnormal grain growth takes place in the substrate, these large grains will pin the single crystal boundary, preventing further growth (Kim et al., 2006). So control of the substrate microstructure is vital if good quality single crystals are to be obtained.

The SSCG method utilizes the phenomenon of abnormal grain growth. Abnormal grain growth also frequently occurs in the ceramic matrix/substrate during the sintering/annealing stage. In order to understand and control SSCG, the principles behind abnormal grain growth in ceramics must first be discussed. When a polycrystalline ceramic undergoes abnormal grain growth, a small number of grains (abnormal grains) grow much more rapidly than the other grains (matrix grains). A bimodal microstructure develops, consisting of fine micron-sized matrix grains and a few large abnormal grains, which can be hundreds of microns in diameter. Sometimes, all of the matrix grains are consumed by the abnormal grains, resulting in a coarse microstructure. Examples of systems which display abnormal grain growth include BaTiO$_3$ (Hennings et al., 1987) and Pb(Mg$_{1/3}$Nb$_{2/3}$)O$_3$–PbTiO$_3$ (Seo & Yoon, 2005).

In a polycrystalline ceramic that is being sintered or annealed, each grain will have its own growth rate $R$, given by the equation (Chiang et al., 1997):

$$R = 2M_b\Delta\mu \tag{1}$$

where $M_b$ is the interface mobility and $\Delta\mu$ is the driving force for grain growth. The driving force for grain growth of a grain (assuming liquid-phase sintering) is given by (Yoon et al., 2001):

$$\Delta\mu = 2\gamma_{sl}\Omega \left(\frac{1}{r} - \frac{1}{r^\star}\right) \tag{2}$$

where $\gamma_{sl}$ is the solid / liquid interfacial energy, $\Omega$ the molar volume of the solid phase, $r$ the grain radius and $r^\star$ the radius of a critical grain that neither grows nor shrinks. This is usually considered to be the mean grain radius. For solid-state sintering, $\gamma_{sl}$ is replaced with the average grain boundary energy $\gamma_{gb}$.
Whether a ceramic undergoes abnormal grain growth or not depends upon its interface structure. Interfaces (both grain boundaries and solid/liquid interfaces) can be either rough (disordered) or faceted (ordered) at an atomic level (Hirth & Pound, 1963). If the interfaces are rough, then atom attachment can take place at any point on the growing grain and grain growth is controlled by diffusion of atoms through the liquid phase or across the grain boundary between the shrinking and growing grain. If the interfaces are faceted then attachment of atoms to a grain is energetically unfavourable because a number of broken bonds are formed. After atoms adsorb on the grain surface, they will quickly desorb again unless they can migrate and attach to a low energy site such as the edge of a 2D nucleus. Such a grain can therefore grow by the formation and spread of 2D nuclei on the grain surface. Alternately, if a defect such as a screw dislocation or twin is present, then this can also act as a site for grain growth.

Fig. 2 shows the variation of the grain growth rate with driving force for rough and faceted interfaces (Hirth & Pound, 1963). For rough solid/liquid interfaces, interface mobility \( M_b \) is constant with \( \Delta \mu \) and the growth rate is given by (Greenwood, 1956):

\[
\dot{R} = \frac{D C_0 \Omega \Delta \mu}{2kT} \quad (3)
\]

where \( D \) is the diffusivity of the solid through the liquid phase, \( C_0 \) the equilibrium solubility and \( T \) the temperature. The growth rate is linearly proportional to the driving force. Grains larger than the mean radius will grow, whilst smaller grains will shrink. For a system with rough solid/liquid interfaces, abnormal grain growth does not occur (Kwon et al., 2000; Lee et al., 2000).

For faceted interfaces, \( M_b \) is not constant with \( \Delta \mu \). For grain growth caused by 2D nucleation, the growth rate is described by the following equation (van der Eerden, 1993):

\[
\dot{R} = v_{st} \exp \left( \frac{-n \Omega^2}{6h\Delta \mu kT} \right) \quad (4)
\]

where \( v_{st} \), \( \epsilon \), and \( h \) are the step velocity of the growing nucleus, edge free energy of the nucleus and step height of the nucleus respectively. For low driving forces, the rate at which stable 2D nuclei form is very low. Hence atoms cannot easily attach to the grain and the growth rate is very slow. Above a critical driving force \( \Delta \mu_C \), the rate at which stable 2D nuclei form increases exponentially (Hirth & Pound, 1963). Atoms can then easily attach to the grain and grain growth can take place. The grain growth rate therefore varies exponentially with \( \Delta \mu \). For \( \Delta \mu > \Delta \mu_C \), kinetic roughening takes place: the number of 2D nuclei available for atom attachment on a grain is so large that atoms can easily attach at any point and grain growth is effectively diffusion controlled, as in the case of a rough interface (Kang, 2005). For a system with faceted interfaces, abnormal grain growth can occur. Most of the grains will have \( \Delta \mu < \Delta \mu_C \) and will grow very slowly, but a few grains will have \( \Delta \mu \geq \Delta \mu_C \) and can grow rapidly to form abnormal grains. This leads to a bimodal microstructure, with large abnormal grains in a matrix of fine grains.

For faceted interfaces, screw dislocations can act as sites for atom attachment and grain growth (Bauser & Strunk, 1982). The growth rate for an interface containing screw dislocations is described by the Burton-Cabrera-Frank theory (Burton et al., 1951). For a
crystal face with a growth spiral, the growth rate increases parabolically with \( \Delta \mu \) for 
\( \Delta \mu < \Delta \mu_c \), and linearly for \( \Delta \mu > \Delta \mu_c \) (Bennema, 1993).

![Diagram](image)

Fig. 2. Variation of growth rate with driving force for rough and faceted interfaces

In the SSCG method, the seed crystal acts as a large grain which can grow abnormally to
form a single crystal. Grains in the matrix that are large enough can also undergo abnormal
grain growth. For the SSCG method to work, the grains must have faceted interfaces. The
seed crystal should have the same crystallographic structure as the desired single crystal,
and should have similar unit cell parameters so that epitaxial growth can take place on the
seed. In addition, the seed crystal should not react chemically with the matrix material or
sintering aid.

3. Characterization methods

Most of the methods that are applicable to the compositional and chemical characterization
of bulk ceramics can be employed for the single crystals. One of the most commonly
employed methods for exploring ceramic structure is X-ray diffraction (XRD) analysis.
Besides crystal structure related analysis, the XRD data gives the information about the bulk
phase composition. However, fractions of minor phases below \( \sim 3 \) to \( \sim 1 \) vol\%, depending on
the XRD configuration, cannot be detected. In case of single crystals, a dedicated XRD setup
can be used, if the size of the investigated crystal exceeds 2 mm (Arndt & Willis, 1966).
The microstructure of the material can be explored by the different methods of microscopy,
depending on the size of the investigated feature. The optical microscope can be employed
for studying larger features and for a general overview of the material. With its specific
applications, such as polarization microscopy, the domain structure of the ferroelectric
material can be studied with a resolution up to 0.5 \( \mu \)m. Further exploration of the material’s
microstructure is generally conveyed with a scanning electron microscope (SEM) and a
transmission electron microscope (TEM). Here, the local microstructure can be studied at
micro- and nano-scales by means of both imaging and electron diffraction. The utilization of
the electron back-scattered diffraction (EBSD) technique in SEM allows probing of the
Ferroelectric domain structure at the microscale, while the selected area electron diffraction (SAED) patterns obtained in the TEM can be used for studying the nanosized domains. As well as facilitating the visualization of the microstructure, the electron microscopy techniques make it possible to gain the compositional information from the localized area of the bulk sample. For the bulk material, the complete quantitative elemental composition can be obtained with Inductively Coupled Plasma (ICP) analysis with ppm precision. With energy dispersive X-ray spectroscopy (EDXS) and wavelength dispersive X-ray spectroscopy (WDXS) in SEM it is possible to gain compositional information with micrometer-scale resolution and with typical detection limits of $\approx 0.1\text{wt}\%$ and $\approx 0.01\text{ wt.}\%$, respectively (Goldstein et al., 2003). Further improvement of spatial resolution in the compositional analysis can be achieved with TEM-EDXS. Although the detection limits of TEM-EDXS are the same as those in SEM-EDXS, the analyses can be performed with the spatial resolution in the nm range.

It is important to mention that due to the presence of the volatile compounds in alkali based single crystals, the data acquisition and the interpretation of the EDXS analysis have to be performed with caution. Issues such as the spatial resolution, beam-specimen interactions and the use of proper standards should be taken into account to obtain the true chemical composition of KNN single crystals (Benčan et al., 2011). For example, Samardžija et al. (Samardžija et al., 2004) showed that the standardless quantitative EDXS analysis of polycrystalline KNN gave erroneous compositions for the KNN solid solution. Another point which was made by the authors was concerning the proper choice of analytical standards. Glasses containing Na and/or K or natural minerals with Na and/or K (albite, orthoclase) which are usually used as standards in virtual standard packages for standardless SEM-EDXS methods are not reliable enough due to the appearance of compositional variations and the well known beam-induced alkali migration within a single specimen. Additionally, the alkali content in these minerals is rather low, which affects the precision of the analysis. Instead, the use of reliable, homogeneous and stable standard materials such as single crystals of KNbO$_3$ and NaNbO$_3$ is proposed.

4. Growth of $(K_{0.5}Na_{0.5})$NbO$_3$ single crystals by SSCG.

As was already discussed in Section 2, seed crystals and ceramic powder precursors are needed to grow KNN single crystals by SSCG. For the KNN system, KTaO$_3$ was found to be a suitable material for seed crystals due to the similarity in unit cell parameter between KTaO$_3$ ($a=3.9883\text{Å}$) (ICSD #39673) and $K_{0.5}Na_{0.5}$NbO$_3$ ($a=4.0046\text{Å}$, $b=3.9446\text{Å}$, $c=4.0020\text{Å}$, and $\beta=90.3327^\circ$) (Tellier et al., 2009). Also, KTaO$_3$ does not undergo any phase transitions during cooling which could produce stresses and cracking in the single crystal. For the growth of KNN single crystals, KTaO$_3$ single crystal seeds (FEE GmbH, Germany) oriented in the $<001>$ and $<110>$ directions were used. The precursor powder with a composition of $(K_{0.5}Na_{0.5})$NbO$_3$ was prepared by attrition milling K$_2$CO$_3$ (Aldrich, 99+%), Na$_2$CO$_3$ (Riedel-de Haën, 99.8%) and Nb$_2$O$_5$ (H. C. Starck, 99.8%) in acetone with ZrO$_2$ media, followed by calcination at 700°C for 4 hours. The ceramic powder should have a fine mean particle size and should also have a narrow particle size distribution. The growth rate of the single crystal is inversely proportional to the mean matrix grain size of the ceramic, so a ceramic with a small mean matrix grain size is preferable (Equation 2). To make a precursor ceramic with a small mean matrix grain size, a fine starting powder is necessary. Also, if the starting powder has a wide particle size distribution, the larger particles can grow rapidly to form abnormal grains during sintering.
of the ceramic. These abnormal grains will then slow down or even block single crystal growth (Kim et al., 2006). It may be necessary to add a liquid phase sintering aid to the powder. For the PMN-PT system, addition of PbO as a liquid phase sintering aid increases the growth rate of the single crystal (Gorzkowski et al., 2006). In the experiments described below, K$_4$CuNb$_8$O$_{23}$ was used as a liquid phase sintering aid (Matsubara et al., 2005). To make K$_4$CuNb$_8$O$_{23}$, K$_2$CO$_3$, CuO (Alfa Aesar, 99.7%) and Nb$_2$O$_5$ were attrition milled and calcined at 700°C for 4 hours. The effect of K$_4$CuNb$_8$O$_{23}$ on single crystal growth of (K$_{0.5}$Na$_{0.5}$)NbO$_3$ will be discussed in a later Section 4.3.

4.1 Growth of (K$_{0.5}$Na$_{0.5}$)NbO$_3$ single crystals at atmospheric pressure

KTaO$_3$ seed crystals with the dimensions of 2 mm × 2 mm × 0.5 mm were buried in 1.2 g of powder and uniaxially pressed at 100 MPa, followed by cold isostatic pressing at 200 MPa. Samples were sintered in air at 1100°C for 10 h, with heating and cooling rates of 2°C.min$^{-1}$. A scanning electron microscopy (SEM) micrograph of a vertically-sectioned, polished and thermally etched sample is shown in Fig. 3 (Fisher et al., 2007a). The inset shows the boundary between the single crystal and the matrix. A single-crystal ~160µm thick has grown on the seed crystal. Both the single crystal and the polycrystalline matrix contain large numbers of pores.

Quantitative SEM-EDXS analysis was carried out using single crystals of KNbO$_3$ and NaNbO$_3$ as standards (Samardžija et al., 2004). Analysis shows that both the single crystal and the matrix grains have the composition (K$_{0.5}$Na$_{0.5}$)NbO$_3$ within the limits of experimental error. Furthermore, the EDXS results show that Ta has not migrated from the seed crystal to the single crystal. High resolution Transmission Electron Microscopy (HRTEM) of the seed/single crystal interface shows that the single crystal grew epitaxially on the seed crystal, as shown by the selected area diffraction pattern of the interface in the inset (Fig. 4).

Fig. 3. SEM micrograph of a Single Crystal of (K$_{0.5}$Na$_{0.5}$)NbO$_3$ grown by SSCG (Fisher et al., 2007a)
4.2 Growth of \((\text{K}_{0.5}\text{Na}_{0.5})\text{NbO}_3\) single crystals in a hot press

As can be seen in Fig. 3, single crystals of \((\text{K}_{0.5}\text{Na}_{0.5})\text{NbO}_3\) grown by the SSCG method are very porous. To solve this problem, single crystals were grown in a hot press (Fisher et al., 2008a). In these experiments, \(<110>\)-oriented \(\text{KTaO}_3\) seed crystals were used. The sample was pre-densified in the hot press at a temperature of 975°C and a pressure of 50 MPa for 2 h, and then annealed at a temperature of 1100°C and a pressure of 50 MPa for 100 h. In Fig. 5a, the optical micrograph of the resulting single crystal is shown. Compared to a single crystal grown in a conventional box furnace under atmospheric pressure (Fig. 5b), hot pressing made it possible to produce a much denser crystal.
During growth of the single crystal in the conventional furnace, single crystal growth, matrix grain growth and matrix densification take place simultaneously. During crystal growth, pores in the matrix can be picked up by the moving single crystal/matrix interface. If the pores then separate from the interface, they will become trapped in the single crystal. The size of the trapped pores increases with crystal growth distance. This is probably due to pore coalescence in the matrix before the crystal/matrix interface reaches them. Application of an external pressure during crystal growth has two benefits. Firstly, during the first stage (975°C/50 MPa for 2 h), the polycrystalline matrix is densified. Application of an external pressure promotes densification without promoting grain growth (Chiang et al., 1997). The sintering temperature can therefore be reduced, allowing the matrix to be densified without much grain growth or single crystal growth. Growing the single crystal in an already dense matrix increases the density of the crystal (Fisher et al., 2007a). Secondly, during the second stage (1100°C/50 MPa for 100 h), the K₄CuNb₈O₂₃ liquid phase sintering aid melts and penetrates the grain boundaries, leaving behind pores which must be eliminated. The applied pressure increases the driving force for shrinkage of these pores within the matrix and also of pores that become trapped within the crystal (Kang and Yoon, 1989).

4.3 Effect of sintering aid on crystal growth and composition

The effect of the amount of sintering aid on single crystal growth, matrix grain growth and single crystal composition was investigated (Fisher et al., 2008b). Single crystals were grown from \((K_{0.5}Na_{0.5})\)NbO₃ powders with additions of 0, 0.5 and 2 mol % K₄CuNb₈O₂₃, using <001>-oriented KTaO₃ seed crystals. Before the crystal growth experiments, samples were pre-densified by hot-pressing at 975°C / 50 MPa for 2 h. Crystals were then grown in air under atmospheric pressure at 1100°C for 1-20 h.

![Fig. 6. Single crystals grown from \((K_{0.5}Na_{0.5})\)NbO₃ powders with additions of (a) 0, (b) 0.5 and (c) 2 mol % K₄CuNb₈O₂₃. Crystals were grown at 1100°C for 10 h. (d) Backscattered electron image of crystal shown in Fig.6 (c) (Fisher et al., 2008b) www.intechopen.com](image-url)
Secondary electron SEM images of crystals which had been grown at 1100°C for 10 h are shown in Fig. 6 (a) – (c). In the sample with 0 mol % \( K_4CuNb_8O_{23} \) the crystal/matrix interface is very irregular. Addition of 0.5 mol % \( K_4CuNb_8O_{23} \) causes the interface to become regular but reduces the single crystal growth distance. Addition of 2 mol % \( K_4CuNb_8O_{23} \) causes the crystal growth distance to increase again. Fig. 6 (d) is a backscattered electron image of the sample with 2 mol % \( K_4CuNb_8O_{23} \). It can be seen that there is a second phase trapped within the crystal. EDXS analysis revealed this phase to be the \( K_4CuNb_8O_{23} \) sintering aid. This phase was not present within the crystals grown from samples with 0.5 mol % \( K_4CuNb_8O_{23} \).

Fig. 7 shows the growth distance of the single crystals and mean matrix grain sizes vs. growth time. For the samples with 0 and 0.5 mol % \( K_4CuNb_8O_{23} \), crystal growth is initially rapid but tails off with growth time (Fig. 7a). Addition of 0.5 mol % \( K_4CuNb_8O_{23} \) causes a reduction in single crystal growth distance at all annealing times. For the sample with 2 mol % \( K_4CuNb_8O_{23} \), the crystal growth rate decreases after 1 hour and then remains approximately constant up to 20 h. For the samples with 0 and 0.5 mol % \( K_4CuNb_8O_{23} \), matrix grain growth is initially rapid but then tails off with annealing time (Fig. 7b). For the samples with 2 mol % \( K_4CuNb_8O_{23} \), after initial growth for 1 h, the matrix grain size remains almost constant up to 20 h.

\[
\Delta \mu = 2Y_p\Omega \left( \frac{1}{r} \right)
\]

This behaviour is explained by considering the effect of the liquid phase on both single crystal growth and matrix grain growth. Because the seed crystal acts as a very large grain, for the single crystal equation [2] can be approximated to:

\[
\Delta \mu = 2Y_p\Omega \left( \frac{1}{r} \right)
\]  

Therefore, the single crystal growth rate is inversely proportional to the mean matrix grain size. In the samples with 0 and 0.5 mol % \( K_4CuNb_8O_{23} \), matrix grain growth causes the driving force for single crystal growth to decrease with annealing time and the single crystal
growth rate to slow down. Addition of 0.5 mol % $K_4CuNb_8O_{23}$ liquid phase sintering aid can further reduce both the crystal and matrix grain growth rates, as the thickness of the solid/liquid interface across which atoms must diffuse increases (Kang, 2005). With addition of 2 mol % $K_4CuNb_8O_{23}$, matrix grain growth effectively ceases after 1 h. This means that the driving for single crystal growth remains constant after 1 h, allowing the crystal to keep growing even for extended annealing times.

Table 1 gives EDXS analyses of single crystals and matrix grains of samples with different amounts of $K_4CuNb_8O_{23}$. Again, single crystals of KNbO$_3$ and NaNbO$_3$ were used as standards. For the samples with 0 and 0.5 mol % $K_4CuNb_8O_{23}$, both the single crystal and matrix grains have compositions close to the nominal composition. For the sample with 2 mol % $K_4CuNb_8O_{23}$, the matrix grains have the nominal composition but the single crystal is Na-rich. According to the KNbO$_3$-NaNbO$_3$ phase diagram, $(K_{0.5}Na_{0.5})NbO_3$ at 1100°C lies just below the solidus line (Jaffe et al., 1971). It is possible that addition of 2 mol % $K_4CuNb_8O_{23}$ lowered the solidus temperature to below 1100°C. This would then cause the equilibrium solid phase to be Na-rich. Indeed, the growing single crystal is Na-rich. The matrix grains retain their original composition as their growth rate is very slow. Therefore, care must be taken when adding a liquid phase sintering aid to promote single crystal growth in this system.

<table>
<thead>
<tr>
<th>Amount of $K_4CuNb_8O_{23}$ (mol %)</th>
<th>K (at. %)</th>
<th>Na (at. %)</th>
<th>K/Na ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>0 (single crystal)</td>
<td>10.34 ± 0.58</td>
<td>10.82 ± 0.64</td>
<td>0.96 ± 0.04</td>
</tr>
<tr>
<td>0 (matrix)</td>
<td>10.64 ± 0.62</td>
<td>10.53 ± 0.58</td>
<td>1.01 ± 0.05</td>
</tr>
<tr>
<td>0.5 (single crystal)</td>
<td>10.41 ± 0.44</td>
<td>10.39 ± 0.41</td>
<td>0.99 ± 0.05</td>
</tr>
<tr>
<td>0.5 (matrix)</td>
<td>10.48 ± 0.63</td>
<td>10.42 ± 0.96</td>
<td>1.02 ± 0.13</td>
</tr>
<tr>
<td>2 (single crystal)</td>
<td>8.46 ± 0.54</td>
<td>13.35 ± 0.65</td>
<td>0.64 ± 0.06</td>
</tr>
<tr>
<td>2 (matrix)</td>
<td>10.58 ± 0.32</td>
<td>10.79 ± 0.99</td>
<td>0.99 ± 0.10</td>
</tr>
<tr>
<td>Nominal composition for $(K_{0.5}Na_{0.5})NbO_3$</td>
<td>10</td>
<td>10</td>
<td>1</td>
</tr>
</tbody>
</table>

Table 1. EDXS analyses of single crystals and matrix grains of samples annealed at 1100°C for 10 h (Fisher et al., 2008b).

4.4 Growth of $[(K_{0.5}Na_{0.5})_{0.97}Li_{0.03}](Nb_{0.8}Ta_{0.2})O_3$ single crystals by SSCG.

The SSCG method was successfully applied to the growth of (Li, Ta)-KNN modified single crystals (Fisher et al., 2007b). Powder of a nominal $[(K_{0.5}Na_{0.5})_{0.97}Li_{0.03}](Nb_{0.8}Ta_{0.2})O_3$ composition was prepared in a similar way as before, but with a higher calcination temperature of 900°C. 0.5 mol % of $K_4CuNb_8O_{23}$ was added as a liquid phase sintering aid. A $<001>$-oriented KTaO$_3$ single crystal was used as a seed. The sample was pre-densified by hot pressing at 975°C / 50 MPa for 2 h. The crystal was grown by annealing in air at 1135°C for 50 hours under atmospheric pressure. A single crystal ~100μm thick grew on the seed (Fig.8). SEM-EDXS analysis showed that the single crystal and the matrix grains have the same composition; however, it was not possible to analyse Li content by means of EDXS.
Fig. 8. SEM micrograph of [(K$_{0.5}$Na$_{0.5}$)$_{0.97}$Li$_{0.03}$]$(Nb_{0.8}Ta_{0.2})O_3$ Single Crystal grown by SSCG (Fisher et al., 2007b)

5. Dedicated structural and compositional study of a (K$_{0.5}$Na$_{0.5}$)NbO$_3$ single crystal

The studies of structure and composition were performed on the hot-pressed KNN single crystals (see Fig. 5a). For the single crystal XRD setup, the size of the single crystals after their removal from the matrix was not sufficient. Therefore, the obtained crystals were crushed and a powder XRD setup was used.

In Fig. 9, experimental XRD powder diffraction patterns of the crushed KNN single crystal and a polycrystalline KNN ceramic, as well as calculated a XRD diffraction pattern are shown. The inset in Fig. 9 shows an enlarged view of the 100/001 and 010 diffraction peaks for the KNN single crystal and ceramic. Both the single crystal and ceramic have narrow and well-defined peaks. No secondary phases were detected (Benčan et al., 2009). In previous work, different workers have refined KNN unit cell parameters using perovskite unit cells with orthorhombic symmetry (Attia et al., 2005), monoclinic symmetry (Shiratori et al., 2005) and also triclinic symmetry (Shiratori et al., 2005). Our experimental data was fitted using the monoclinic symmetry given by Tellier et al. (Tellier et al., 2009), with unit cell parameters $a$=4.0046 Å, $b$=3.9446 Å, $c$=4.0020 Å, and $\beta$=90.3327º.

A precise chemical analysis of the KNN single crystal was performed by WDXS and semi-quantitative EDXS analysis in the SEM at twelve selected points across the KNN single crystal. For WDXS analysis, KNbO$_3$ and NaNbO$_3$ single crystals were used as standards. Table 2 shows the determined elemental composition of the KNN single crystal, which is very close to the nominal one. The small variations in the values of standard deviation for both WDXS and EDXS analysis serve as proof of the crystal’s homogeneity. The latter makes it possible to use these crystals as reference standards for the quantitative analysis of sodium and potassium in other materials (Benčan et al., 2009).
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Fig. 9. XRD powder diffraction patterns of the crushed KNN single crystal and polycrystalline KNN ceramic. A calculated XRD pattern using a monoclinic KNN unit cell is added (Benčan et al., 2009)

<table>
<thead>
<tr>
<th>Element</th>
<th>Nominal composition</th>
<th>WDXS at%</th>
<th>STDEV</th>
<th>EDXS at%</th>
<th>STDEV</th>
</tr>
</thead>
<tbody>
<tr>
<td>K</td>
<td>10</td>
<td>10.06</td>
<td>0.08</td>
<td>9.5</td>
<td>0.1</td>
</tr>
<tr>
<td>Na</td>
<td>10</td>
<td>10.03</td>
<td>0.07</td>
<td>9.8</td>
<td>0.2</td>
</tr>
<tr>
<td>Nb</td>
<td>20</td>
<td>19.89</td>
<td>0.10</td>
<td>20.3</td>
<td>0.3</td>
</tr>
<tr>
<td>O</td>
<td>60</td>
<td>60.02</td>
<td>0.15</td>
<td>60.4*</td>
<td>0.5</td>
</tr>
</tbody>
</table>

Table 2. Elemental composition in at% of the KNN single crystal, determined by WDXS and EDXS, with standard deviation (STDEV). Nominal composition is shown for comparison. Oxygen (*) is calculated from the stoichiometry (Benčan et al., 2009)

The domain structure of KNN single crystals at micro- and nano-scales was analysed using the techniques of optical, scanning and transmission electron microscopy (Benčan et al., 2009). A polarized light optical micrograph of the KNN single crystal is shown in Fig. 10a. The crystal is still embedded in the KNN ceramic matrix. Large ferroelectric domains from 50 to 100 microns in size are revealed by dark/bright contrast oscillations in the micrograph. These large domains in turn contain smaller domains with dimensions from tens of microns down to hundreds of nm. The smaller domains have a herring bone 90° arrangement, as shown in the inset of Fig. 10a. The larger domains in the single crystal were also probed by electron backscattered diffraction (EBSD). The EBSD image (Fig. 10b) shows the distribution of the orientations in the crystal and surrounding matrix. Differences in colour inside the single crystal are attributed to the differently oriented ferroelectric domains. From the colour-key inverse-pole-figure it can be seen that the orientation inside the single crystal is
changing by 90° and that there are three different orientations rotated to each other by 90° angles.

Fig. 10. Optical microscope micrographs of the KNN single crystal and its domain microstructure. The inset shows a herring bone 90° arrangement of smaller domains (a) EBSD orientation map of the KNN single crystal and the corresponding color-key inverse-pole-figure (b) (Benčan et al., 2009)

In order to determine the domain structure at the nanometer scale, the specimen was investigated by TEM (Benčan et al., 2009). Smaller saw-like domains with a size of about 50nm were arranged within the larger ones (Fig.11).

Fig. 11. TEM-BF image of the KNN single crystal with corresponding SAED patterns showing the presence of 180° domains. Due to the very small difference in a and c unit cell parameters, a and c axes were chosen arbitrarily (Benčan et al., 2009)

The overlapping of these domains is represented by the selected area diffraction (SAED) pattern in the [010] zone axis, taken from the area of ~1.5 μm. Splitting of the {h00} or {00l} reflections parallel to the <001> or <100> directions is seen. This is due to the β angle (~90.3°). Such patterns can be experimentally observed only in the case where the [100] or
[001] direction of one domain is parallel to the [-100] or [00-1] direction of the other one, meaning that these are 180° domains.

6. Dielectric, ferroelectric, piezoelectric and electrostrictive properties of K$_{0.5}$Na$_{0.5}$NbO$_3$ single crystals

The dielectric properties of a hot-pressed KNN single crystal (see Fig. 5a for reference) were measured on the as-cut piece of crystal in two perpendicular orientations. These were determined from EBSD analysis and described as [1 3 1] and the [3 2 3]. Fig. 12 shows the temperature dependence of the dielectric constant ($\varepsilon$) and the dielectric losses (tan $\delta$) measured for the KNN single crystal in the above mentioned directions and also for the surrounding polycrystalline KNN matrix. The highest value of $\varepsilon$ was obtained for the [1 3 1] direction of the KNN single crystal across whole temperature range. At the same time, two phase transitions from the monoclinic to the tetragonal phase (T$_{1}$) at around 193°C, and from the tetragonal to the cubic phase (T$_{2}$) at around 410°C were measured (Ursič et al, 2010). The latter are in accordance with the transitions observed in the surrounding polycrystalline KNN ceramic, which is another indication of the obtained crystal compositional homogeneity. Table 3 summarizes the dielectric properties obtained for the KNN single crystal in both directions and for the surrounding polycrystalline KNN matrix, and gives a comparison with the dielectric properties of KNN-based single crystals reported in the literature.

Due to the high dielectric constant, the [1 3 1] direction of KNN single crystal was chosen for further measurements of the ferroelectric, piezoelectric and electrostrictive properties. The ferroelectric properties, i.e. the remnant polarization (Pr) and coercive field (Ec) measured for the KNN single crystal and surrounding polycrystalline KNN matrix, are compared to the literature and shown in Table 4.
Table 3. The $\epsilon$, $\tan\delta$ and monoclinic - tetragonal ($T_1$) and tetragonal - cubic ($T_2$) phase transition temperatures for KNN single crystal in the $[1\ 3\ 1]$ and the $[3\ 2\ 3]$ directions and for KNN ceramics. For comparison the dielectric properties obtained on KNN based single crystals by different groups are added (Uršič et al., 2010)

<table>
<thead>
<tr>
<th>System</th>
<th>Freq. (kHz)</th>
<th>$\epsilon$ Troom</th>
<th>$\tan\delta$ Troom</th>
<th>$T_1$ (°C)</th>
<th>$T_2$ (°C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>KNN s.c. $[1\ 3\ 1]$ this study</td>
<td>100</td>
<td>1015</td>
<td>0.01</td>
<td>192</td>
<td>410</td>
</tr>
<tr>
<td>KNN s.c. $[3\ 2\ 3]$ this study</td>
<td>100</td>
<td>650</td>
<td>0.01</td>
<td>193</td>
<td>409</td>
</tr>
<tr>
<td>KNN ceramics this study</td>
<td>100</td>
<td>750</td>
<td>0.01</td>
<td>193</td>
<td>411</td>
</tr>
<tr>
<td>$K_{0.55}Na_{0.45}NbO_3$ s.c. [001] Lin et al., 2009</td>
<td>100</td>
<td>240</td>
<td>0.02</td>
<td>205</td>
<td>393</td>
</tr>
<tr>
<td>$K_{0.47}Na_{0.53}NbO_3$ s.c. [100] Kizaki et al., 2007</td>
<td>1000</td>
<td>600</td>
<td>below 0.1</td>
<td>190</td>
<td>390</td>
</tr>
<tr>
<td>$K_{0.53}Na_{0.47}Mg_{0.03}Nb_{0.97}O_3$ s.c. [100] Kizaki et al., 2007</td>
<td>1000</td>
<td>740</td>
<td>below 0.1</td>
<td>160</td>
<td>390</td>
</tr>
<tr>
<td>$0.95(K_{0.5}Na_{0.5})NbO_3-0.05LiNbO_3$ s.c. [001] Chen et al., 2007</td>
<td>100</td>
<td>185</td>
<td>0.01</td>
<td>192</td>
<td>426</td>
</tr>
<tr>
<td>$Li_{0.02}(Na_{0.5}K_{0.5})_{0.98}NbO_3$ s.c. [001] Davis et al., 2007</td>
<td>1</td>
<td>205</td>
<td>0.33</td>
<td>177</td>
<td>/</td>
</tr>
</tbody>
</table>

Table 4. Ferroelectric properties of KNN single crystals in the $[1\ 3\ 1]$ direction and for KNN ceramics. For comparison the ferroelectric properties obtained on KNN based single crystals by different groups are added (Uršič et al., 2010)

<table>
<thead>
<tr>
<th>System</th>
<th>Freq. (Hz)</th>
<th>$P_r$ (µC/cm$^2$)</th>
<th>$E_c$ (kV/cm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>KNN s.c. $[1\ 3\ 1]$ this study</td>
<td>50</td>
<td>17</td>
<td>24</td>
</tr>
<tr>
<td>KNN ceramics this study</td>
<td>50</td>
<td>15</td>
<td>24</td>
</tr>
<tr>
<td>$K_{0.47}Na_{0.53}NbO_3$ s.c. [100] Kizaki et al., 2007</td>
<td>1</td>
<td>/</td>
<td>/</td>
</tr>
<tr>
<td>$K_{0.53}Na_{0.47}Mg_{0.03}Nb_{0.97}O_3$ s.c. [100] Kizaki et al., 2007</td>
<td>1</td>
<td>40</td>
<td>12</td>
</tr>
<tr>
<td>$0.95(K_{0.5}Na_{0.5})NbO_3-0.05LiNbO_3$ s.c. [001] Chen et al., 2007</td>
<td>10</td>
<td>9</td>
<td>22</td>
</tr>
</tbody>
</table>

The displacement signal versus the applied voltage of the KNN single crystal in the $[1\ 3\ 1]$ direction and of the surrounding KNN ceramic were measured using an atomic force microscope (AFM). Prior to the analysis, an AFM measurement was performed as a reference on glass under the same experimental conditions as used for the KNN single crystal and ceramics. No strain was observed for the non-piezoelectric glass, confirming that strains observed during AFM analysis of the KNN crystal and ceramics are piezoelectric in nature. The KNN single crystals were not poled before the AFM measurement. The obtained displacement signal consists of two components. The first component has the same frequency as the applied voltage, i.e., this is the linear piezoelectric component (see Fig. 13). The second component is the pronounced quadratic component with the double frequency (see inset in Fig. 14). The piezoelectric coefficients $d_{33}$, shown in Fig. 13, were determined from the slopes of the linear fits of the linear component of displacement versus the applied voltage (Uršič et al., 2010). The $d_{33}$ piezoelectric coefficients for the KNN single crystal and for the surrounding ceramic are approximately 80 pm/V at a measurement frequency of 2 Hz. As frequency increases,
the $d_{33}$ value for the KNN single crystal decreases (see Fig. 13). Although very small applied electric fields (up to 0.1 kV/mm) were used to measure the piezoelectric coefficient for the KNN single crystal, the obtained $d_{33}$ value (80 pm/V) was in the same range as for the poled KNN ceramic. The explanation of such behaviour can be given by the domain structure of the KNN single crystal. As shown in Section 5 the KNN single crystal consists of large 90° domains with widths of up to 100 microns, and smaller 180° domains with widths ranging between a few tens of nms to 300 nm. Since the contact area of the AFM tip is around 20 nm, it is likely that only the smaller 180° domain walls are moving during the AFM measurements. These small 180° domains probably contribute to the obtained linear response of the KNN single crystal. The inability of the 180° domains to reorientate quickly enough at higher frequencies explains the decrease in $d_{33}$ with increasing measurement frequency. It has been previously demonstrated by McKinstry et al. (McKinstry et al., 2006) that if the mobility of 90° domains is limited, then the 180° domains can contribute to the piezoelectric linear response.

![Graph](https://example.com/graph.png)

**Fig. 13.** The linear part of displacement versus voltage amplitude of KNN single crystal in [1 3 1] direction measured at 2 Hz, 20 Hz and 200 Hz. The measurement for KNN surrounding ceramics at 2 Hz is added for comparison (Uršič et al., 2010)

The electrostrictive coefficients ($M_{33}$) were determined from the slope of the linear fit of the relative strain versus the square of the amplitude of the electric field, as shown in Fig. 14. The $M_{33}$ for the surrounding KNN ceramic was lower than that of the KNN single crystal. The measured values $M_{33}$ for the KNN single crystal are significantly higher than values of $M_{33}$ for PMN-based single crystals. The highest obtained electrostrictive coefficient for a 0.65Pb(Mg$_{1/3}$Nb$_{2/3}$)O$_3$-0.35PbTiO$_3$ single crystal was in the range 1.3 to 4x10$^{-15}$ m$^2$/V$^2$ at 0.01 Hz; a 90° domain wall contribution to electrostriction was reported (Bokov&Ye, 2002). Such a high $M_{33}$ value for the KNN single crystal can arise from the intrinsic electrostrictive behaviour as well as the extrinsic contribution, i.e., the strain from the domain-wall motion. Most probably in the KNN single crystal, the main contribution to electrostrictive strain arises from the contribution of 180° domain walls. Our results agree with the findings obtained by McKinstry et al. (McKinstry et al., 2006), who showed that 180° domains walls...
can contribute to the linear response as well as to electrostrictive strain response in ferroelectric materials. Although the pure electrostrictive response should be frequency independent, they observed in (111) Pb(Zr$_{0.45}$Ti$_{0.55}$)O$_3$ thin films a decrease of the second-order strain with frequency by 20%, as was also the case for our KNN single crystal.

Fig. 14. Relative strain versus square of the amplitude of the electric field of KNN single crystal in the [1 3 1] direction at 2 Hz, 20 Hz and 200 Hz. Inset shows the quadratic part of displacement versus voltage for KNN single crystal. The measurement for KNN surrounding ceramics at 2 Hz is added for comparison (Uršič et al., 2010)

7. Conclusions

In this chapter the principles of the SSCG technique and its application to the growth of K$_{0.5}$Na$_{0.5}$NbO$_3$ (KNN) and Li,Ta-modified KNN single crystals were presented. With the use of the complementary analytical characterization techniques, i.e. XRD, optical microscopy and electron microscopy (SEM, EDXS, WDXS, EBSD, TEM, SAED), the precise compositional and structural analysis of KNN single crystals was performed and the correlation with its electrical properties was given.

There are several possible directions for future work. First, it would be useful to grow larger single crystals. This will enable crystals to be cut in controlled orientations e.g along the [001] or [110] directions and their properties measured and compared with KNN crystals grown by solution-based methods. Furthermore, alternative seed crystals need to be found. Although KTaO$_3$ single crystals make excellent seeds, they are rather expensive and to grow large single crystals, large seed crystals are needed. If cheaper alternatives could be found, this would reduce the cost of growing large KNN single crystals. Work needs to be done in growing single crystals from seeds placed on top of the ceramic substrate. Finally, growth of other compositions such as Li-doped KNN should be carried out.

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8. Acknowledgments

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9. References


Chen, K., Xu, G., Yang, D., Wang, X. & Li J. (2007). Dielectric and piezoelectric properties of lead-free 0.95(K$_{0.5}$Na$_{0.5}$)NbO$_3$–0.05LiNbO$_3$ crystals grown by the Bridgman method. *Journal of Applied Physics*, Vol. 101, No. 4, (February 2007), pp. 044103-1, ISSN:0021-8979


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Lin, D., Li, Z., Zhang, S., Xu Z. & Yao, X. (2009). Dielectric/piezoelectric properties and temperature dependence of domain structure evolution in lead free $K_0.3Na_0.7NbO_3$ single crystal. Solid State Communications, Vol. 149, No.39-40, (October 2009), pp. 1646-1649, ISSN:0038-1098


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Ferroelectric materials have been and still are widely used in many applications, that have moved from sonar towards breakthrough technologies such as memories or optical devices. This book is a part of a four volume collection (covering material aspects, physical effects, characterization and modeling, and applications) and focuses on ways to obtain high-quality materials exhibiting large ferroelectric activity. The book covers the aspect of material synthesis and growth, doping and composites, lead-free devices, and thin film synthesis. The aim of this book is to provide an up-to-date review of recent scientific findings and recent advances in the field of ferroelectric materials, allowing a deep understanding of the material aspects of ferroelectricity.

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