We are IntechOpen, the world’s leading publisher of Open Access books
Built by scientists, for scientists

4,200
Open access books available

116,000
International authors and editors

125M
Downloads

154
Countries delivered to

TOP 1%
Our authors are among the most cited scientists

12.2%
Contributors from top 500 universities

WEB OF SCIENCE™
Selection of our books indexed in the Book Citation Index in Web of Science™ Core Collection (BKCI)

Interested in publishing with us?
Contact book.department@intechopen.com

Numbers displayed above are based on latest data collected.
For more information visit www.intechopen.com
1. Introduction

Buildings are exposed to outside weather, which cannot remain free of water in liquid and vapour phases. “Except for structural errors, about 90% of all building construction problems are associated with water in some way” by Lieff and Trechsel (Lieff & Trechsel, 1982). Moisture problem has become one of the most important factors decreasing indoor air quality (IAQ) and limiting the building service life. Over the last decade, moisture failures in building systems have reached billions of Euros in damages in Europe, many of which involved the deterioration of sheathing panels. Research has verified the existence of health problems in relation with moisture problems. In Finland, for example, it has been reported that 38% of detached houses and 25% of apartments had notable or significant moisture problems (Haverinen, 2002). The cost of repairing moisture damage that resulted in negative health effects was estimated as € 10 000 – 40 000 per case. Therefore, the prediction and control of moisture transport in buildings are important from both technical and health points of view.

Moisture can migrate into a building in several ways, depending on vapour, liquid or ice/snow. In general, three major moisture sources can be identified: outdoors (e.g. air humidity, precipitation, moisture in the ground), the indoors (e.g. humans, water use), and wet construction materials (Rousseau, 1984). Moisture accumulation into building structures may lead to physical, biological or chemical deterioration of building materials as well as the growth of some microbial or chemical contaminations (Saltheimer, 1999; Andersson, 1997). One major problem caused by moisture is mould.

Moulds are the most typical form of fungus, which can be found anywhere. They can grow on virtually any organic substances as long as moisture and oxygen are present. Like other fungi, moulds reproduce through the production of spores. Mould spores continually waft through the air, both indoors and out-of-doors. Many types of moulds exist indoors, and almost all moulds could cause health effects (through air), depending on the type and amount of mould present as well as the sensitivity of individual experiencing mould exposure. Certain health effects, such as irritation of eyes, nose and throat, dermatitis, exacerbation of asthma, and respiratory distress, have been reported to be associated with mould exposure (Verhoeff et al., 1995; Pope et al., 1993). Other effects such as fever, flu-like symptoms, fatigue, respiratory dysfunction, excessive and regular nose bleeds, dizziness, headaches, diarrhea, vomiting, liver damage, and impaired or altered inhalation have been
identified in persons who have been exposed to mould (Croft et al., 1986; Jarvis, 1995; Smith & Moss, 1985). Some moulds even produce toxins (mycotoxins) (Jarvis, 1990; Burge, 1986; Yang, 1995).

Indoor mould was reported worldwide. A series of studies conducted in European countries, Canada and the United States showed that at least 20% of buildings had one or more signs of visible mould growth indoors on walls, floors or ceilings (Institute of Medicine, 2004). Similar reports also come from other areas of the world. A survey in rural Taiwan and China showed that 30.1% of visited people reported the presence of visible mould inside their houses (Yang et al., 1997). In a study of 98 houses in Japan, 15.6% was reported to have visible mould (Saigo et al., 2004). In another study in three China cities (Beijing, Guangzhou and Hong Kong), about 11% of parents of 10,902 schoolchildren reported visible mould on the ceilings and walls (Wong et al., 2004). Indoor mould was also reported to occur in school buildings, day-care centres, offices and other buildings (Mudarri & Fisk, 2007).

Excessive moisture is generally the cause of mould growth. Relevant experiments were committed to study the lowest moisture level for mould growth. Adan (Adan, 1994) found that moulds don’t grow below a relative humidity of 80%. In Viitanen and Ritschkoff’s work (Viitanen & Ritschkoff, 1991), they suggested relative humidity should be kept below 75% within a temperature range of 5-40 °C to avoid mould growth. This result was confirmed by Rowan et al. (Rowan et al., 1999). In a more detailed review work, Johansson et al. (Johansson et al., 2005) described that critical moisture conditions for mould growth were 75-90% for clean materials and 75-80% for contaminated or solid materials (Table 1).

<table>
<thead>
<tr>
<th>Building material group</th>
<th>Relative humidity (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Wood and wood-based materials</td>
<td>75-80</td>
</tr>
<tr>
<td>Paper on plasterboard</td>
<td>80-85</td>
</tr>
<tr>
<td>Mineral insulation materials</td>
<td>90-95</td>
</tr>
<tr>
<td>Extruded and expanded polystyrene</td>
<td>90-95</td>
</tr>
<tr>
<td>Concrete</td>
<td>90-95</td>
</tr>
</tbody>
</table>

Source: Johansson et al. (2005)

Table 1. Critical relative humidity for various groups of materials.

Therefore, indoor moisture becomes the major factor on the presence of mould. Indoor moisture was also linked to the growth of Bacteria (Heinz & Mark, 2009). Hence, control of indoor moisture level becomes essential concerning IAQ. It is not uncommon in some climates to have moisture loads in excess of over 20 kg per day (Kerestecioglu & Gu, 1990). The load mainly comes from indoor activities like occupants, washing and cooking etc. In residential buildings, the largest single moisture load is from people’s respiration and perspiration.

However, methods of evaluating indoor moisture generation rates in buildings are generally lacking. The difficulty lies on the fact that the moisture generation rate has no clear relationship with the number of occupants. Factors like cleaning and plants have big effect (Hite & Bray, 1948). Large background contributions from the foundation and soil have been reported (TenWolde, 1994). Typically, a trial-and-error method is adopted in evaluating the indoor moisture generation rate in calculating building heat and moisture transfer. Values of
indoor moisture generation rate are adjusted in comparing the measured and the calculated moisture contents. The final selected value is based on the minimum difference of the moisture contents between the measured and the calculated. TenWolde (TenWolde, 1994) used this method and the mathematical model developed by the same author to analyse the indoor moisture generation rates for six manufactured houses during winter. Houses were occupied by one to two persons in each house and dimensions were varying from 4.3 × 20.1 to 4.9 × 23.2 m². The estimated average values of moisture generation rates were $32 \times 10^{-6}$ to $75 \times 10^{-6}$ kg s$^{-1}$ per person. Very often, an experimental value is used.

In this chapter, a mathematical method in predicting indoor moisture generation rate is developed. The method is based on a series of measured indoor moisture contents. Using a Stirling interpolation fitting of the measured indoor moisture contents, the time-dependent indoor moisture generation rate can be determined. The moisture generation pattern can be obtained thereafter. The developed method provides an easy and concise way of determining indoor moisture generation levels, hence can be served as a useful tool in predicting building heat and moisture transfer.

This chapter is trying to accomplish two objectives. The first is to apply the mathematical method to predict the indoor moisture generation rate for a real test house. Results are analysed by the heat and moisture transfer model developed by Lu (Lu, 2002; Viljanen et al., 1999). With this model, the validation of the proposed mathematical method in deriving indoor moisture generation rate is studied. The second objective is to study the effect of indoor moisture generation patterns on the indoor moisture level using the developed heat and moisture transfer model.

The chapter is organised as follows: Following the introduction is a brief description of overall heat and moisture transfer model equations for the building system. The mathematical method used in predicting indoor moisture generation rate is given in details after the heat and moisture transfer model description. The validation of the developed model is conducted for a real test house. Finally, simulation results are presented, which mainly involve the study of the effect on indoor moisture behaviour of different moisture generation patterns.

2. Model equations for a building system

A building system is divided into building envelopes such as walls, roof, floor, foundation etc and building indoor air. The modelling work can be generalised as following main steps: 1) developing heat and moisture transfer model equations for building envelopes; 2) developing heat and moisture transfer model equations for indoor air and 3) numerically solving the system equations for building envelopes and indoor air at any time with outdoor conditions expressed as boundary conditions. Hence the transient temperature and moisture variations can be obtained for a building system under outdoor conditions. A complete heat and moisture transfer model for a building system is described by Lu in (Lu & Viljanen, 2000; Viljanen et al., 1999).

2.1 Model equations for building envelopes

The fundamentals of heat and moisture transfer in porous media (building envelopes) can be found in pioneering papers by Philip and DeVries (Philip & DeVries, 1957) and Whitaker (Whitaker, 1977). In modelling heat and moisture transfer in building porous materials,
Whitaker’s REV method (Whitaker, 1977) is adopted. The general approach is to start with conservation equations, constitutive equations and state equations by means of the thermodynamics of the Gibbs relation. The conservation equations include the mass, the momentum and the energy conservation equations. In writing the heat and moisture transfer model equations for building envelopes, simplifications have been made. These include:

i. In considering moisture transfer for building envelopes, convection effect is not included. Moisture transfer is described as Fick’s generalised diffusion equation with water vapour concentration as a driving potential. This is justified by Liesen and Pedersen (Liesen & Pedersen, 1999) for example. However, in the case of existence of liquid phase, the transport of liquid by Darcy’s law can be taken into account.

ii. Local thermodynamic equilibrium is assumed at every point of the material.

iii. For all moisture transport coefficients, any hysteresis effect is not included.

iv. The flux of heat or moisture at the interface of contacted materials has a continuous property.

v. Heat and moisture transfer equations are limited to one-dimensional for building walls and roof and two-dimensional for building floor, foundation and soil.

vi. Soil is a homogeneous material.

vii. At a depth of 5 m of the soil ground, the temperature is constant equal to 5°C. At certain depths, the relative humidity of soil is 100%.

Having the above assumptions the heat and moisture transfer equations for different components of building envelopes can be written down. For example, for building walls, we have:

\[
\rho_w C_w \frac{\partial T_w}{\partial t} = \frac{\partial}{\partial x} (\gamma_w \frac{\partial T_w}{\partial x}),
\]

(1)

\[
\frac{\partial c_w}{\partial t} = \frac{\partial}{\partial x} (D_w \frac{\partial c_w}{\partial x}).
\]

(2)

**Boundary condition:** The interfaces between layers are treated separately and the conditions of continuity assumption (iv) are applied. Thus we have for example:

\[
\lambda_w \frac{\partial T_w}{\partial x} \bigg|_{\text{interface}} = \lambda_w \frac{\partial T_w}{\partial x} \bigg|_{\text{interface}},
\]

(3)

\[
T_w \bigg|_{1 \text{interface}} = T_w \bigg|_{2 \text{interface}},
\]

(4)

\[
D_w \frac{\partial c_w}{\partial x} \bigg|_{\text{interface}} = D_w \frac{\partial c_w}{\partial x} \bigg|_{\text{interface}},
\]

(5)

\[
c_w \bigg|_{1 \text{interface}} = c_w \bigg|_{2 \text{interface}}.
\]

(6)

For surfaces exposed to the outdoor and indoor air, we have for example:

\[
\lambda_w \frac{\partial T_w}{\partial x} \bigg|_{\text{surface,out}} = h_{T, w} \big( T_{\text{out}} - T_w \big) + q_w
\]

(7)
Moisture and Estimation of Moisture Generation Rate

$$D_w \frac{\partial c_{w}}{\partial x} \bigg|_{\text{surface,out}} = h_{m,w}^{out} (c_{out} - c_{w} \bigg|_{\text{surface,out}})$$  (8)

and

$$\lambda_w \frac{\partial T_w}{\partial x} \bigg|_{\text{surface,in}} = h_{m,w}^{in} (T_w - T_{in})$$  (9)

$$D_w \frac{\partial c_{w}}{\partial x} \bigg|_{\text{surface,in}} = h_{m,w}^{in} (c_{w} \bigg|_{\text{surface,in}} - c_{in})$$  (10)

where $q_w$ is the solar energy received by the exterior wall surface. Empirical values of the surface heat and moisture transfer coefficients, $h_{m,w}^{out}$ and $h_{m,w}^{in}$, are taken from RIL 117 (RIL 117, 1979). Lewis relation can be used to determine $h_{m,w}^{out}$ and $h_{m,w}^{in}$. Currently, raining effect is not included.

Similar equations of Eqs. (1)–(10) for building floor, foundation and soil are given with two-dimensional. In writing the boundary conditions, the heat and moisture fluxes normal to the boundary surfaces which are selected as far as possible from the interest building are assumed to be 0 in soil ground. Assumption (vii) is also employed. We are not going to address the equations here for space limitation. More details can be referred to Viljanen et al. (Viljanen et al., 1999).

For initial conditions for building envelopes, the temperature or the relative humidity is assumed at the steady state with indoor and outdoor temperatures or relative humidity. For soil, the initial temperature distribution is treated differently accounting for its big thermal capacity (Viljanen et al., 1999).

### 2.2 Model equations for building indoor air

The following physical condition is assumed for building indoor air:

viii. Indoor air is well mixed. Indoor temperature and moisture content are uniformly distributed.

The well-mixed indoor air model is generally not valid, however, the resultant error may be negligible depending on the model’s application. For a normal residential house for example, the effect of the indoor air flow on the indoor temperature and moisture level is normally small if the ventilation rate is not very big. Hence a well-mix indoor air model is a good approximation of the practical situation.

The heat and moisture balance equations therefore can be written in the following forms:

$$V \rho_n c_{p}^{in} \frac{dT_{in}}{dt} = nV \rho_n c_{p}^{in} (T_{out} - T_{in}) + \Sigma Q_v$$  (11)

$$V \frac{dc_{in}}{dt} = nV (c_{out} - c_{in}) + G + \Sigma M_v$$  (12)

where $\Sigma Q_v$ is the sum of heat transfer rates between building envelopes and indoor air (W), $\Sigma M_v$ is the sum of moisture transfer rates between building envelopes and indoor air (kg s$^{-1}$) and $G$ is the indoor moisture generation rate (kg s$^{-1}$).
To have a closed system of heat and moisture equations for building systems, all material property data have to be taken into account. These data are taken from RIL 117 (RIL 117, 1979), some of which are based on the experimental fittings (Viljanen et al., 1999). Moreover, the time-dependent indoor moisture generation rate G has to be given in order to solve the equations. A mathematical method of calculating G is given in the following section. The model partial differential equations, Eqs. (1)–(12), are discretized in space by the finite difference method. The resultant ordinary differential equations are discretized in time by the Crank-Nicolson scheme. The final algebraic equations are solved by the Newton iteration method. Transient temperatures and moisture contents for building envelopes and indoor air are then solved at any time under outdoor climatic conditions.

3. Calculation of indoor moisture generation rate

Eq. (12) gives the moisture generation rate as:

$$G = V \frac{dc_{in}}{dt} - nV(c_{out} - c_{in}) - \sum M_{i}.$$  \hspace{1cm} (13)

To deduce G, the derivative of indoor moisture content $c_{in}$ versus time, $\frac{dc_{in}}{dt}$, is needed. However, direct differentiation of the indoor moisture contents can be unstable even though the data show smooth and continuous properties. The moisture generation rate increases exponentially when the moisture source releases the moisture and decreases exponentially after the source stops the release. Bennett et al. (Bennett et al., 1996) developed an approach in estimating emission rate from concentration data for formaldehyde measurement. A Stirling interpolation polynomial fitting was used in constructing the derivatives of contaminant concentrations. Applying this idea, indoor moisture contents $c_{in}$ are interpolated by a Stirling polynomial, the derivatives can therefore be obtained by simply differentiating the smooth continuous polynomial. Stirling interpolation polynomial is based on the average of the backward and forward Gauss interpolation polynomials. It uses a diagonal difference table with three successive points. It is a symmetrical approximation for the given values. Relevant formulas are shown in the appendix. Similarly, a Bessel interpolation polynomial can be used also. It is based on a diagonal difference table and uses four points. It is able to interpolate with data that are not evenly spaced apart. More details can be seen in Kunz (Kunz, 1957).

Another unknown value presented in Eq. (13) is the time-dependent moisture transfer rate $\sum M_{i}$ between building envelopes and indoor air. In deriving the indoor moisture generation rate G, it is customarily assumed that $\sum M_{i}$ is 0, for example in Bennett et al. (Bennett et al., 1996). However, it may affect the calculation accuracy. We propose two different methods in calculating $\sum M_{i}$ here, namely the explicit and the numerical methods.

For the explicit method, we assume a steady-state condition in Eq. (13) and ignore the thermal lag between the envelopes and indoor air, so the moisture transfer rate M for any building envelope can be approximated as

$$M = A\delta(c_{out} - c_{in}).$$  \hspace{1cm} (14)

where A and $\delta$ are the area and the overall moisture transfer coefficient of the building envelope respectively.
The implication behind the approximation Eq. (14) is that the moisture profile of the building envelope is given by a linear combination of \(c_{\text{out}}\) and \(c_{\text{in}}\). For a thin, uniform construction material, the method can give a good estimation. However, for a general situation, Eq. (14) gives a poor estimation. One way of modifying it is to introduce more interpolation nodes for example \(c_{\text{out}}, c_1, \ldots, c_n, c_{\text{in}}\). The Laplace transform can be used and Eq. (14) is reduced to a first order time lag corresponding to \(c_{\text{out}}\) and \(c_{\text{in}}\). As it involves tedious basic mathematical manipulations, details are skipped here. More information can be found in Underwood (Underwood, 1999), where an approximated heat conduction equation was studied. It can be applied to moisture transfer equation.

For the numerical method, the developed program is adopted to predict \(\Sigma M_i\) at any time.

One difficulty is that in calculating \(\Sigma M_i\), the time-dependent moisture generation rate \(G\) is needed. Values of \(G\) can be approximated first by assuming \(\Sigma M_i = 0\).

### 3.1 Model validation criteria

The Normalized Mean Squared Error (NMSE) and the Correlation Coefficient \((r)\) are accepted as two key criteria to evaluate the fit to the identification data.

\[
\text{NMSE} = \frac{\sum_{i=1}^{N} (\bar{x}_i - x_i)^2}{\sum_{i=1}^{N} (\bar{x}_i)^2}
\]

\[
r = \frac{N \sum_{i=1}^{N} z_i y_i - \sum_{i=1}^{N} z_i \sum_{i=1}^{N} y_i}{\sqrt{(N \sum_{i=1}^{N} z_i^2 - (\sum_{i=1}^{N} z_i)^2)(N \sum_{i=1}^{N} y_i^2 - (\sum_{i=1}^{N} y_i)^2)}}
\]

where \(x_i\) and \(\bar{x}_i\) are predicted value and the mean of measured ones \((x_i)\) respectively, \(N\) is the number of samples, \(z_i\) and \(y_i\) are samples. By definition, the minimum of NMSE is zero, indicating the exact match between actual and estimated values. The higher NMSE, the worse is our estimation. The value of \(r\) is such that \(-1 < r < +1\), where + and - signs are used for positive linear correlations and negative linear correlations, respectively. An \(r\) value of exactly +1 indicates a perfect positive fit while -1 means a perfect negative fit.

### 4. Simulation results and discussion

#### 4.1 Validation of the heat and moisture transfer model

In order to apply the proposed mathematical method in predicting indoor moisture generation rate, a comparison of calculated indoor moisture content using the heat and moisture transfer model described in the last section with available measurement data for a test house without occupants was done. The result is shown in Fig. 1. In the simulation process, as the time-dependent ventilation rate was not measured, a fitted value of \(n = 0.3\ \text{h}^{-1} = 8.3 \times 10^{-5}\ \text{s}^{-1}\) was used. It can be seen that good agreement is obtained with \(\text{NMSE} = 0.44\) and \(r = 0.81\). The relative difference between the calculated and the measured data is less than 10%.
4.2 Validation of the indoor moisture generation rate model

To perform a validation of the proposed mathematical method in predicting indoor moisture generation rate, we measured a series of indoor temperatures and moisture contents for a real test house. The measurement period was from 24th of November to 2nd of December 1998 and the average ventilation rate was measured as $0.4 \text{ h}^{-1} = 1.1 \times 10^4 \text{ s}^{-1}$. The test house is a one-storey detached house, a massive log house, with a dimension $7.6 \times 14.3 \times 2.5 \text{ m}^3$ located near Helsinki of Finland (Lehtinen et al., 1998). The floor area is about $110 \text{ m}^2$. The inner and outer walls, roof and floor are mainly composed of wood, mineral wool and concrete with thickness 200, 300 and 120 mm, separately. A schematic picture of the house dimensions and constructions is given in Figs. 2 and 3. The house was occupied by a family with two adults and a baby.

As reference figures, Figs. 4 and 5 display a comparison between the calculated and the measured indoor moisture contents and relative humidity. Indoor moisture generation rate was assumed to be 0. The measured indoor temperatures were used in the calculation, see Fig. 6. It can be seen that the calculated levels of indoor moisture contents and relative humidity are lower than those of the measured data. Indoor moisture generation rate has to be taken into account.

Table 2 lists some of the measurement data including outdoor and indoor moisture contents. The last column presents the calculated indoor moisture generation rate per unit volume using the method described in the previous section, see the appendix. Here we assume that the moisture transfer rate between building envelopes and indoor air is 0, i.e. $\Sigma M_i = 0$. 

---

Fig. 1. Comparison between calculated and measured indoor moisture contents. Validation of the heat and moisture transfer model.

![Graph showing calculated and measured indoor moisture contents](image-url)
Fig. 2. Layout of cross-section view of the test house.

Fig. 3. Schematic picture of the constructions of the test house.
Fig. 4. Comparison between calculated and measured indoor moisture contents for the test house. Indoor moisture generation rate is assumed to be 0.

Fig. 5. Comparison between calculated and measured indoor relative humidity for the test house. Indoor moisture generation rate is assumed to be 0.
Fig. 6. Measured indoor and outdoor temperatures for the test house.

Fig. 7. Measured indoor moisture contents and calculated indoor moisture generation rate for the test house.
Fig. 7 shows the measured indoor moisture content and the calculated time-dependent indoor moisture generation rate for the test house. It can be seen that the trend of indoor moisture generation rate very much follows that of the indoor moisture contents. The rate values vary from 0 to 2.6 gm⁻³ h⁻¹ = 196 × 10⁻⁶ kg s⁻¹. And the average rate value is 0.76 gm⁻³ h⁻¹ = 57 × 10⁻⁶ kg s⁻¹. These values fall within the range of moisture generation rate reported by other researchers. For example, TenWold (TenWold, 1994) estimated the moisture generation rate in one- to two-person house between 63×10⁻⁶ kgs⁻¹ and 75×10⁻⁶ kgs⁻¹in winter period.

<table>
<thead>
<tr>
<th>Time (24th, Nov.)</th>
<th>c_in (gm⁻³)</th>
<th>dc_in/dt (gm⁻³ h⁻¹)</th>
<th>c_out (gm⁻³)</th>
<th>n(c_out-c_in) (gm⁻³ h⁻¹)</th>
<th>G/V (gm⁻³ h⁻¹)</th>
</tr>
</thead>
<tbody>
<tr>
<td>12:00 am</td>
<td>5.67</td>
<td>0.2040</td>
<td>3.7521</td>
<td>-0.7672</td>
<td>0.9712</td>
</tr>
<tr>
<td>12:30 am</td>
<td>5.43</td>
<td>-0.5027</td>
<td>3.7260</td>
<td>-0.6816</td>
<td>0.1788</td>
</tr>
<tr>
<td>01:00 am</td>
<td>5.34</td>
<td>-0.0360</td>
<td>3.7096</td>
<td>-0.65214</td>
<td>0.6161</td>
</tr>
<tr>
<td>01:30 am</td>
<td>5.34</td>
<td>0.0160</td>
<td>3.7336</td>
<td>-0.6426</td>
<td>0.6886</td>
</tr>
<tr>
<td>02:00 am</td>
<td>5.34</td>
<td>0</td>
<td>3.7579</td>
<td>-0.6329</td>
<td>0.6329</td>
</tr>
<tr>
<td>02:30 am</td>
<td>5.34</td>
<td>-0.0270</td>
<td>3.7774</td>
<td>-0.6264</td>
<td>0.5994</td>
</tr>
<tr>
<td>03:00 am</td>
<td>5.34</td>
<td>0.1350</td>
<td>3.7839</td>
<td>-0.6224</td>
<td>0.7575</td>
</tr>
<tr>
<td>03:30 am</td>
<td>5.43</td>
<td>0</td>
<td>3.7695</td>
<td>-0.6642</td>
<td>0.6642</td>
</tr>
<tr>
<td>04:00 am</td>
<td>5.34</td>
<td>-0.1350</td>
<td>3.7474</td>
<td>-0.6370</td>
<td>0.5020</td>
</tr>
<tr>
<td>04:30 am</td>
<td>5.34</td>
<td>0.0270</td>
<td>3.7226</td>
<td>-0.6470</td>
<td>0.6740</td>
</tr>
</tbody>
</table>

Table 2. Measured indoor moisture contents and calculated indoor moisture generation rate.

Fig. 8. Comparison between calculated and measured indoor moisture contents for the test house. Time-dependent moisture generation rate in Fig. 7 is applied.
Fig. 9. Comparison between calculated and measured indoor relative humidity for the test house. Time-dependent moisture generation rate in Fig. 7 is applied.

From the obtained time-dependent indoor moisture generation rate in Fig. 7 we can see that the moisture generation pattern consists of different peaks, which are coincident with occupants' activities. Applying the result in Fig. 7, Figs. 8 and 9 present the results of the comparison between the measured and the calculated indoor moisture contents and relative humidity. Table 3 lists the model performances for results (Figs. 8 and 9). Good agreement is obtained.

<table>
<thead>
<tr>
<th>Model</th>
<th>Normalized Mean Squared Error (NMSE)</th>
<th>Correlation Coefficient (r)</th>
<th>(\frac{\text{calculated} - \text{measured}}{\text{measured}})</th>
</tr>
</thead>
<tbody>
<tr>
<td>Calculated indoor moisture content vs. measured indoor moisture content (Fig. 8)</td>
<td>0.71</td>
<td>0.55</td>
<td>Maximum = 15%; Average = 5%;</td>
</tr>
<tr>
<td>Calculated indoor relative humidity vs. measured indoor relative humidity (Fig. 9)</td>
<td>0.38</td>
<td>0.83</td>
<td>Maximum = 15%; Average = 6%;</td>
</tr>
</tbody>
</table>

\(\text{a The range of errors between calculated and measured.}\)

Table 3. Model performances between measured indoor moisture content and calculated indoor moisture generation rate.
It is worth noting that the moisture generation rate in Fig. 7 was obtained by assuming the moisture transfer rate $\Sigma M_i = 0$. It seems this assumption influences the model accuracy in calculating indoor moisture content, which gives relatively low Correlation Coefficient ($r=0.55$). But, the error range is small and satisfactory (last column in Table 3). Using the program and the information of Fig. 7 we have calculated the moisture transfer rate per unit area $\sum \frac{M_i}{\sum A_i}$. Values vary from $0.02 \times 10^{-9}$ kg m$^{-2}$ s$^{-1}$ to $0.13 \times 10^{-6}$ kg m$^{-2}$ s$^{-1}$. The average value is $0.03 \times 10^{-6}$ kg m$^{-2}$ s$^{-1}$. Considering the magnitude of the moisture transfer rate, it is neglected in deducing the moisture generation rate. Calculations would not make any principle difference if the effect of moisture transfer rate were taken into account. TenWolde (TenWolde, 1994) used a moisture transfer rate of $0.068 \times 10^{-6}$ kg m$^{-2}$ s$^{-1}$ to match the calculated and the measured indoor relative humidity.

One interesting phenomenon is that the model gives very good agreement for indoor relative humidity (Table 3). As mentioned earlier, the model has assumed that the heat transfer rates between building envelope and indoor air were assumed as zero ($\Sigma Q_i$, Eq. (11)). This assumption may have effects on model accuracy of both indoor temperature and moisture content estimates which is beyond statistical explanation. This guess is further proved by the following simulations (Section 4.3).

In the following, a number of simulations are conducted for the test house shown in Figs. 2 and 3. These calculations are concerned with the study of the effect on indoor moisture contents of different moisture generation rate patterns.

### 4.3 Effect of moisture generation rate patterns

Consider a varied moisture generation pattern shown in Fig. 7 and a constant moisture generation pattern. Figs. 10 and 11 present the calculated indoor moisture contents and relative humidity. For the constant moisture generation pattern, the rate value of $57 \times 10^{-6}$ kg s$^{-1}$ is assumed, which is predicted for the test house as an average rate value. It is observed that the indoor moisture content with the constant moisture generation rate is an average curve of that with the varied moisture generation rate in Fig. 10. Moreover, the difference is so small that it can be neglected. This conclusion is applicable to the indoor relative humidity in Fig. 11.

Next, assume that the test house is a commercial house with occupant activities existing only for certain working hours, for example from 9:00 a.m. to 5:00 p.m. for 8 hours. The moisture generation rate is assumed to be $171 \times 10^{-6}$ kg s$^{-1}$ during the working hours and 0 otherwise, which has a periodic pulse pattern. Note that the daily average moisture generation rate is still $57 \times 10^{-6}$ kg s$^{-1}$ as in Figs. 10 and 11. Figs. 12 and 13 show the comparison of the indoor moisture contents with these two different moisture generation rate patterns. Table 4 illustrates model performances. The difference is within a very small range, especially for indoor relative humidity.

Model performances are excellent in indoor relative humidity estimation. Results also show consistency with ones in Section 4.2, which evidences our guess. Neglecting moisture transfer between building envelope and indoor air can affect the model accuracy in calculating indoor moisture content, but the impact is limited and very small normally (Section 4.2). As such, the model may give relatively poor agreement for indoor moisture content which may go beyond statistics, such as Correlation Coefficient, but in general
errors are small and acceptable (last columns in Tables 3 and 4). Furthermore, note that a relationship between two variables must be approximately linear when applying Correlation Coefficient. When the assumption of linearity is violated, the correlation will underestimate the strength of the relationship. In addition, the developed model in this

<table>
<thead>
<tr>
<th>Model</th>
<th>Normalized Mean Squared Error (NMSE)</th>
<th>Correlation Coefficient (r)</th>
<th>Maximum</th>
<th>Average</th>
</tr>
</thead>
<tbody>
<tr>
<td>Constant moisture generation rate vs. time-dependent moisture generation rate (indoor moisture content, Fig. 10)</td>
<td>0.74</td>
<td>0.54</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Constant moisture generation rate vs. time-dependent moisture generation rate (indoor relative humidity, Fig. 11)</td>
<td>0.12</td>
<td>0.94</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Moisture generation rate with constant pattern vs. Moisture generation rate with periodic pulse pattern (indoor moisture content, Fig. 12)</td>
<td>0.69</td>
<td>0.56</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Moisture generation rate with constant pattern vs. Moisture generation rate with periodic pulse pattern (indoor relative humidity, Fig. 13)</td>
<td>0.14</td>
<td>0.93</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

*a* The range of errors between simulated and target.

Table 4. Model performances for the effect of moisture generation rate patterns
Fig. 10. Comparison of the effect on indoor moisture contents of different moisture generation patterns for the test house. Constant moisture generation rate and time-dependent moisture generation rate in Fig. 7 are applied.

Fig. 11. Comparison of the effect on indoor relative humidity of different moisture generation patterns for the test house. Constant moisture generation rate and time-dependent moisture generation rate in Fig. 7 are applied.
Fig. 12. Comparison of the effect on indoor moisture contents of different moisture generation patterns for the test house. Moisture generation rates with constant and periodic pulse patterns are applied.

Fig. 13. Comparison of the effect on indoor relative humidity of different moisture generation patterns for the test house. Moisture generation rates with constant and periodic pulse patterns are applied.
paper (e.g. Eq. (13)) is physically verified in many related works (Lu, 2002). In this study, the differences between simulated and measurements are all in small margins (last columns in Tables 3 and 4), which further verify the model's usefulness in practice. This is an interesting result as it can greatly simplify the calculation procedure. Note that any moisture generation pattern function can be approximated by a combination of periodic pulse functions, so the result actually implies that a constant moisture generation rate pattern is always 'enough' in calculating the indoor moisture content, especially in deciding indoor moisture level.

It is worth mentioning that Isetti et al. (Isetti et al., 1988) studied the effect on indoor relative humidity of three periodic pulse types of moisture generation patterns with different numbers of occupants in an office room. A similar result was obtained. A constant moisture generation pattern was not included in their paper.

5. Conclusion

The importance of the effect of the indoor moisture generation rate on accurately predicting moisture content for a building system has been demonstrated. Hence in studying the heat and moisture transfer for a building system, a method of precisely calculating indoor moisture generation rate is needed. To address the problem, this chapter proposes a mathematical method to derive time-dependent moisture generation rate function from a series of measured indoor moisture contents. The method incorporates the developed heat and moisture transfer model to calculate transient temperatures and moisture contents for building envelopes and indoor air exposed to any outdoor climatic conditions. The model is validated by a real test house. The effect on indoor moisture level of different moisture generation patterns is also investigated.

Through simulation results, we can draw the following main conclusions:

- The performance of indoor moisture generation rate has a big effect on indoor moisture level. In conducting the simulation work, this aspect has to be considered.
- Given a series of measured indoor moisture contents, it is possible to calculate time-dependent moisture generation rate using the method proposed in this chapter.
- A constant moisture generation rate model is generally not valid, but the resultant error may be negligible. This has important implication for simplifying a simulation procedure.

Finally, it is stressed that the present model is based on the condition of well-mixed indoor air moisture from the moisture sources. For some special cases especially right after the moisture release from a big moisture release source, special attention must be paid. Moreover, for a heavy moisture content room like sauna or bathroom, the effect of different moisture generation rate patterns may be too big to be neglected.

6. Acknowledgement

This research was supported by the Finnish Academy.

7. Appendix

Table 5 presents a difference table used in interpolating a series of measured data by a Stirling polynomial.
Moisture and Estimation of Moisture Generation Rate

With equal space \( h \), at point \( x = x_0 \), the approximation of the derivative of Stirling polynomial is given as (p127, Kunz, 1957):

\[
\left[ \frac{dy}{dx} \right]_{x=x_0} = \frac{1}{h} \left( \frac{\Delta y_{-1} + \Delta y_0}{2} + \frac{1}{6} \frac{\Delta^3 y_{-2} + \Delta^3 y_{-1} + 1}{2} \frac{\Delta^5 y_{-3} + \Delta^5 y_{-2}}{2} + \ldots \right). \tag{A.1}
\]

Applying the above formula Eq. (A.1) to the indoor moisture content we get

\[
\left[ \frac{dc_{in}}{dt} \right]_{t=t_0} = \frac{1}{\Delta t} \left( \frac{\Delta c_{in,-1} + \Delta c_{in,0}}{2} + \frac{1}{6} \frac{\Delta^3 c_{in,-2} + \Delta^3 c_{in,-1} + 1}{2} \frac{\Delta^5 c_{in,-3} + \Delta^5 c_{in,-2}}{2} + \ldots \right). \tag{A.2}
\]

Take Table 5 as an example, Eq. (A.2) gives the following result at time 2:30 am:

\[
\left[ \frac{dc_{in}}{dt} \right]_{2:30am} = \frac{1}{0.5} \left( \frac{0 + 0}{2} + \frac{0 + 0.09}{6} + \frac{1}{30} \frac{0.09 - 0.45}{2} \right) = -0.0270 \text{ g m}^{-3} \text{ h}^{-1}. \tag{A.3}
\]

In Table 2, it shows that

\[
\left[ \frac{dc_{in}}{dt} \right]_{2:30am} = -0.0270 \text{ g m}^{-3} \text{ h}^{-1}.
\]

<table>
<thead>
<tr>
<th>index no.</th>
<th>Time</th>
<th>( c_{in} )</th>
<th>( \Delta c_{in} )</th>
<th>( \Delta^2 c_{in} )</th>
<th>( \Delta^3 c_{in} )</th>
<th>( \Delta^4 c_{in} )</th>
<th>( \Delta^5 c_{in} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>-5</td>
<td>12:00 am</td>
<td>5.67</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>-0.24</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>-4</td>
<td>12:30 am</td>
<td>5.43</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>-0.09</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>-3</td>
<td>01:00 am</td>
<td>5.34</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>-0.09</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>-2</td>
<td>01:30 am</td>
<td>5.34</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>0</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>-1</td>
<td>02:00 am</td>
<td>5.34</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>0</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>0</td>
<td>02:30 am</td>
<td>5.34</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>0</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>03:00 am</td>
<td>5.34</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>0.09</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>03:30 am</td>
<td>5.43</td>
<td></td>
<td></td>
<td>-0.18</td>
<td></td>
<td>0.54</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>-0.09</td>
<td></td>
<td>0.27</td>
<td></td>
<td>0.9</td>
</tr>
<tr>
<td>3</td>
<td>04:00 am</td>
<td>5.34</td>
<td></td>
<td></td>
<td>0.09</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>0</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>04:30 am</td>
<td>5.34</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 5. Difference table.

**Nomenclature**

- \( A \) area, m\(^2\)
- \( c \) vapour content, kg m\(^{-3}\)

www.intechopen.com
specific heat, $J \, kg^{-1} \, K^{-1}$

moisture diffusion coefficient, $m^2 \, s^{-1}$

moisture generation rate, $kg \, s^{-1}$

surface moisture transfer coefficient, $m \, s^{-1}$

surface heat transfer coefficient, $W \, m^{-2} \, K^{-1}$

ventilation rate, $s^{-1}$

solar heat flux, $W \, m^{-2}$

heat transfer rate between envelope and indoor air, $W$

moisture transfer rate between envelope and indoor air, $kg \, s^{-1}$

time, $s$

temperature, $K$

volume, $m^3$

space co-ordinate, $m$

overall moisture transfer coefficient, $m \, s^{-1}$

thermal conductivity, $W \, m^{-1} \, K^{-1}$

density, $kg \, m^{-3}$

8. References


Haverinen, U. (2002). *Modeling moisture damage observations and their association with symptoms* [thesis], National Public Health Institute, Department of Environmental Health, University of Kuopio.
Moisture and Estimation of Moisture Generation Rate


Hite, SC. & Bray, JL. (1948). Research in humidity control. *Research Series No. 106*, Purdue University, Engineering Experiment Station, Lafayette, USA


www.intechopen.com


www.intechopen.com
The atmosphere may be our most precious resource. Accordingly, the balance between its use and protection is a high priority for our civilization. While many of us would consider air pollution to be an issue that the modern world has resolved to a greater extent, it still appears to have considerable influence on the global environment. In many countries with ambitious economic growth targets the acceptable levels of air pollution have been transgressed. Serious respiratory disease related problems have been identified with both indoor and outdoor pollution throughout the world. The 25 chapters of this book deal with several air pollution issues grouped into the following sections: a) air pollution chemistry; b) air pollutant emission control; c) radioactive pollution and d) indoor air quality.

How to reference

In order to correctly reference this scholarly work, feel free to copy and paste the following:
