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First-Principles Study of ABO_3 : Role of the $B-O$ Coulomb Repulsions for Ferroelectricity and Piezoelectricity

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1. Introduction

Since Cohen (Cohen & Krakauer, 1990; Cohen, 1992) proposed an origin for ferroelectricity in perovskite oxides, investigations of ferroelectric materials using first-principles calculations have been extensively studied (Ahart et al., 2008; Bévilion et al., 2007; Bousquet et al., 2006; Chen et al., 2004; Diéguez et al., 2005; Furuta & Miura, 2010; Khenata et al., 2005; Kornev et al., 2005; Miura & Tanaka, 1998; Miura, 2002; Miura et al., 2009; 2010a;b; Miura & Furuta, 2010; Miura et al., 2011; Oguchi et al., 2009; Ricinski et al., 2006; Uratani et al., 2008; Vanderbilt, 2000; Z. Wu et al., 2005). Currently, using the pseudopotential (PP) methods, most of the crystal structures in ferroelectric perovskite oxides (ABO_3) as well as perovskite-related oxides can be precisely predicted. However, it is also known that the most stable structures of ABO_3 optimized by the first-principles PP methods are sometimes inconsistent with the experimental results.

$BaTiO_3$ is a well-known ferroelectric ABO_3 , and shows the tetragonal structure at room temperature. However, even in this well-known material, the optimized structure by the PP methods of first-principles calculations is strongly dependent on the choice of the Ti PPs, i.e., preparation for Ti 3s and 3p semicore states in addition to Ti 3d and 4s valence states is essential to the appearance of the tetragonal structure. This is an important problem for ferroelectricity, but it has been generally recognized for a long time that this problem is within an empirical framework of the calculational technics (Gonze et al., 2005).

It is known that ferroelectric state appears when the long-range forces due to the dipole-dipole interaction overcome the short-range forces due to the Coulomb repulsions. Cohen (Cohen & Krakauer, 1990; Cohen, 1992) proposed that the hybridization between Ti 3d state and O 2p state (Ti 3d–O 2p) in $BaTiO_3$ and $PbTiO_3$, which weakens the short-range force of the Coulomb repulsions between Ti and O ions, is origin of ferroelectricity. However, it seems to be difficult to consider explicitly whether the long-range force due to the dipole-dipole interaction can or cannot overcome the short-range force only with the Ti 3d–O 2p hybridization. Investigations about the relationship between the Ti–O Coulomb repulsions and the appearance of ferroelectricity were separately reported. Theoretically, we previously investigated (Miura & Tanaka, 1998) the influence of the Ti– O_z Coulomb repulsions on Ti ion displacement in tetragonal $BaTiO_3$ and $PbTiO_3$, where O_z denotes the O atom to the z-axis (Ti is displaced to the z-axis). Whereas the hybridization between Ti 3d state and O_z 2p_z state stabilize Ti ion displacement, the strong Coulomb repulsions between Ti 3s and 3p_z

states and O $2p_z$ states do not favourably cause Ti ion displacement. Experimentally, on the other hand, Kuroiwa *et al.* (Kuroiwa *et al.*, 2001) showed that the appearance of ferroelectric state is closely related to the total charge density of Ti–O bondings in BaTiO_3 . As discussed above, investigation about a role of Ti 3s and 3p states is important in the appearance of the ferroelectric state in tetragonal BaTiO_3 .

It has been generally known (Miura & Furuta, 2010) that the most stable structure of ABO_3 is closely related to the tolerance factor t ,

$$t \equiv \frac{r_A + r_O}{\sqrt{2}(r_B + r_O)}, \quad (1)$$

where r_A , r_B , and r_O denote the ionic radii of A, B, and O ions, respectively. Generally, the most stable structure is tetragonal for $t \gtrsim 1$, cubic for $t \approx 1$, and rhombohedral or orthorhombic for $t \lesssim 1$. In fact, BaTiO_3 ($t = 1.062$) and SrTiO_3 ($t = 1.002$) show tetragonal and cubic structures in room temperature, respectively. However, under external pressure, e.g., hydrostatic or in-plane pressure (Ahart *et al.*, 2008; Fujii *et al.*, 1987; Haeni *et al.*, 2004), the most stable structures of ABO_3 generally change; e.g., SrTiO_3 shows the tetragonal and ferroelectric structure even in room temperature when the a lattice parameter along the [100] axis (and also the [010] axis) is smaller than the bulk lattice parameter with compressive stress (Haeni *et al.*, 2004). Theoretical investigations of ferroelectric ABO_3 under hydrostatic or in-plane pressure by first-principles calculations have been reported (Bévilion *et al.*, 2007; Diéguez *et al.*, 2005; Furuta & Miura, 2010; Khenata *et al.*, 2005; Kornev *et al.*, 2005; Miura *et al.*, 2010a; Ricinchi *et al.*, 2006; Uratani *et al.*, 2008; Z. Wu *et al.*, 2005), and their calculated results are consistent with the experimental results. However, even in BaTiO_3 , which are a well-known lead-free ferroelectric and piezoelectric ABO_3 , few theoretical papers about the piezoelectric properties with in-plane compressive stress have been reported.

Recently, we investigated the roles of the Ti–O Coulomb repulsions in the appearance of a ferroelectric states in tetragonal BaTiO_3 by the analysis of a first-principles PP method (Miura *et al.*, 2010a). We investigated the structural properties of tetragonal and rhombohedral BaTiO_3 with two kind of Ti PPs, and propose the role of Ti 3s and 3p states for ferroelectricity. Moreover, we also investigated the structural, ferroelectric, and piezoelectric properties of tetragonal BaTiO_3 and SrTiO_3 with in-plane compressive structures (Furuta & Miura, 2010). We discussed the difference in the piezoelectric mechanisms between BaTiO_3 and SrTiO_3 with in-plane compressive structures, which would be important for piezoelectric material design. In this chapter, based on our previous reports (Furuta & Miura, 2010; Miura *et al.*, 2010a), the author discusses a general role of B–O Coulomb repulsions for ferroelectricity and piezoelectricity in ABO_3 , especially in BaTiO_3 and SrTiO_3 .

2. Calculations

Calculations of BaTiO_3 and SrTiO_3 were performed using the ABINIT package code (Gonze *et al.*, 2002), which is one of the norm-conserving PP (NCPP) methods. Electron-electron interaction was treated in the local-density approximation (LDA) (Perdew & Wang, 1992). Pseudopotentials were generated using the OPIUM code (Rappe, 2004):

(i) In order to investigate the role of Ti 3s and 3p states for BaTiO_3 , two kinds of Ti PPs were prepared: one is the Ti PP with 3s, 3p, 3d and 4s electrons treated as semicore or valence electrons (Ti3spd4s PP), and the other is the Ti PP with only 3d and 4s electrons treated as valence electrons (Ti3d4s PP). The above pseudopotentials were generated using the OPIUM

code (Rappe, 2004), and the differences between the calculated result and the experimental one are within 1.5 % of the lattice parameter and within 10 % of the bulk modulus in the optimized calculation of bulk Ti in both PPs. Moreover, Ba PP with 5s, 5p and 6s electrons treated as semicore or valence electrons, and O PP with 2s and 2p electrons treated as semicore or valence electrons, were also prepared. The cutoff energy for plane-wave basis functions was set to be 50 Hartree (Hr). A $6 \times 6 \times 6$ Monkhorst-Pack k -point mesh was set in the Brillouin zone of the unit cell. The number of atoms in the unit cell was set to be five, and positions of all the atoms were optimized within the framework of the tetragonal ($P4mm$) or rhombohedral ($R3m$) structure.

(ii) The ferroelectric and piezoelectric properties of $SrTiO_3$ and $BaTiO_3$ with compressive tetragonal structures are investigated. Pseudopotentials were generated using the OPIUM code (Rappe, 2004); 4s (5s), 4p (5p) and 5s (6s) electrons for Sr (Ba), 3s, 3p, 3d and 4s electrons for Ti, and 2s and 2p electrons for O were treated as semicore or valence electrons. The cutoff energy for the plane wave basis functions was set to be 50 Hr. A $6 \times 6 \times 6$ Monkhorst-Pack k -point mesh was set in the Brillouin zone of the unit cell. The number of atoms in the ABO_3 unit cell was set to be five, and the coordinations of all the atoms were optimized within a framework of the tetragonal ($P4mm$) structure. An $6 \times 6 \times 6$ Monkhorst-Pack k -point sampling was set in Brillouin zone of the unit cell.

In the present calculations, spontaneous polarizations and piezoelectric constants were also evaluated, due to the Born effective charges (Resta, 1994) and density-functional perturbation theory (Hamann et al., 2005; X. Wu et al., 2005). The spontaneous polarization of tetragonal structures along the [001] axis, P_3 , is defined as,

$$P_3 \equiv \sum_k \frac{ec}{\Omega} Z_{33}^*(k) u_3(k), \quad (2)$$

where e , c , and Ω denote the charge unit, the lattice parameter of the unit cell along the [001] axis, and the volume of the unit cell, respectively. $u_3(k)$ denotes the displacement along the [001] axis of the k th atom, and $Z_{33}^*(k)$ denotes the Born effective charges (Resta, 1994) which contributes to the P_3 from the $u_3(k)$. The piezoelectric e constants, on the other hand, are defined as

$$e_{\alpha\beta} \equiv \left(\frac{\partial P_\alpha}{\partial \eta_\beta} \right)_u + \sum_k \left(\frac{\partial P_\alpha}{\partial u_\alpha(k)} \right)_\eta \frac{\partial u_\alpha(k)}{\partial \eta_\beta}, \quad (3)$$

where P , η , and $u(k)$ denote the spontaneous polarization, the strain, and the displacement of the k th atom, respectively. α and β denote the direction-indexes of the axis, i.e., 1 along the [100] axis, 2 along the [010] axis, and 3 along the [001] axis, respectively. In eq. (3), the first term of the right hand denotes the clamped term evaluated at vanishing internal strain, and the second term denotes the relaxed term that is due to the relative displacements. According to the eqs. (2) and (3), therefore, e_{33} or e_{31} can be especially written as,

$$e_{3\beta} = \left(\frac{\partial P_3}{\partial \eta_\beta} \right)_u + \sum_k \frac{ec}{\Omega} Z_{33}^*(k) \frac{\partial u_3(k)}{\partial \eta_\beta} \quad (\beta = 3, 1). \quad (4)$$

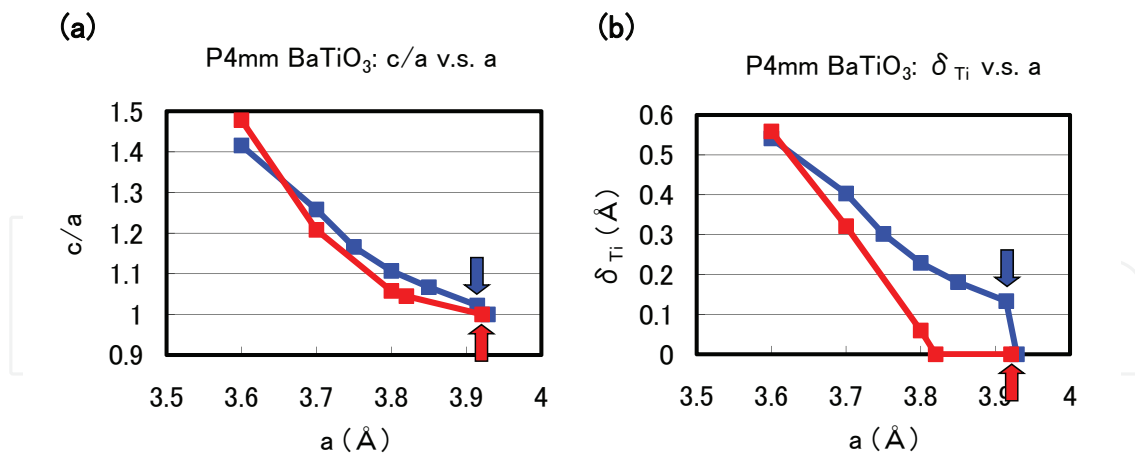


Fig. 1. Optimized calculated results as a function of a lattice parameters in tetragonal BaTiO₃: (a) c/a ratio and (b) δ_{Ti} to the [001] axis. Blue lines correspond to the results with the Ti3spd4s PP, and red lines correspond to those with the Ti3d4s PP. Results with arrows are the fully optimized results, and the other results are those with c and all the inner coordinations optimized for fixed a (Miura et al., 2010a).

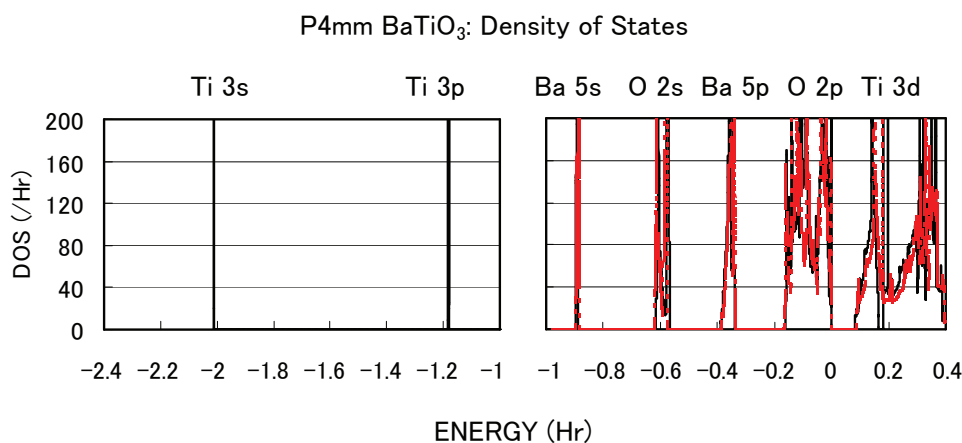


Fig. 2. Total density of states (DOS) of fully optimized tetragonal BaTiO₃ with the Ti3spd4s PP (solid line) and cubic BaTiO₃ with the Ti3d4s PP (red dashed line) (Miura et al., 2010a).

3. Results and discussion

3.1 BaTiO₃: Role of Ti 3s and 3p states for ferroelectricity

In this subsection, the author discusses the role of Ti 3s and 3p states for ferroelectricity for ferroelectricity in tetragonal BaTiO₃.

Figures 1(a) and 1(b) show the optimized results for the ratio c/a of the lattice parameters and the value of the Ti ion displacement (δ_{Ti}) as a function of the a lattice parameters in tetragonal BaTiO₃, respectively. Results with arrows are the fully optimized results, and the others results are those with the c lattice parameters and all the inner coordinations optimized for fixed

a. Note that the fully optimized structure of $BaTiO_3$ is tetragonal with the Ti3spd4s PP, whereas it is cubic ($Pm\bar{3}m$) with the Ti3d4s PP. As shown in Fig. 1(a) and 1(b), c/a and δ_{Ti} show significantly different results for $a \gtrsim 3.7$ whereas they show almost the same results for $a \lesssim 3.7$, for both Ti PPs. This result suggests that the optimized results of ABO_3 with smaller lattice parameters, e.g., under high pressure (Bévilion et al., 2007), are almost independent of the choice of PP.

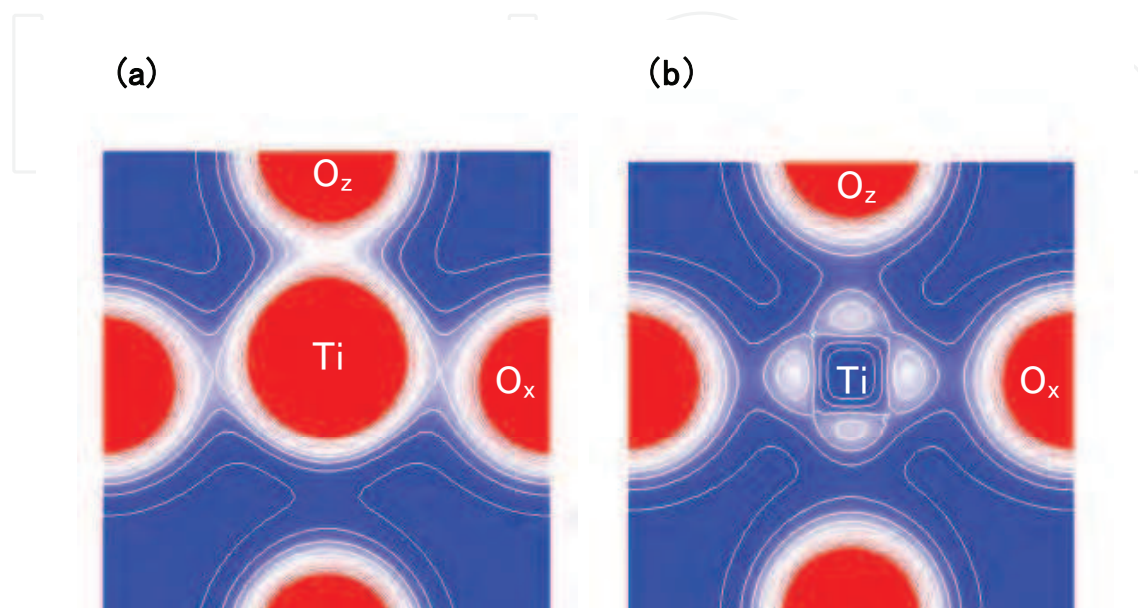


Fig. 3. Two-dimensional electron-density contour map on the xz -plane for tetragonal $BaTiO_3$: (a) with the Ti3spd4s PP, and (b) with the Ti3d4s PP. The optimized calculated results with a fixed to be 3.8 are shown in both figures. The electron density increases as color changes from blue to red via white. Contour curves are drawn from 0.4 to $2.0 e^3$ with increments of $0.2 e^3$ (Miura et al., 2010a).

The calculated results shown in Fig. 1 suggest that the explicit treatment of Ti 3s and 3p semicore states is essential to the appearance of ferroelectric states in $BaTiO_3$. In the following, the author investigates the role of Ti 3s and 3p states for ferroelectricity from two viewpoints. One viewpoint concerns hybridizations between Ti 3s and 3p states and other states. Figure 2 shows the total density of states (DOS) of tetragonal $BaTiO_3$ with two Ti PPs. Both results are in good agreement with previous calculated results (Chen et al., 2004; Khenata et al., 2005) by the full-potential linear augmented plane wave (FLAPW) method. In the DOS with the Ti3spd4s PP, the energy “levels”, not bands, of Ti 3s and 3p states, are located at -2.0 Hr and -1.2 Hr, respectively. This result suggests that the Ti 3s and 3p orbitals do not make any hybridizations but only give Coulomb repulsions with the O orbitals as well as the Ba orbitals. In the DOS with the Ti3d4s PP, on the other hand, the energy levels of Ti 3s and 3p states are not shown because Ti 3s and 3p states were treated as the core charges. This result means that the Ti 3s and 3p orbitals cannot even give Coulomb repulsions with the O orbitals as well as the Ba orbitals.

Another viewpoint is about the Coulomb repulsions between Ti 3s and $3p_{x(y)}$ states and $O_{x(y)}$ 2s and $2p_{x(y)}$ states in tetragonal $BaTiO_3$. Figures 3(a) and 3(b) show two-dimensional electron-density contour map on the xz -plane for tetragonal $BaTiO_3$ with the Ti3spd4s PP, and that with the Ti3d4s PP, respectively. These are the optimized calculated results with a fixed

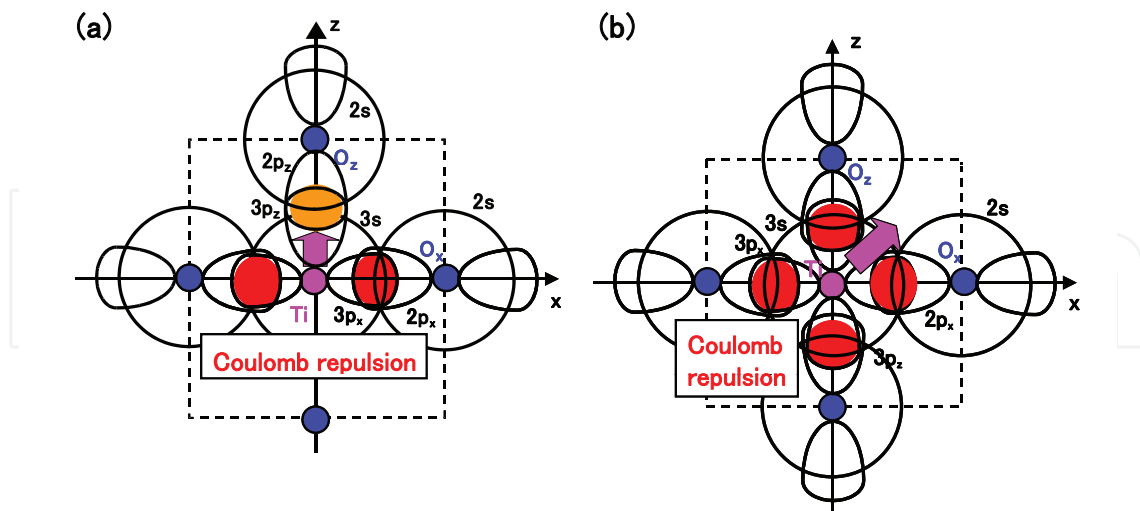


Fig. 4. Illustrations of the proposed mechanisms for the Coulomb repulsions between Ti 3s and 3p states and O 2s and 2p states in BaTiO₃: (a) anisotropic Coulomb repulsions between Ti 3s and 3p_{x(y)} states and O_{x(y)} 2s and 2p_{x(y)} states, and between Ti 3s and 3p_z states and O_z 2s and 2p_z states, in the tetragonal structure. (b) isotropic Coulomb repulsions between Ti 3s and 3p_{x(y)(z)} states and O_{x(y)(z)} 2s and 2p_{x(y)(z)} states, in the rhombohedral structure (Miura et al., 2010a).

to be 3.8, and the electron density in Fig. 3(a) is quantitatively in good agreement with the experimental result (Kuroiwa et al., 2001). The electron density between Ti and O_x ions in Fig. 3(a) is larger than that in Fig. 3(b), which suggests that Ti ion displacement is closely related to the Coulomb repulsions between Ti 3s and 3p states and O 2s and 2p states along the [001] axis (the z-axis in this case).

The present discussion of the Coulomb repulsions is consistent with the previous reports. A recent soft mode investigation (Oguchi et al., 2009) of BaTiO₃ shows that Ba ions contribute little to the appearance of Ti ion displacement along the [001] axis. This result suggests that Ti ion displacement is closely related to the structural distortion of TiO₆ octahedra. In the present calculations, on the other hand, the only difference between BaTiO₃ with the Ti3spd4s PP and with the Ti3d4s PP is the difference in the expression for the Ti 3s and 3p states, i.e., the explicit treatment and including core charges. However, our previous calculation (Miura & Tanaka, 1998) shows that the strong Coulomb repulsions between Ti 3s and 3p_z states and O_z 2s and 2p_z states do not favour Ti ion displacement along the [001] axis. This result suggests that the Coulomb repulsions between Ti 3s and 3p_{x(y)} states and O_{x(y)} 2s and 2p_{x(y)} states would contribute to Ti ion displacement along the [001] axis, and the suggestion is consistent with a recent calculation (Uratani et al., 2008) for PbTiO₃ indicating that the tetragonal and ferroelectric structure appears more favourable as the *a* lattice parameter decreases.

Considering the above investigations, the author proposes the mechanism of Ti ion displacement as follows: Ti ion displacement along the z-axis appears when the Coulomb repulsions between Ti 3s and 3p_{x(y)} states and O_{x(y)} 2s and 2p_{x(y)} states, in addition to the dipole-dipole interaction, overcome the Coulomb repulsions between Ti 3s and 3p_z states and O_z 2s and 2p_z states (Miura & Tanaka, 1998). An illustration of the Coulomb repulsions is shown in Fig. 4(a). In fully optimized BaTiO₃ with the Ti3spd4s PP, the Ti ion can be displaced due to the above mechanism. In fully optimized BaTiO₃ with the Ti3d4s PP, on the other

hand, the Ti ion cannot be displaced due to the weaker Coulomb repulsions between Ti and $O_{x(y)}$ ions. However, since the Coulomb repulsion between Ti and O_z ions in $BaTiO_3$ with the Ti3d4s PP is also weaker than that in $BaTiO_3$ with the Ti3spd4s PP, the Coulomb repulsions between between Ti and $O_{x(y)}$ ions in addition to the log-range force become comparable to the Coulomb repulsions between Ti and O_z ions both in Ti PPs, as the lattice parameter a becomes smaller. The above discussion suggests that the hybridization between Ti 3d and O_z 2s and $2p_z$ stabilizes Ti ion displacement, but contribute little to a driving force for the appearance of Ti ion displacement.

It seems that the above proposed mechanism for tetragonal $BaTiO_3$ can be applied to the mechanism of Ti ion displacement in rhombohedral $BaTiO_3$, as illustrated in Fig. 4(b). The strong isotropic Coulomb repulsions between Ti 3s and $3p_{x(y)(z)}$ states and $O_{x(y)(z)}$ 2s and $2p_{x(y)(z)}$ states yield Ti ion displacement along the [111] axis. On the other hand, when the isotropic Coulomb repulsions are weaker or stronger, the Ti ion cannot be displaced and therefore it is favoured for the crystal structure to be cubic.

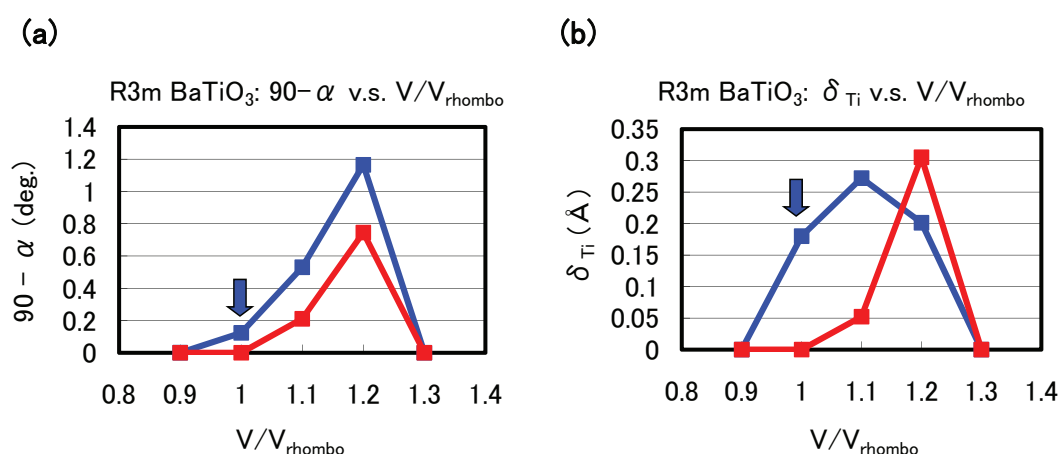


Fig. 5. Optimized calculated results as a function of the fixed volumes of the unit cells in rhombohedral $BaTiO_3$: (a) $90 - \alpha$ degree and (b) δ_{Ti} to the [111] axis. Blue lines correspond to the results with the Ti3spd4s PP, and red lines correspond to those with the Ti3d4s PP. V_{rhombo} denote the volume of the fully optimized unit cell with the Ti 3spd4s PP. Results with arrows are the fully optimized results, and the other results are those with all the inner coordinations optimized for fixed volumes of the unit cells (Miura et al., 2010a).

Let us investigate the structural properties of rhombohedral $BaTiO_3$. Figures 5(a) and 5(b) show the optimized results of the $90 - \alpha$ degree and δ_{Ti} as a function of fixed volumes of the unit cells in rhombohedral $BaTiO_3$, respectively, where α denotes the angle between two lattice vectors. In these figures, α denotes the angle between two crystal axes of rhombohedral $BaTiO_3$, and δ_{Ti} denotes the value of the Ti ion displacement along the [111] axis. Results with arrows are the fully optimized results; V_{rhombo} denote the volume of the fully optimized unit cell with the Ti 3spd4s PP. The other results are those with all the inner coordinations optimized with fixed volumes of the unit cells. The proposal mechanisms about the Coulomb repulsions seem to be consistent with the calculated results shown in Fig. 5: For $V/V_{\text{rhombo}} \lesssim 0.9$ or $\gtrsim 1.3$, the isotropic Coulomb repulsions are weaker or stronger, and the Ti ion cannot be displaced along the [111] axis and therefore the crystal structure is cubic for both Ti PPs. For $0.9 \lesssim V/V_{\text{rhombo}} \lesssim 1.3$, on the other hand, the isotropic Coulomb repulsions

are strong enough to yield Ti ion displacement for both Ti PPs. However, since the magnitude of the isotropic Coulomb repulsion is different in the two Ti PPs, the properties of the $90-\alpha$ degree and δ_{Ti} are different quantitatively.

3.2 Role of the Ti–O Coulomb repulsions for piezoelectric SrTiO₃ and BaTiO₃

As discussed in the previous subsection, the Coulomb repulsions between Ti 3s and $3p_{x(y)}$ states and $O_{x(y)}$ 2s and $2p_{x(y)}$ states have an important role in the appearance of the ferroelectric state in tetragonal BaTiO₃. In this subsection, the author discusses the role of the Ti–O Coulomb repulsions for piezoelectric SrTiO₃ and BaTiO₃.

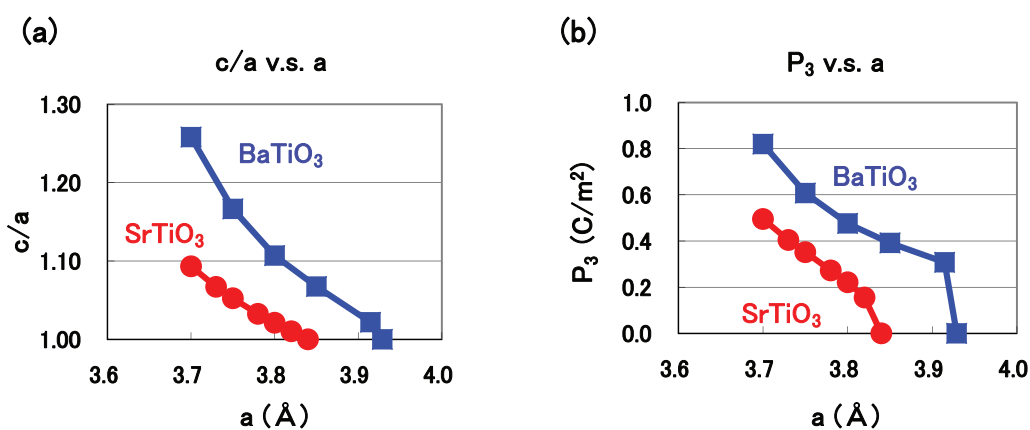


Fig. 6. Optimized calculated results as a function of a lattice parameters in compressive tetragonal SrTiO₃ and BaTiO₃: (a) c/a ratio and (b) P_3 , i.e., spontaneous polarization along the [001] axis (Furuta & Miura, 2010).

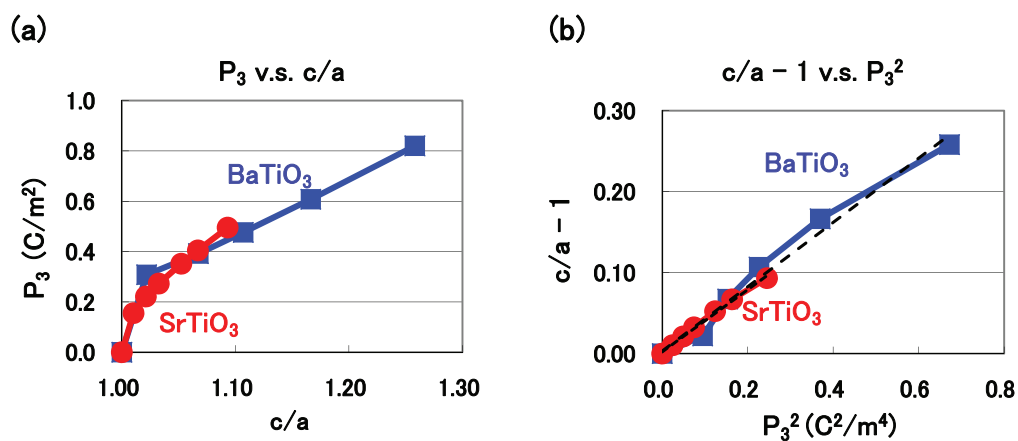


Fig. 7. (a) P_3 as a function of c/a ratios, and (b) c/a ratio as a function of P_3^2 . These values are derived from the calculated results as shown in Figs. 6(a) and (b). Dotted and dashed lines in Fig. 7(b) serve as visual guides for SrTiO₃ and BaTiO₃, respectively (Furuta & Miura, 2010).

Figures 6(a) shows the optimized results for the ratio c/a as a function of the a lattice parameters in tetragonal SrTiO₃ and BaTiO₃. These results are the fully optimized results and the results with the c lattice parameters and all the inner coordinations optimized for

fixed a . The fully optimized parameters of $SrTiO_3$ ($a = 3.84$: cubic) and $BaTiO_3$ ($a = 3.91$ and $c = 4.00$: tetragonal) are within 2.0% in agreement with the experimental results in room temperature. Figure 6(b) shows the evaluated results for P_3 as a function of the a lattice parameters in tetragonal $SrTiO_3$ and $BaTiO_3$, where P_3 , which is evaluated by eq. (2), denotes the spontaneous polarization along the [001] axis. Note that the tetragonal and ferroelectric structures appear even in $SrTiO_3$ when the fixed a lattice parameter is compressed to be smaller than the fully-optimized a lattice parameter. As shown in Figs. 6(a) and 6(b), the tetragonal and ferroelectric structure appear more favorable as the fixed a lattice parameter decreases, which is consistent with previous calculated results (Miura et al., 2010a; Ricinchi et al., 2006; Uratani et al., 2008). The results would be due to the suggestion discussed in the previous section that the large Coulomb repulsion of Ti - O bondings along the [100] axis (and the [010] axis) is a driving force of the displacement of Ti ions along the [001] axis, i.e., the large Coulomb repulsion along the [100] axis (and the [010] axis) is essential for the appearance of the tetragonal structure. Figure 7(a) shows the relationship between P_3 and the ratio c/a , where P_3 and c/a are derived from the calculated results shown in Figs. 6(a) and 6(b). The property of $BaTiO_3$ in Fig. 7(a) is in qualitatively agreement with a previous calculational result (Ricinchi et al., 2006). Figure 7(b) shows the relationship between the ratio c/a and P_3^2 . Note that $c/a - 1$ is proportional to P_3^2 with almost the same coefficients in both $SrTiO_3$ and $BaTiO_3$. Clearly, the ratio c/a is a good parameter in both tetragonal $SrTiO_3$ and $BaTiO_3$ with in-plane compressive stress. Therefore, in the following, the author uses the ratio c/a as a parameter for the investigations of the piezoelectric properties.

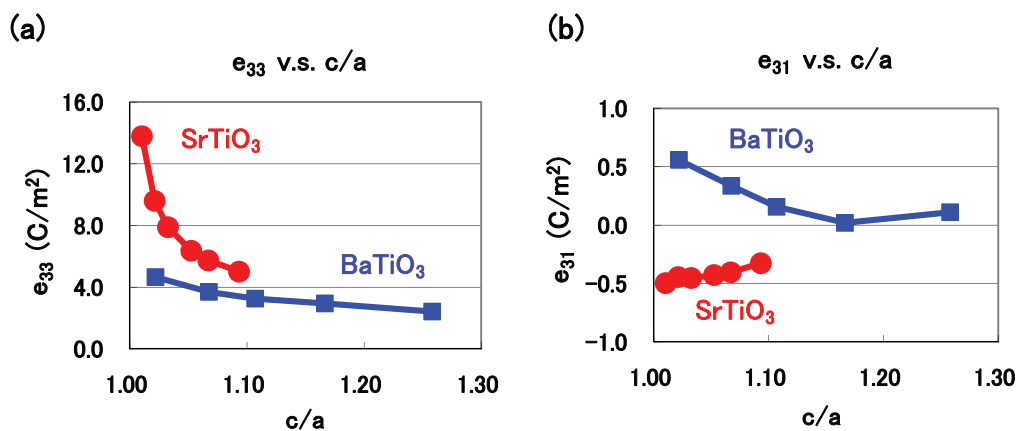


Fig. 8. Evaluated piezoelectric constants as a function of c/a ratios in optimized tetragonal $SrTiO_3$ and $BaTiO_3$: (a) e_{33} and (b) e_{31} (Furuta & Miura, 2010).

Figures 8(a) and 8(b) shows the piezoelectric properties of e_{33} and e_{31} as a function of the ratio c/a in tetragonal $SrTiO_3$ and $BaTiO_3$. The ratio c/a is optimized value as shown in Fig. 6(a) and e_{33} and e_{31} are evaluated values in their optimized structures. Note that e_{33} become larger at $c/a \approx 1$, especially in $SrTiO_3$. These properties seem to be similar to the properties around the Curie temperatures in piezoelectric ABO_3 ; Damjanovic emphasized the importance of the polarization extension as a mechanism of larger piezoelectric constants in a recent paper (Damjanovic, 2010). Contrary to e_{33} , on the other hand, the changes in e_{31} are much smaller than the changes in e_{33} , but note that e_{31} shows negative in $SrTiO_3$ while positive in $BaTiO_3$.

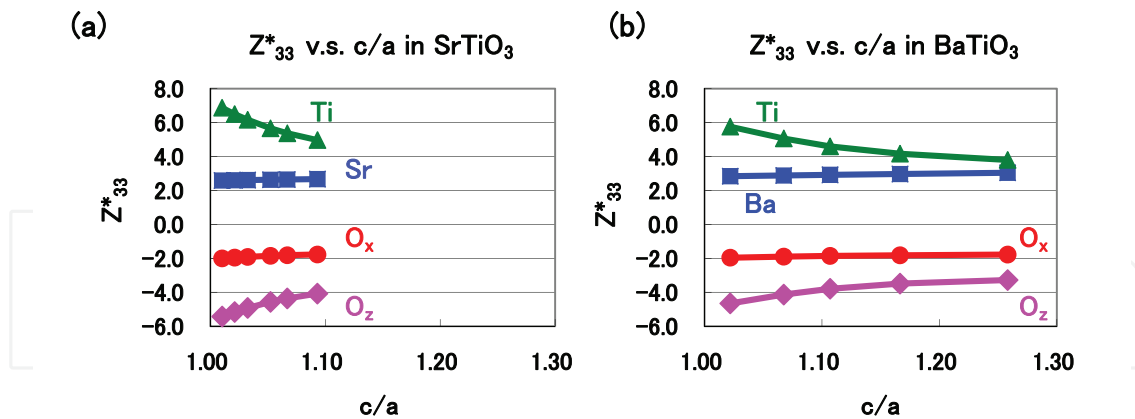


Fig. 9. Evaluated Born effective charges $Z_{33}^*(k)$ as a function of c/a ratios: (a) SrTiO_3 and (b) BaTiO_3 . O_x and O_z denote oxygen atoms along the [100] axis and the [001] axis, respectively (Furuta & Miura, 2010).

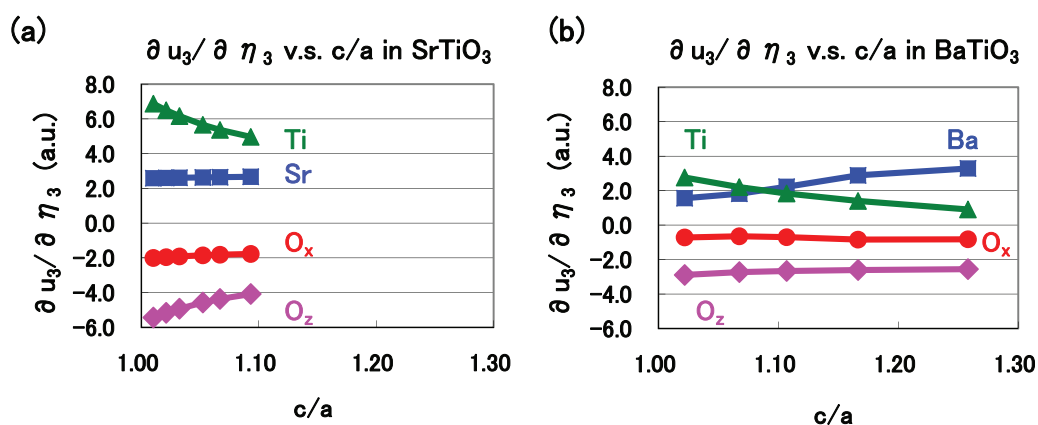


Fig. 10. Evaluated values of $\partial u_3(k) / \partial \eta_3$ as a function of c/a ratios: (a) SrTiO_3 and (b) BaTiO_3 . "a.u." denotes the atomic unit (≈ 0.53) (Furuta & Miura, 2010).

As expressed in eq. (4), e_{3j} is the sum of the contributions from the clamped term and the relaxed term. However, it has been generally known that the contribution to e_{3j} from the clamped term is much smaller than that from the relaxed term; in fact, the absolute values of the e_{33} clamped terms are less than 1 C/m^2 in both SrTiO_3 and BaTiO_3 . The author therefore investigates the contributions to the relaxed term of e_{33} and e_{31} in detail. As expressed in eq. (4), the relaxed terms of e_{3j} are proportional to the sum of the products between the $Z_{33}^*(k)$ and $\partial u_3(k) / \partial \eta_j$ ($j = 3$ or 1) values. Let us show the evaluated results of $Z_{33}^*(k)$, $\partial u_3(k) / \partial \eta_3$, and $\partial u_3(k) / \partial \eta_1$ in the following. Figures 9(a) and 9(b) show the $Z_{33}^*(k)$ values in SrTiO_3 and BaTiO_3 , respectively. Properties of the $Z_{33}^*(k)$ values are quantitatively similar in both SrTiO_3 and BaTiO_3 . Therefore, the difference in the properties of e_{33} and e_{31} between SrTiO_3 and BaTiO_3 must be due to the difference in the properties of $\partial u_3(k) / \partial \eta_j$. Figures 10(a) and 10(b) show the $\partial u_3(k) / \partial \eta_3$ values in SrTiO_3 and BaTiO_3 , respectively. In these figures, O_x and O_z denote oxygen atoms along the [100] and [001] axes, respectively, and η_3 is defined as $\eta_3 \equiv (c - c_0) / c_0$, where c_0 denotes the c lattice parameter with fully optimized structure. Clearly, the absolute values of $\partial u_3(k) / \partial \eta_3$ are different in between SrTiO_3 and BaTiO_3 . On

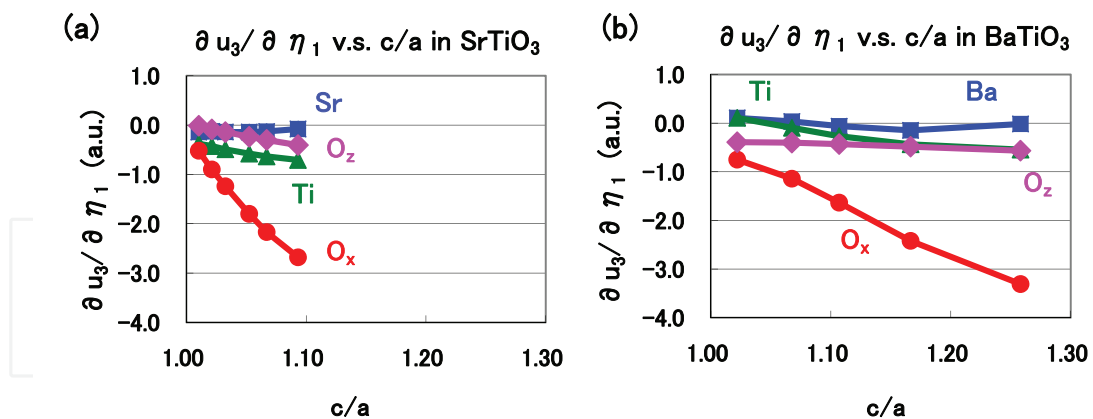


Fig. 11. Evaluated values of $\partial u_3(k)/\partial \eta_1$ as a function of c/a ratios: (a) $SrTiO_3$ and (b) $BaTiO_3$ (Furuta & Miura, 2010).

the other hand, Figs. 11(a) and 11(b) show the $\partial u_3(k)/\partial \eta_1$ values in $SrTiO_3$ and $BaTiO_3$, respectively; η_1 is defined as $\eta_1 \equiv (a - a_0)/a_0$, where a_0 denotes the a lattice parameter with fully optimized structure. The absolute values of $\partial u_3(k)/\partial \eta_1$, especially for Ti, O_x , and O_z , are different in between $SrTiO_3$ and $BaTiO_3$. As a result, the quantitative differences in e_{33} and e_{31} in between $SrTiO_3$ and $BaTiO_3$ are due to the differences in the contribution of the $\partial u_3(k)/\partial \eta_j$ values. In the following, the author would like to discuss the reasons of the quantitative differences in e_{33} and e_{31} in between $SrTiO_3$ and $BaTiO_3$.

Figure 12(a) shows the difference between the $A-O_x$ distance (R_{A-O_x}) and the sum of r_A and r_{O_x} ($r_A + r_{O_x}$) on the (100) plane as a function of the ratio c/a , where the values of the ionic radii are defined as Shannon's ones (Shannon, 1976). Note that R_{A-O_x} is smaller than $r_A + r_{O_x}$ in both $SrTiO_3$ and $BaTiO_3$. However, the difference in absolute value between R_{A-O_x} and $r_A + r_{O_x}$ in $SrTiO_3$ is much smaller than the difference in $BaTiO_3$ for $1.00 \lesssim c/a \lesssim 1.10$. This result suggests that the $Sr-O_x$ Coulomb repulsion on the (100) plane in $SrTiO_3$ is much smaller than the $Ba-O_x$ Coulomb repulsion in $BaTiO_3$ and that therefore Sr and O_x ions of $SrTiO_3$ can be displaced more easily along the [001] axis than Ba and O_x ions of $BaTiO_3$. This would be a reason why the absolute values of $\partial u_3(k)/\partial \eta_3$ of Sr and O_x ions in $SrTiO_3$ are larger than those of Ba and O_x ions in $BaTiO_3$. Figure 12(b) shows the difference between the $Ti-O_z$ distance (R_{Ti-O_z}) and $r_{Ti} + r_{O_z}$ along the [001] axis as a function of the ratio c/a . Note that R_{Ti-O_z} is smaller than $r_{Ti} + r_{O_z}$ in both $SrTiO_3$ and $BaTiO_3$. However, the difference in absolute value between R_{Ti-O_z} and $r_{Ti} + r_{O_z}$ in $SrTiO_3$ is smaller than the difference in $BaTiO_3$ for $1.00 \lesssim c/a \lesssim 1.10$. This result suggests that the $Ti-O_z$ Coulomb repulsion along the [001] axis in $SrTiO_3$ is smaller than that in $BaTiO_3$ and that therefore the Ti ion of $SrTiO_3$ can be displaced more easily along the [001] axis than that of $BaTiO_3$. This would be a reason why the absolute values of $\partial u_3(k)/\partial \eta_3$ of Ti and O_z ions in $SrTiO_3$ are larger than that in $BaTiO_3$.

In the following, the author discusses the relationship between $\partial u_3(Ti)/\partial \eta_3$ and the ratio c/a in detail. Figure 13(a) shows the properties of the differences in the total energy (ΔE_{total}) as a function of u_{Ti} . In this figure, the properties of $SrTiO_3$ with $c/a = 1.021$ ($\eta = 0.011$), $SrTiO_3$ with $c/a = 1.093$ ($\eta = 0.053$) and $BaTiO_3$ with $c/a = 1.022$ as a reference, are shown. Calculations of E_{total} were performed with the fixed crystal structures of previously optimized structures except Ti ions. Figure 13(b) shows illustrations of ΔE_{total} curves with deviations at the minimum points of the ΔE_{total} values, corresponding to the ΔE_{total} curves of $SrTiO_3$ in Fig. 13(a). Clearly, as η_3 becomes smaller, the deviated value at the minimum point of the

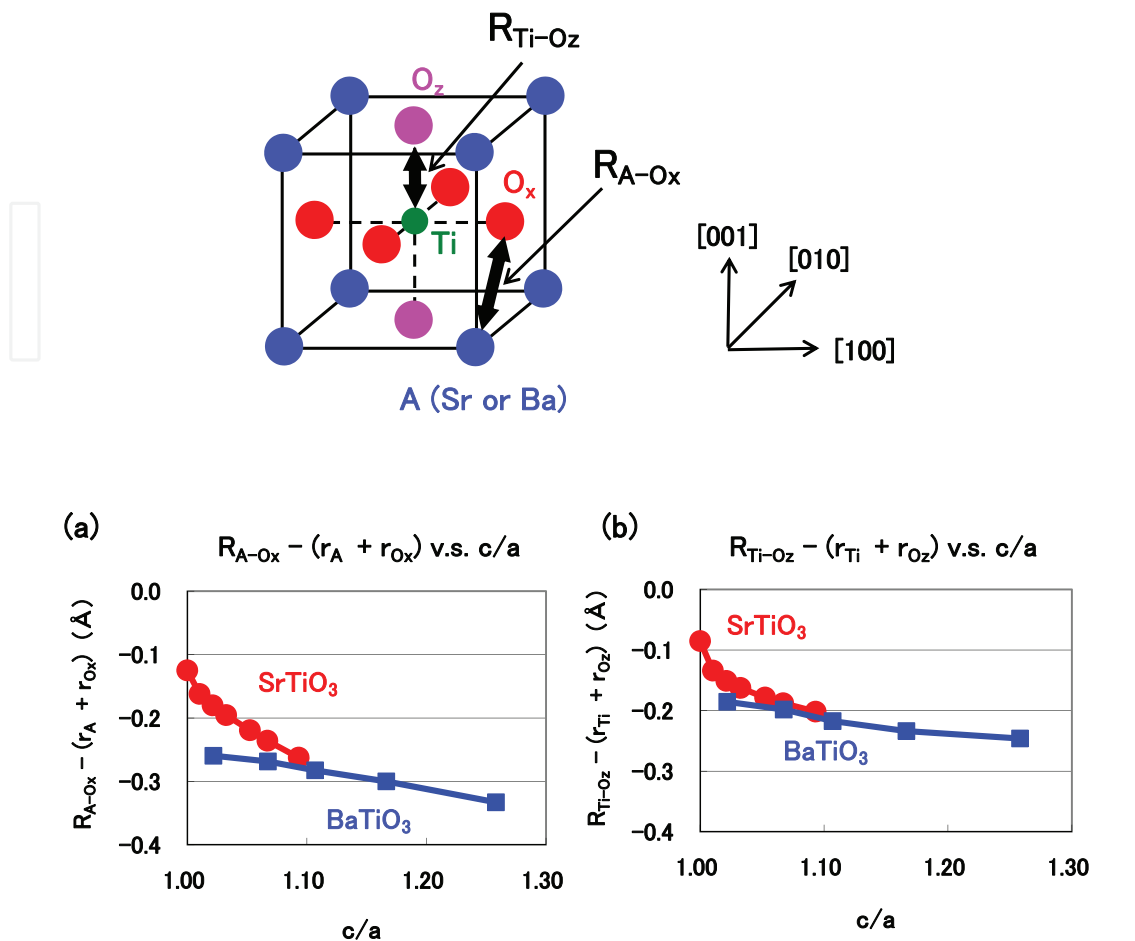


Fig. 12. Evaluated values as a function of c/a ratios in optimized tetragonal SrTiO₃ and BaTiO₃: (a) difference between the $A-O_x$ distance (R_{A-O_x}) and $r_A + r_{O_x}$, and (b) difference between the $Ti-O_z$ distance (R_{Ti-O_z}) and $r_{Ti} + r_{O_z}$, as a function of the ratio c/a . R_{A-O_x} and R_{Ti-O_z} in $ATiO_3$ are also illustrated; all the ionic radii are much larger, and A and Ti ions are displaced along the [001] axis in real $ATiO_3$ (Furuta & Miura, 2010).

ΔE_{total} values becomes smaller, i.e., the Ti ion can be displaced more favourably. On the other hand, as shown in Fig. 10(a), the absolute value of $\partial u_3(Ti)/\partial \eta_3$ becomes larger as η_3 becomes smaller. Therefore, the Ti ion can be displaced more favourably as the deviated value at the minimum point of the ΔE_{total} values becomes smaller.

Next, let us discuss quantitative properties of e_{31} , especially the reason why e_{31} in SrTiO₃ shows negative while positive in BaTiO₃. Figure 14(a) shows the difference between the $Ti-O_x$ distance (R_{Ti-O_x}) and $r_{Ti} + r_{O_x}$ along the [100] axis as a function of the ratio c/a . Note that R_{Ti-O_x} is smaller than $r_{Ti} + r_{O_x}$ in both SrTiO₃ and BaTiO₃. However, the difference in absolute value between R_{Ti-O_x} and $r_{Ti} + r_{O_x}$ in SrTiO₃ is larger than that in BaTiO₃, i.e., R_{Ti-O_x} in SrTiO₃ is smaller than R_{Ti-O_x} in BaTiO₃. This result suggests that the $Ti-O_x$ Coulomb repulsion along the [100] axis in SrTiO₃ is larger than that in BaTiO₃ and that therefore Ti and O_x ions of SrTiO₃ can be displaced along the [001] axis more easily than those of BaTiO₃, as discussed in previous subsection. This would be a reason why the absolute values of $\partial u_3(k)/\partial \eta_1$ of Ti and O_x ions in SrTiO₃ are larger than those in BaTiO₃. Therefore, each

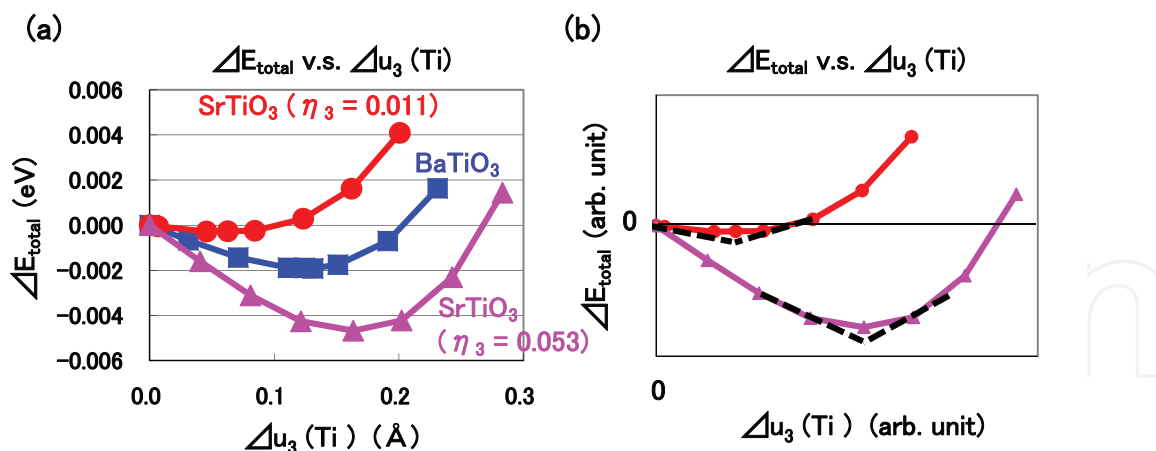


Fig. 13. (a) ΔE_{total} as a function of u_{Ti} in tetragonal SrTiO₃ and BaTiO₃. (b) Illustration of the ΔE_{total} curves in tetragonal SrTiO₃ ($\eta = 0.011$) and SrTiO₃ ($\eta = 0.053$) with deviations at the minimum point of ΔE_{total} .

absolute value of $Z_{\text{Ti}}^* \times \partial u_3(\text{Ti}) / \partial \eta_1 (< 0)$ and $Z_{\text{O}_x}^* \times \partial u_3(\text{O}_x) / \partial \eta_1 (> 0)$ in SrTiO₃ is larger than that in BaTiO₃. Figure 14(b) shows the difference between the $A-O_z$ distance (R_{A-O_z}) and $r_A + r_{O_z}$ on the (001) plane as a function of the ratio c/a . Note that R_{A-O_z} is smaller than $r_A + r_{O_z}$ in both SrTiO₃ and BaTiO₃. However, the difference in absolute value between R_{A-O_z} and $r_A + r_{O_z}$ in BaTiO₃ is larger than that in SrTiO₃. This result suggests that the Ba- O_z Coulomb repulsion on the (001) plane in BaTiO₃ is larger than that in SrTiO₃ and that therefore O_z ion of BaTiO₃ can be displaced along the [001] axis more easily than that of SrTiO₃, as discussed in previous subsection. This would be a reason why the absolute value of $\partial u_3(k) / \partial \eta_1$ of O_z ion in BaTiO₃ is larger than that in SrTiO₃. Therefore, the absolute value of $Z_{\text{O}_z}^* \times \partial u_3(\text{O}_z) / \partial \eta_1 (> 0)$ in BaTiO₃ is larger than that in SrTiO₃. Finally, as a result, the above investigations suggest that the signature of e_{31} in SrTiO₃ or BaTiO₃ is closely related to the difference in absolute values between $Z_{\text{Ti}}^* \times \partial u_3(\text{Ti}) / \partial \eta_1$ and the sum of $Z_{\text{O}_x}^* \times \partial u_3(\text{O}_x) / \partial \eta_1$ and $Z_{\text{O}_z}^* \times \partial u_3(\text{O}_z) / \partial \eta_1$.

4. Summary

Using a first-principles calculation with optimized structures, the author has investigated the role of the Coulomb repulsions between Ti 3s and 3p states and O 2s and 2p states in ferroelectric BaTiO₃. It has been found that the Coulomb repulsions between Ti 3s and 3p_{x(y)} states and O_{x(y)} 2s and 2p_{x(y)} states are closely related to the appearance of Ti ion displacement in tetragonal BaTiO₃. This mechanism seems to be consistent with the appearance of Ti ion displacement in rhombohedral BaTiO₃. The present investigation suggests that the Coulomb repulsions between Ti 3s and 3p states and O 2p states have an important role in ferroelectricity. In addition to this suggestion, the author believes that the present investigation will show a guideline for the choice of PPs when first-principles calculations with PP methods are performed. The author has also investigated the ferroelectric and piezoelectric properties of SrTiO₃ and BaTiO₃ with in-plane compressive tetragonal structures using a first-principles calculation. It has been found that the ferroelectric structure even in SrTiO₃ appears with in-plane compressive structures. The piezoelectric constant e_{33} drastically increases in SrTiO₃ rather than that in BaTiO₃ as the tetragonal ratio $c/a (> 1)$ is

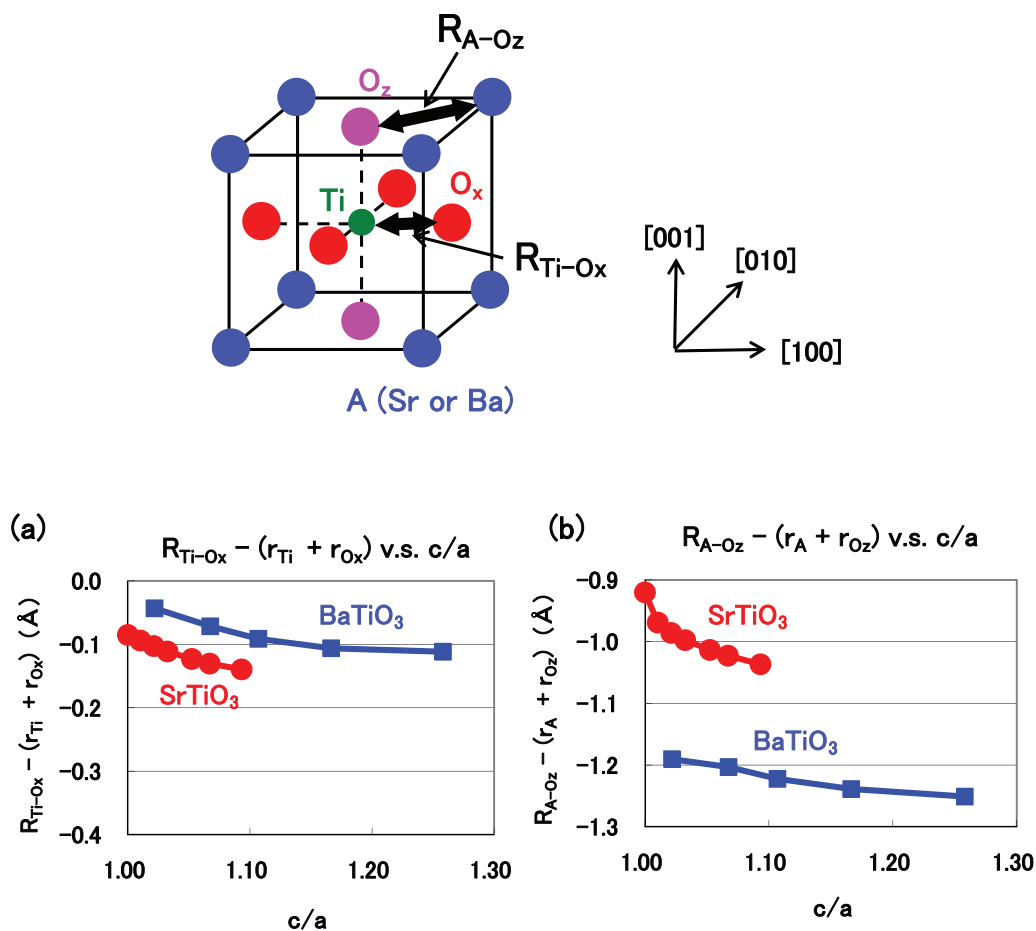


Fig. 14. Evaluated values as a function of c/a ratios in optimized tetragonal SrTiO₃ and BaTiO₃: (a) difference between the Ti-O_x distance (R_{Ti-O_x}) and $r_{Ti} + r_{O_x}$, as a function of the ratio c/a , and (b) difference between the A-O_z distance (R_{A-O_z}) and $r_A + r_{O_z}$. R_{Ti-O_x} and R_{A-O_z} in ATiO₃ are also illustrated (Furuta & Miura, 2010).

close to 1. On the other hand, e_{31} shows negative in SrTiO₃ while positive in BaTiO₃, although the changes in their absolute values are very small. The author has found that these properties of e_{33} and e_{31} in SrTiO₃ and BaTiO₃ are closely related to the ionic distances.

5. Acknowledgements

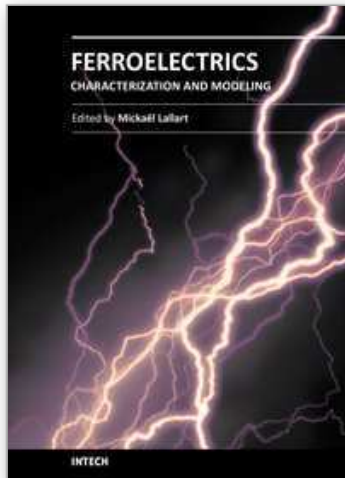
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Ferroelectric materials have been and still are widely used in many applications, that have moved from sonar towards breakthrough technologies such as memories or optical devices. This book is a part of a four volume collection (covering material aspects, physical effects, characterization and modeling, and applications) and focuses on the characterization of ferroelectric materials, including structural, electrical and multiphysic aspects, as well as innovative techniques for modeling and predicting the performance of these devices using phenomenological approaches and nonlinear methods. Hence, the aim of this book is to provide an up-to-date review of recent scientific findings and recent advances in the field of ferroelectric system characterization and modeling, allowing a deep understanding of ferroelectricity.

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